

# UHECR and HADRONIC INTERACTIONS

Paolo Lipari

“Highlights of Astroparticle Physics”  
In memory of Gianni Navarra  
Torino 20<sup>th</sup> september 2010

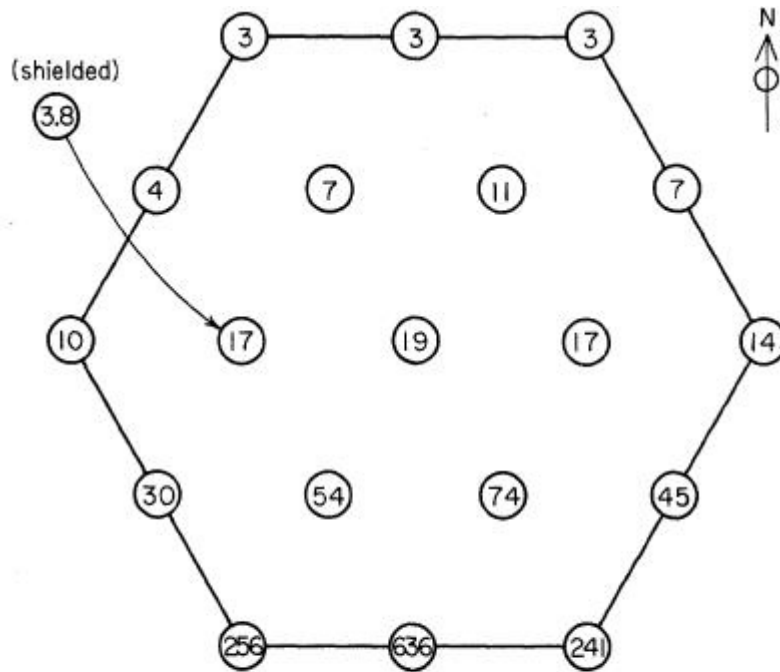
EXTREMELY ENERGETIC COSMIC-RAY EVENT\*

John Linsley, Livio Scarsi,<sup>†</sup> and Bruno Rossi

Laboratory for Nuclear Science, Massachusetts Institute of Technology, Cambridge, Massachusetts

(Received April 12, 1961)

# Energy



it follows on any reasonable shower model that the energy of the primary particle was about  $10^{19}$  ev. Taking the usual estimate  $3 \times 10^{-6}$  gauss for the galactic magnetic field, one finds the radius of curvature of the path of a proton of such energy to be about  $10^4$  light years. Since, according to current estimates, the radius of the galactic halo is only about five times this value, while the thickness of the galactic disk is about five or ten times smaller, it seems certain that the primary particle acquired its energy outside our galaxy.

An important question is whether the primary particle was a proton or a heavier nucleus.

# Mass A

Hadronic interaction Modeling

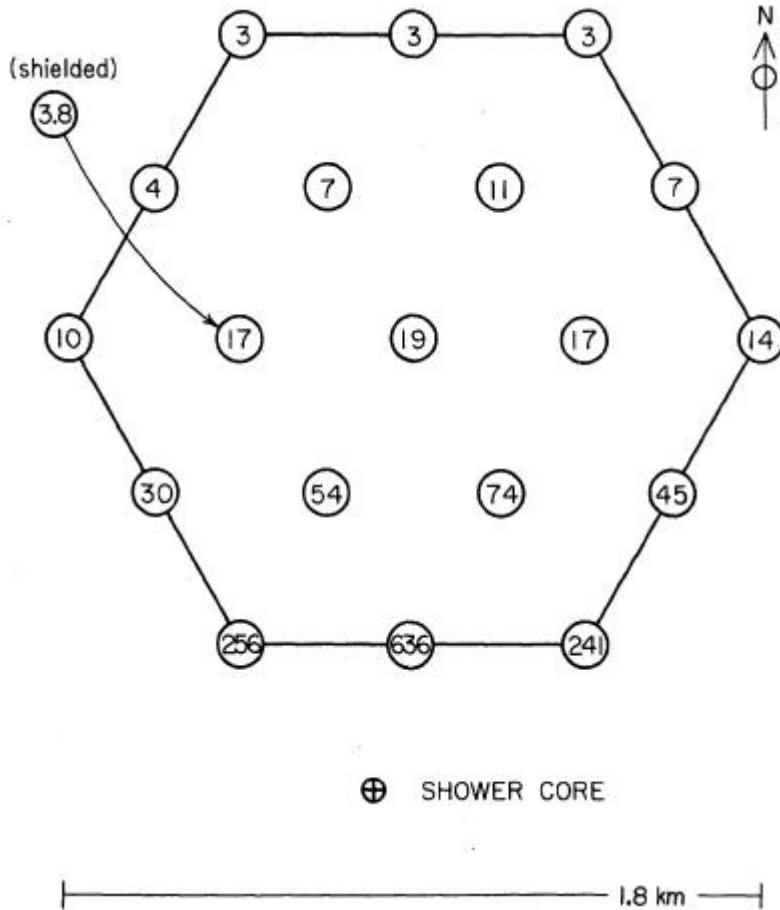
Measure a single slice of the shower at the ground

EXTREMELY ENERGETIC COSMIC-RAY EVENT\*

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Hadronic interaction  
Modeling

$e^{\pm} \quad \gamma$

$\mu^{\pm}$

hadrons

Different components

Measure a single slice of  
the shower at the ground

# “Multi Components Air Shower Array”

## EASTOP at Gran Sasso

[A very important “jump of quality”:  
Electromagnetic part  
Hadronic calorimeter  
Cherenkov light  
Deep underground Muons ]

Hadronic Model  
dependence.

# “Multi Components Air Shower Array”

## EASTOP at Gran Sasso

[A very important “jump of quality”:

Electromagnetic part

Hadronic calorimeter

Cherenkov light

Deep underground Muons (unique !!) ]

Hadronic Model  
dependence.

A beautiful idea !!

That perhaps has not received the recognition it deserves.

Very valuable results that it would be useful

To re-analyze with the best “modeling instruments”

We are developing now.

# “Multi Components Air Shower Array”

## EASTOP at Gran Sasso

[A very important “jump of quality”:  
Electromagnetic part  
Hadronic calorimeter  
Cherenkov light  
Deep underground Muons ]

## KASCADE (Karlsruhe)

“competitors”  
and  
collaborators

## KASCADE-GRANDE

a “bridge to higher energy”

Common  
project  
New Results!

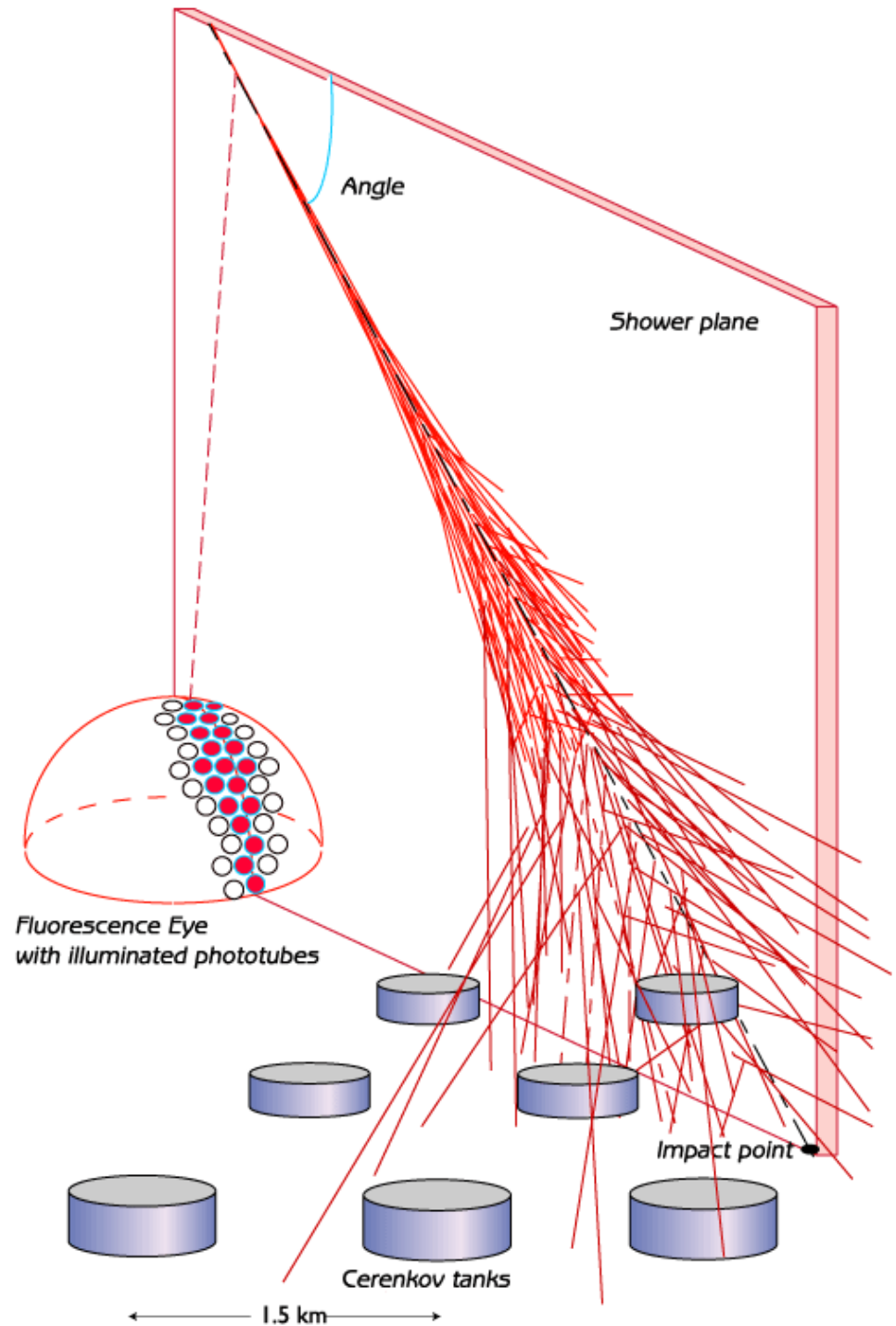
# The Fly's Eye Detector concept

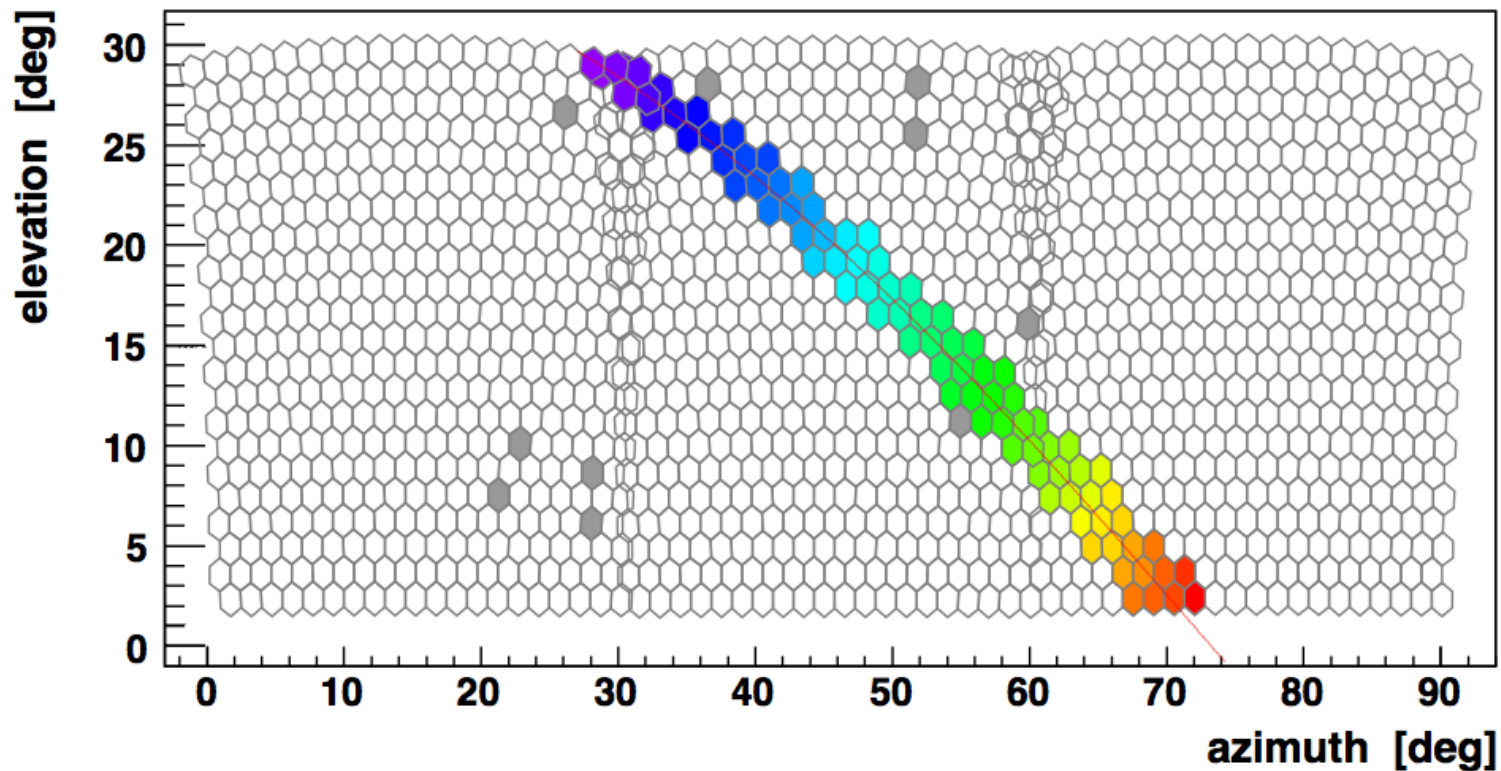


“Quasi-Calorimetric”  
Energy Measurement

Fluorescence Light

Artists View of Hybrid Set-Up





$$L(\Omega) \rightarrow F_{\gamma}(X) \rightarrow N_{e^{\pm}}(X)$$

Observed  
Light



Emitted  
Photons

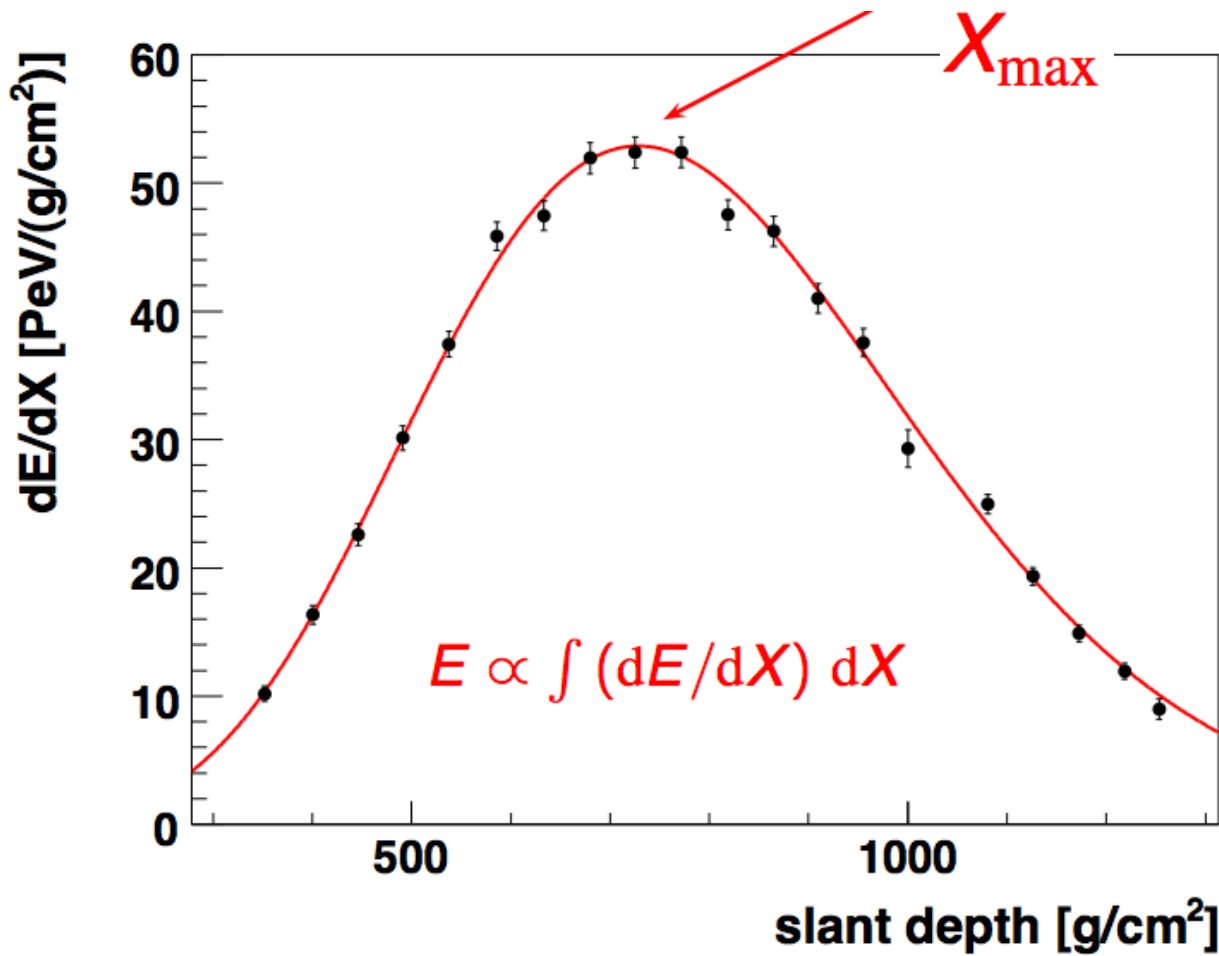


Shower  
Size

Geometry  
Atmospheric Absorption

Fluorescence  
Yields

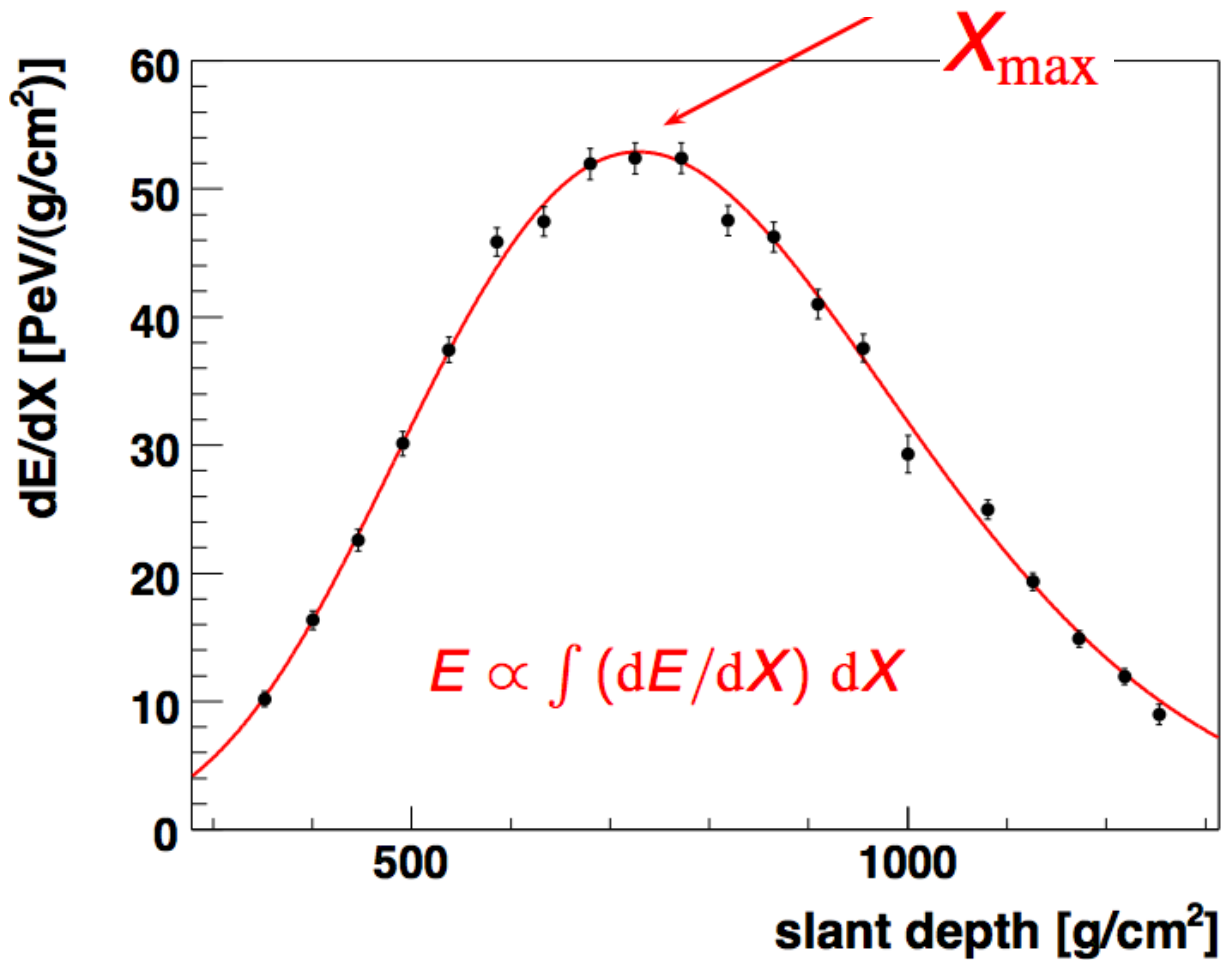




$$E_{\text{ionization}} = \int dX N_e(X) \left\langle -\frac{dE}{dX} \right\rangle$$

Small  
Model  
dependence

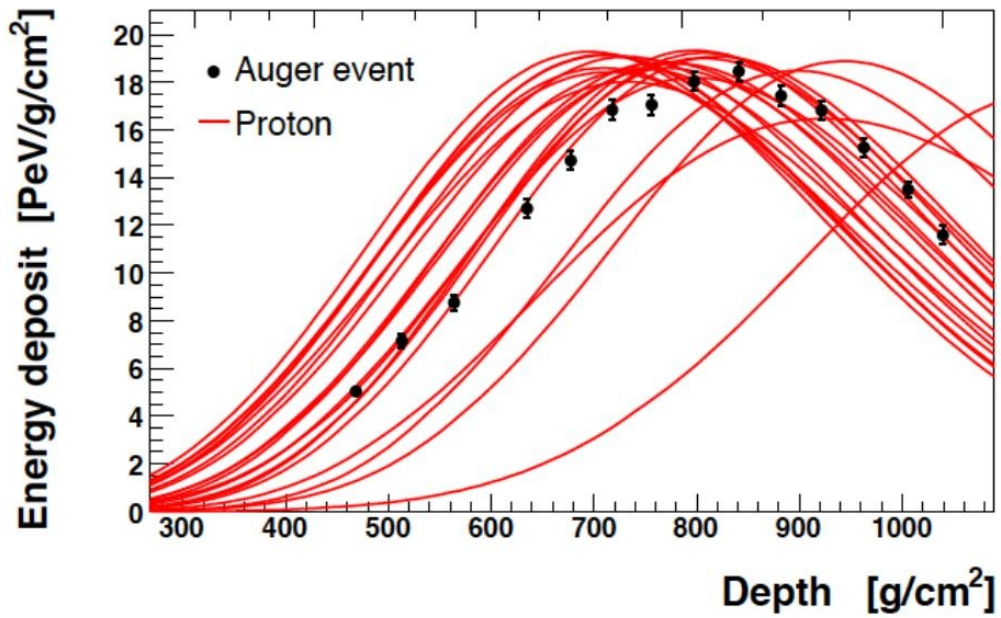
$$E_{\text{tot}} = E_{\text{ionization}} + E_{\nu} + E_{\mu} + E_{\text{ground}}$$



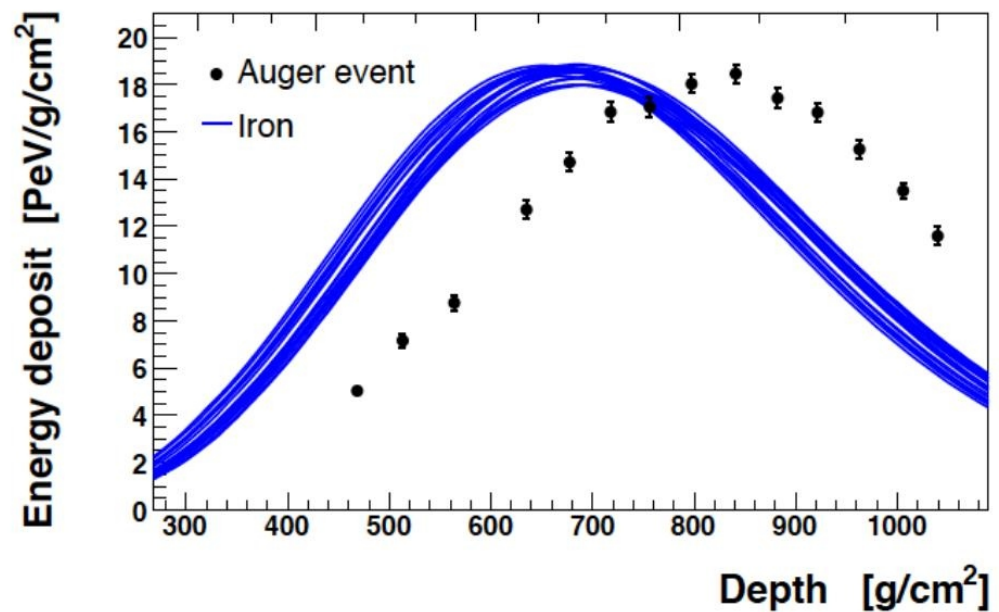
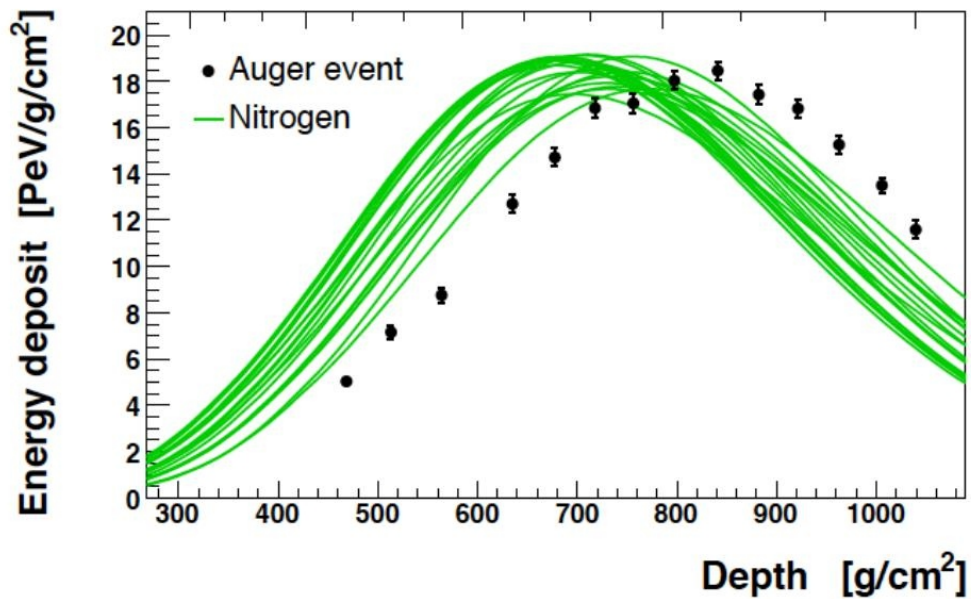
Area  $\propto$  Energy

Shape depends on :

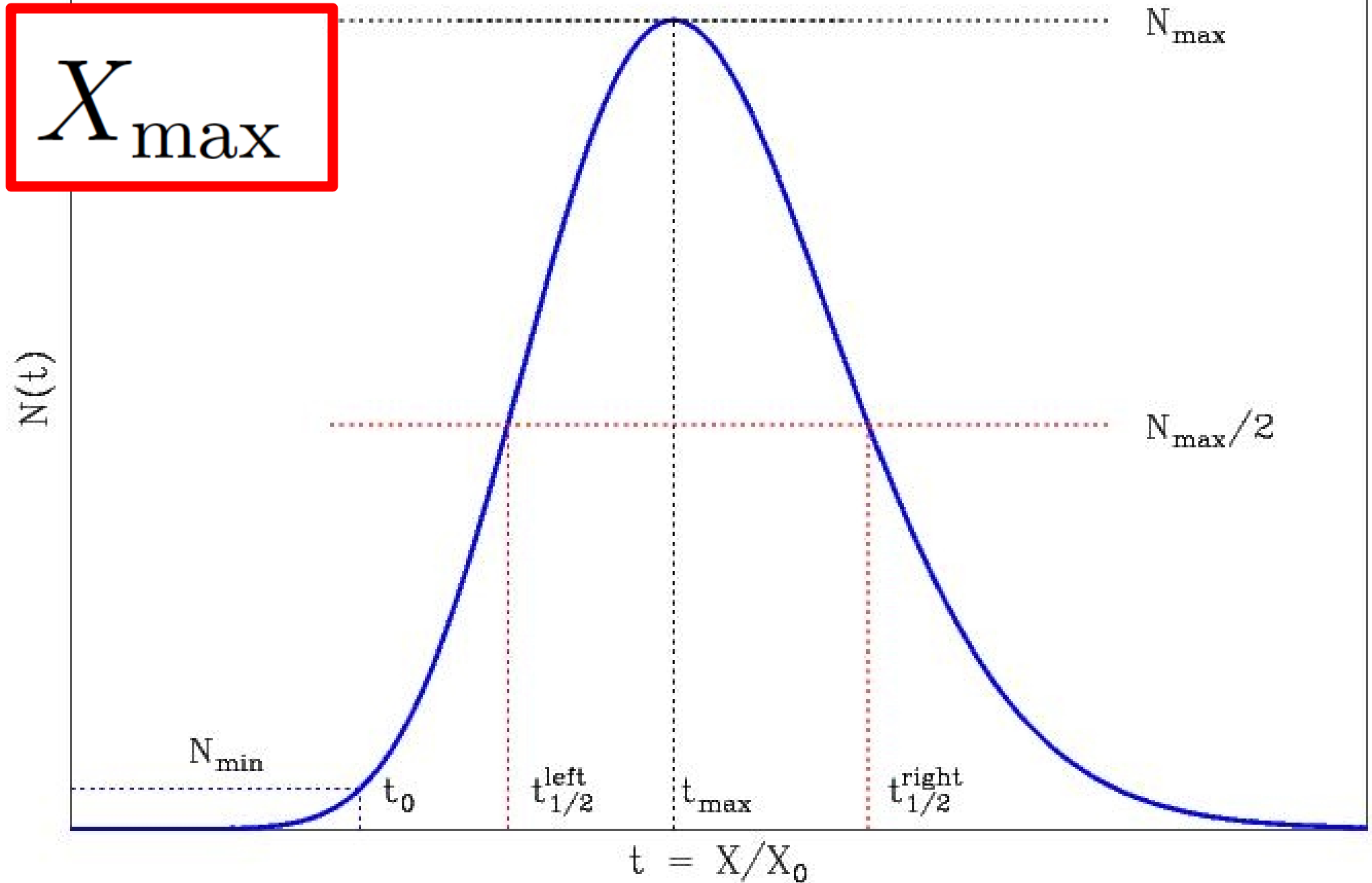
- Primary Identity
- Interaction Model



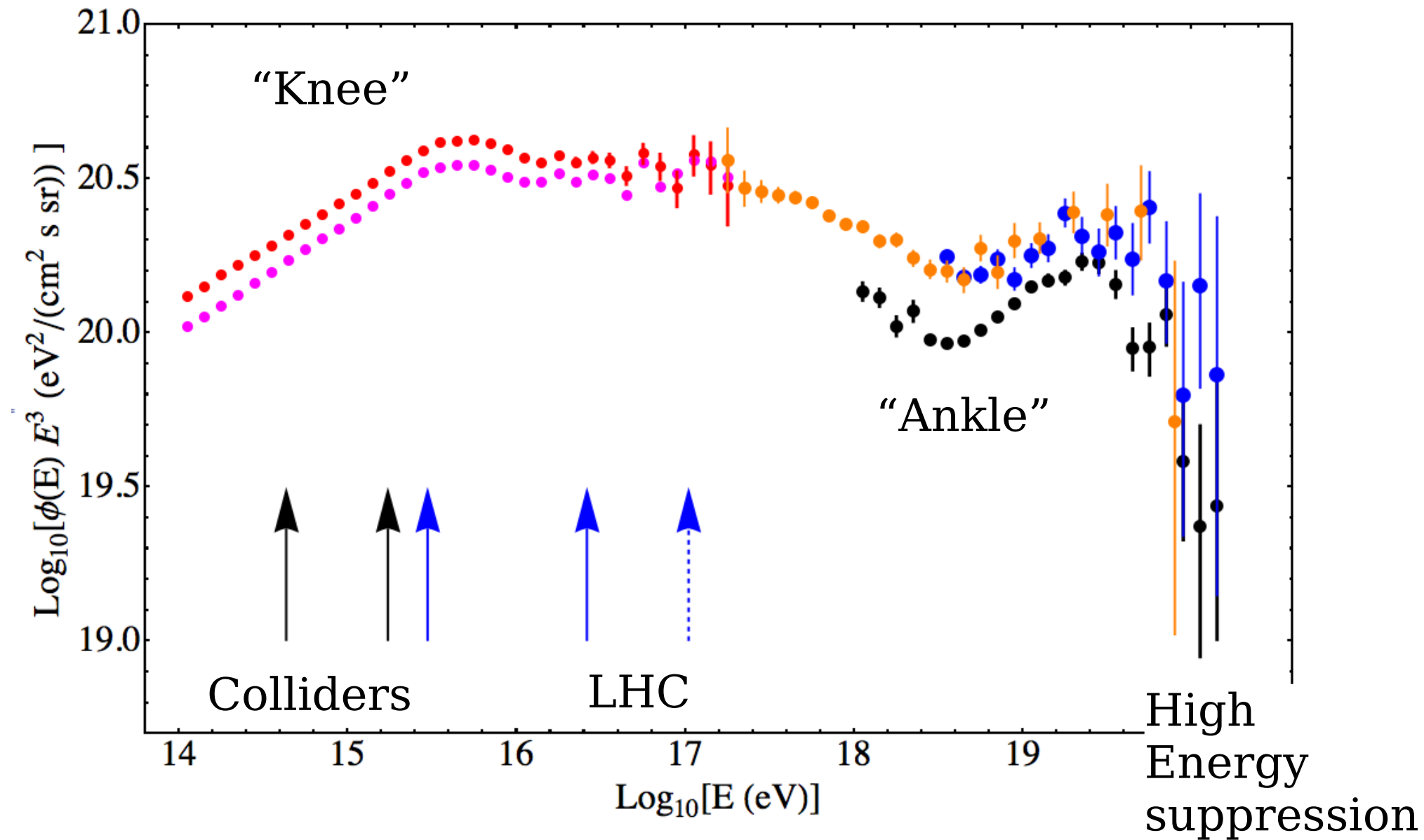
$$E \simeq 10^{20} \text{ eV}$$



# Longitudinal Development Shape studies



# Structure in the energy spectrum



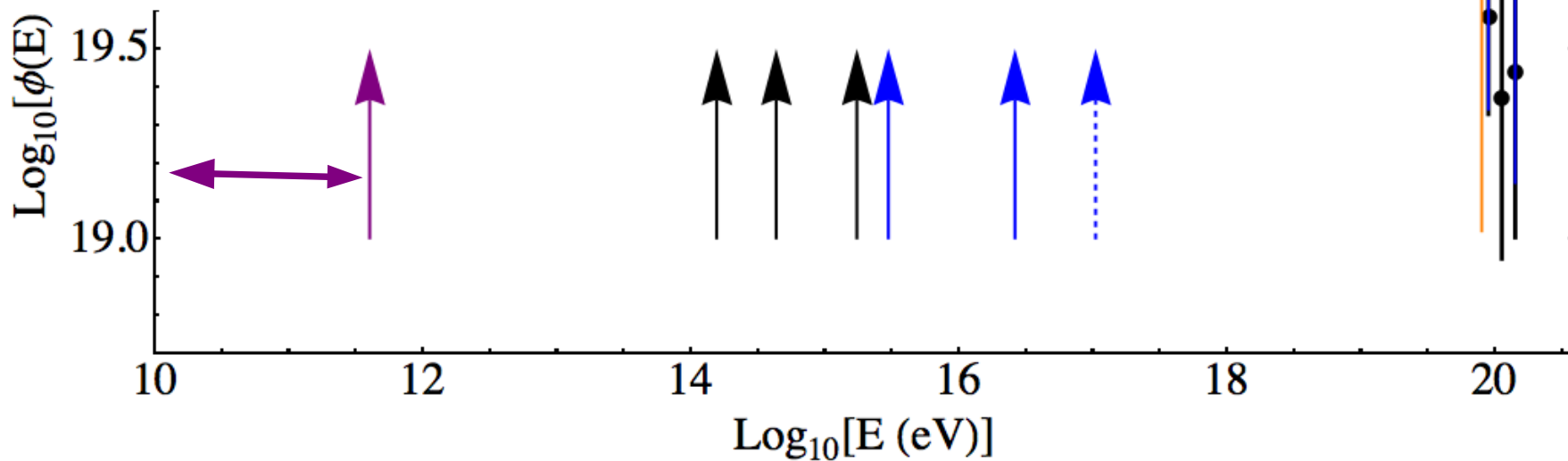
“Fixed Target” measurements

Nucleus targets

Pion/kaon projectiles.

Cover entire  
kinematical Phase Space  
[including fast particles  
in forward region]

## COLLIDERS



Fixed  
Target

Cern  
Tevatron

LHC

# COMPOSITION of UHECR

Very high astrophysical importance

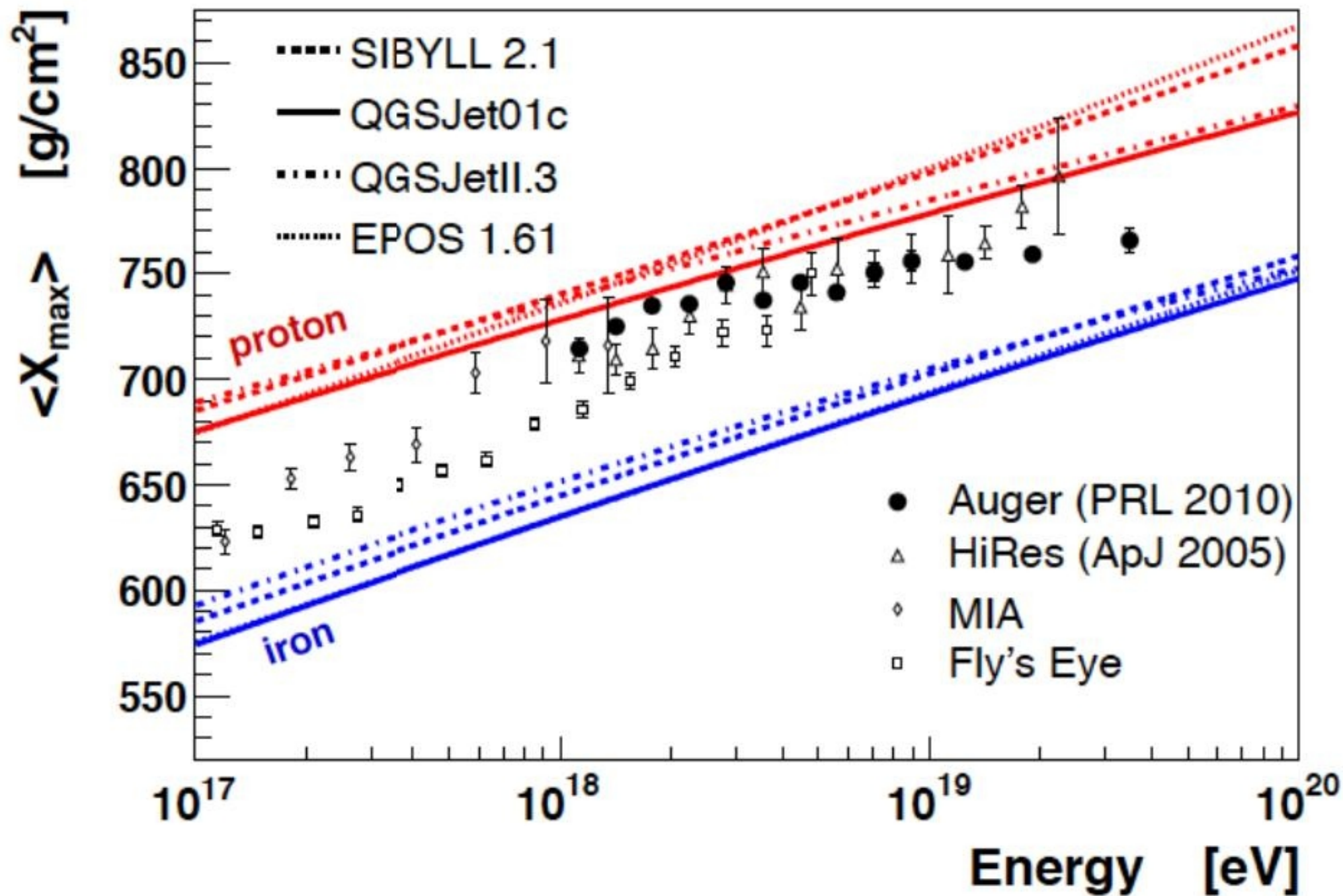
Controversial - inconsistent observations.

$X_{\max}$

Fluctuations of  $X_{\max}$

Other methods

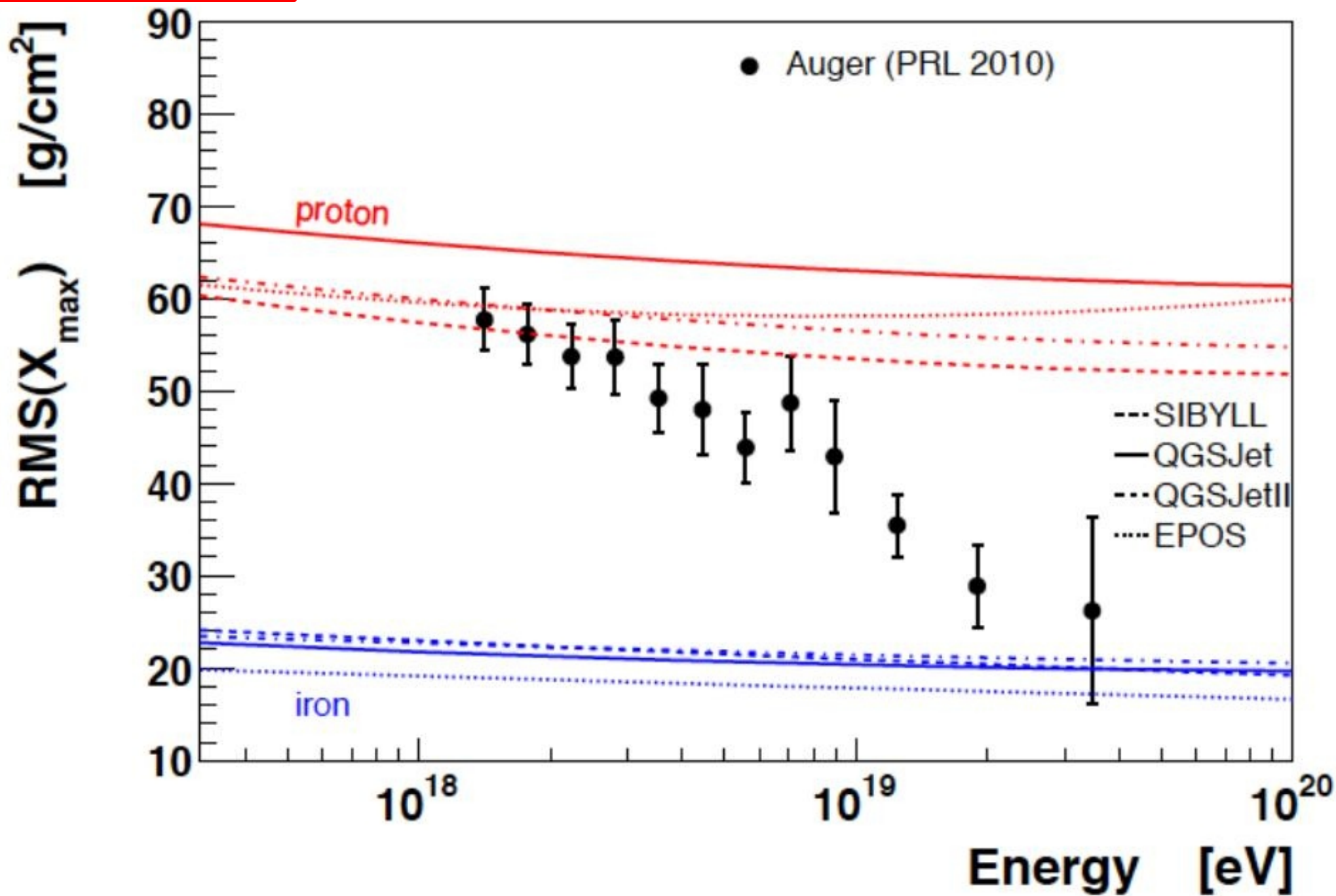
# AUGER



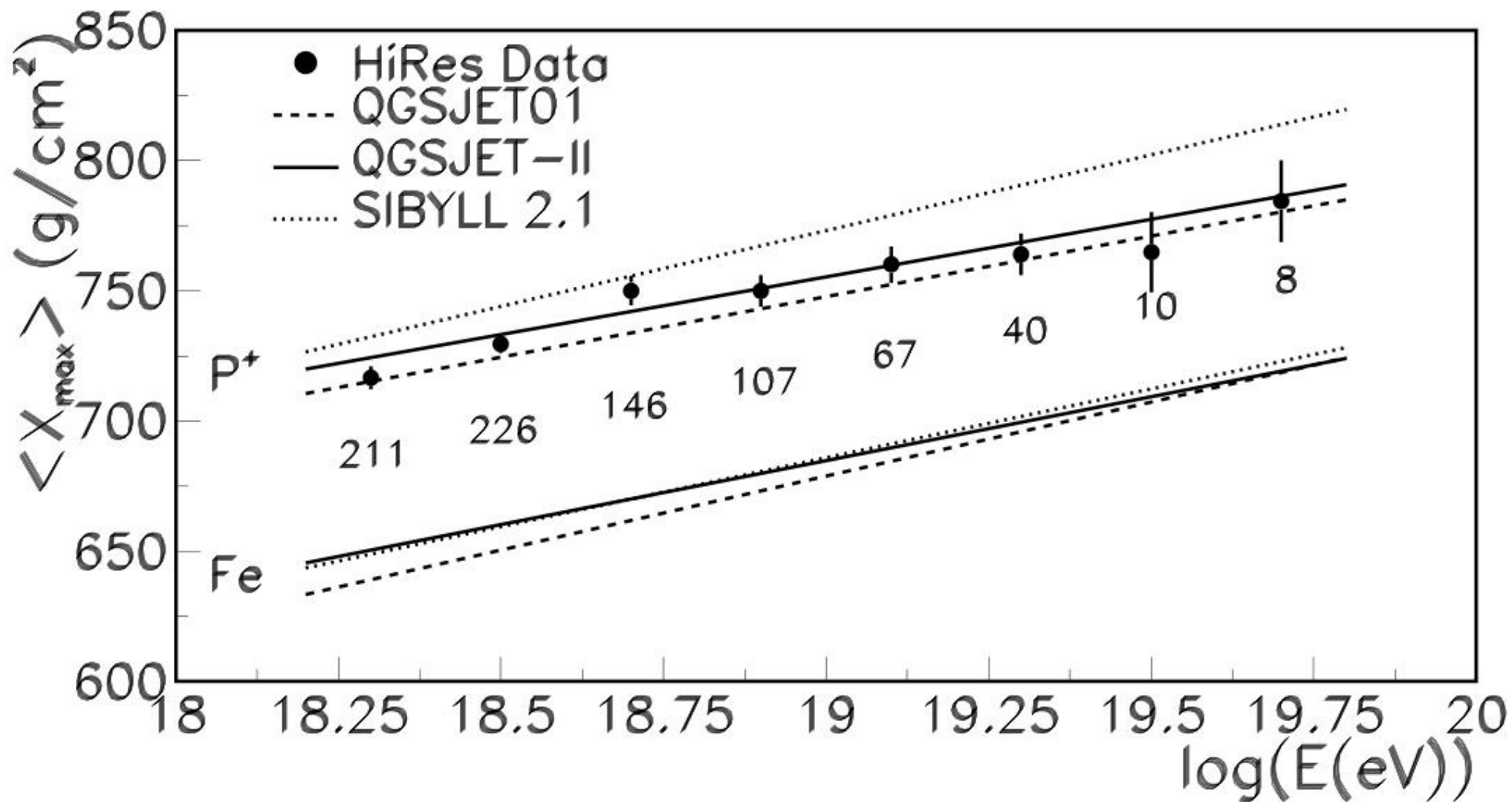


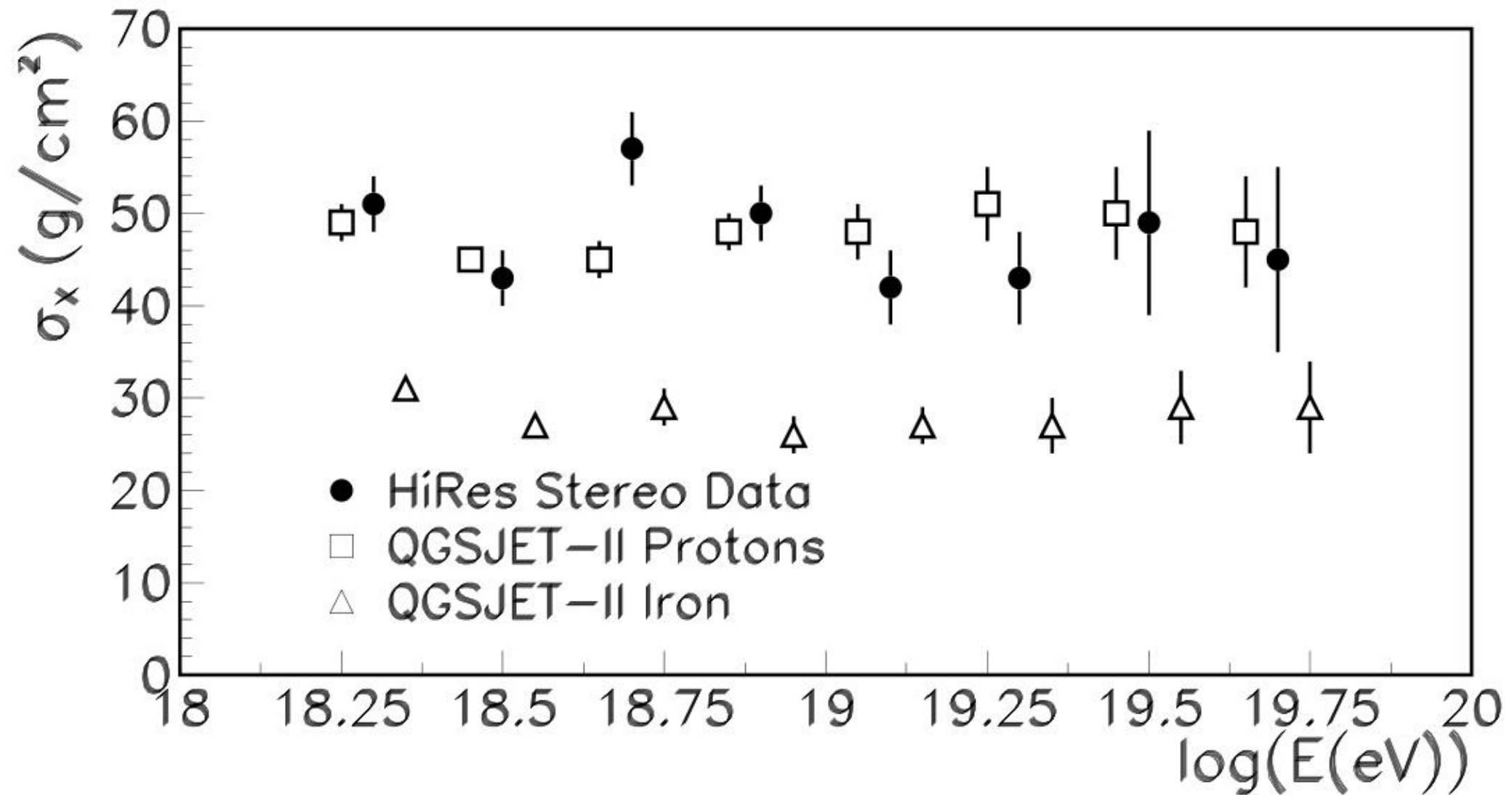
# AUGER

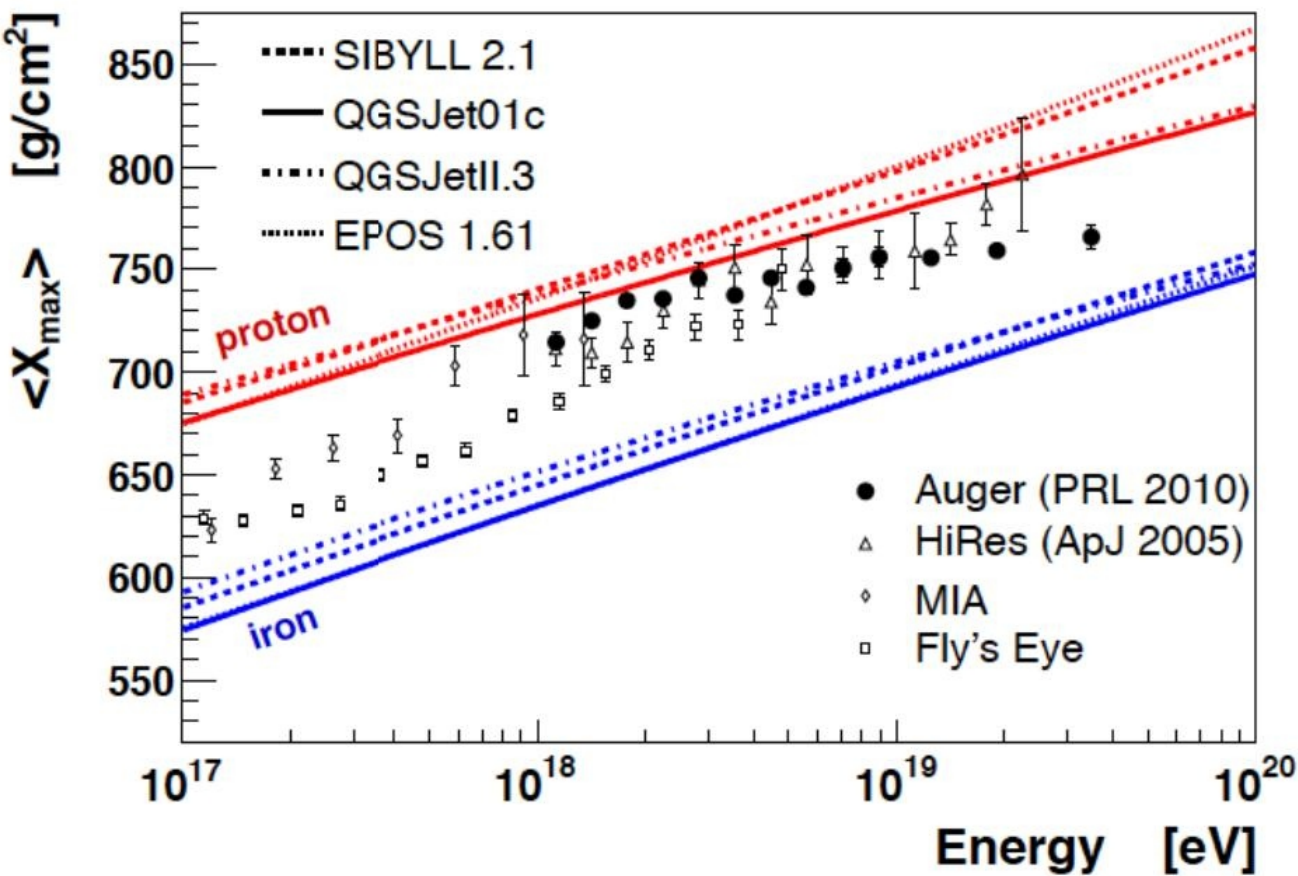
## Shower fluctuations



HiRes 2009







The “theory curves”  $\langle X_{\max}(E) \rangle$  are determined by the parameters that describe hadronic interactions. (and by their energy dependence).

Interaction Lengths  
 Multiplicity  
 Inclusive Spectra  
 .....

Theoretical curves:

$$|\langle X_p \rangle_{\text{Model 1}} - \langle X_p \rangle_{\text{Model 2}}| \lesssim 20 \text{ g cm}^{-2}$$

$$10^{19} \text{ eV}$$

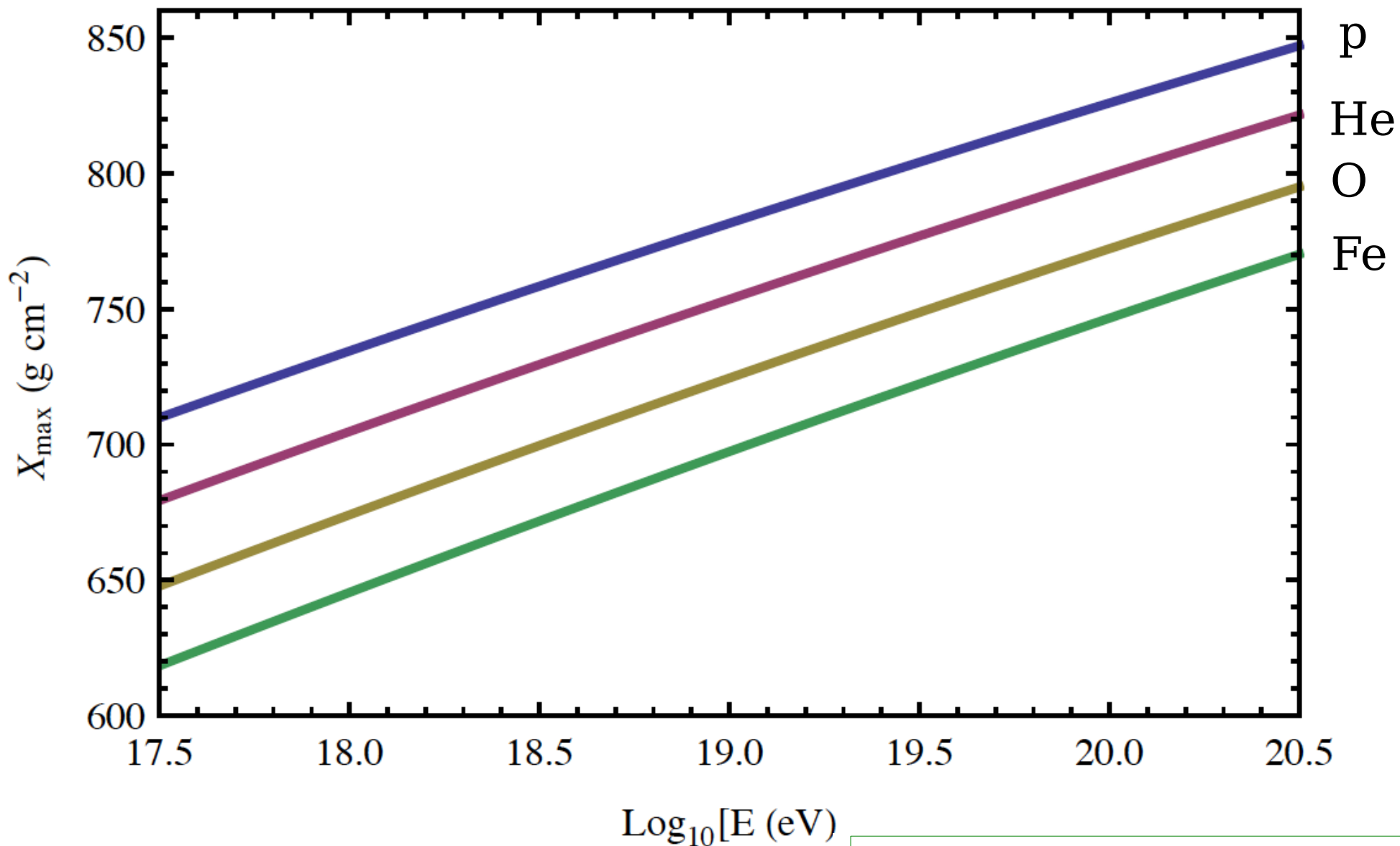
$$D_p = \frac{d\langle X_{\max} \rangle}{d \log_{10} E} \simeq 45 - 55 \text{ g cm}^{-2}$$

# $X_{\max}$ and the Composition of Cosmic Rays

$$\langle X_A(E) \rangle \simeq \left\langle X_p \left( \frac{E}{A} \right) \right\rangle$$

$$\langle X_p(E) \rangle \simeq X_0 + D_p \log_{10} E$$

$$\langle X_A \rangle \simeq \langle X_p \rangle - D_p \log_{10} A$$

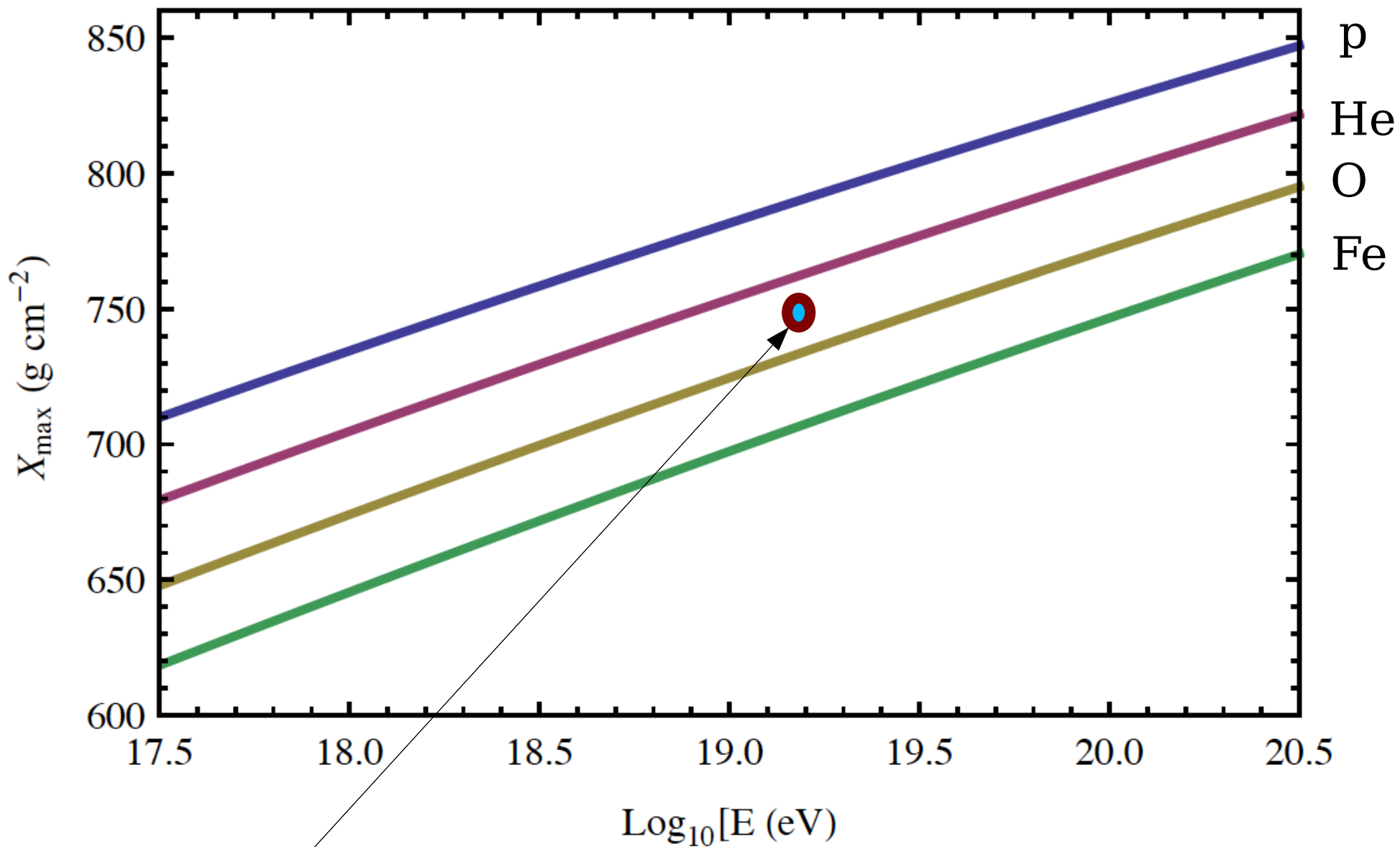


$$\langle X_A \rangle \simeq \langle X_p \rangle - D_p \log_{10} A$$

$$\langle X_{\text{He}} \rangle \simeq \langle X_p \rangle - 30 \text{ g cm}^{-2}$$

$$\langle X_{\text{O}} \rangle \simeq \langle X_p \rangle - 60 \text{ g cm}^{-2}$$

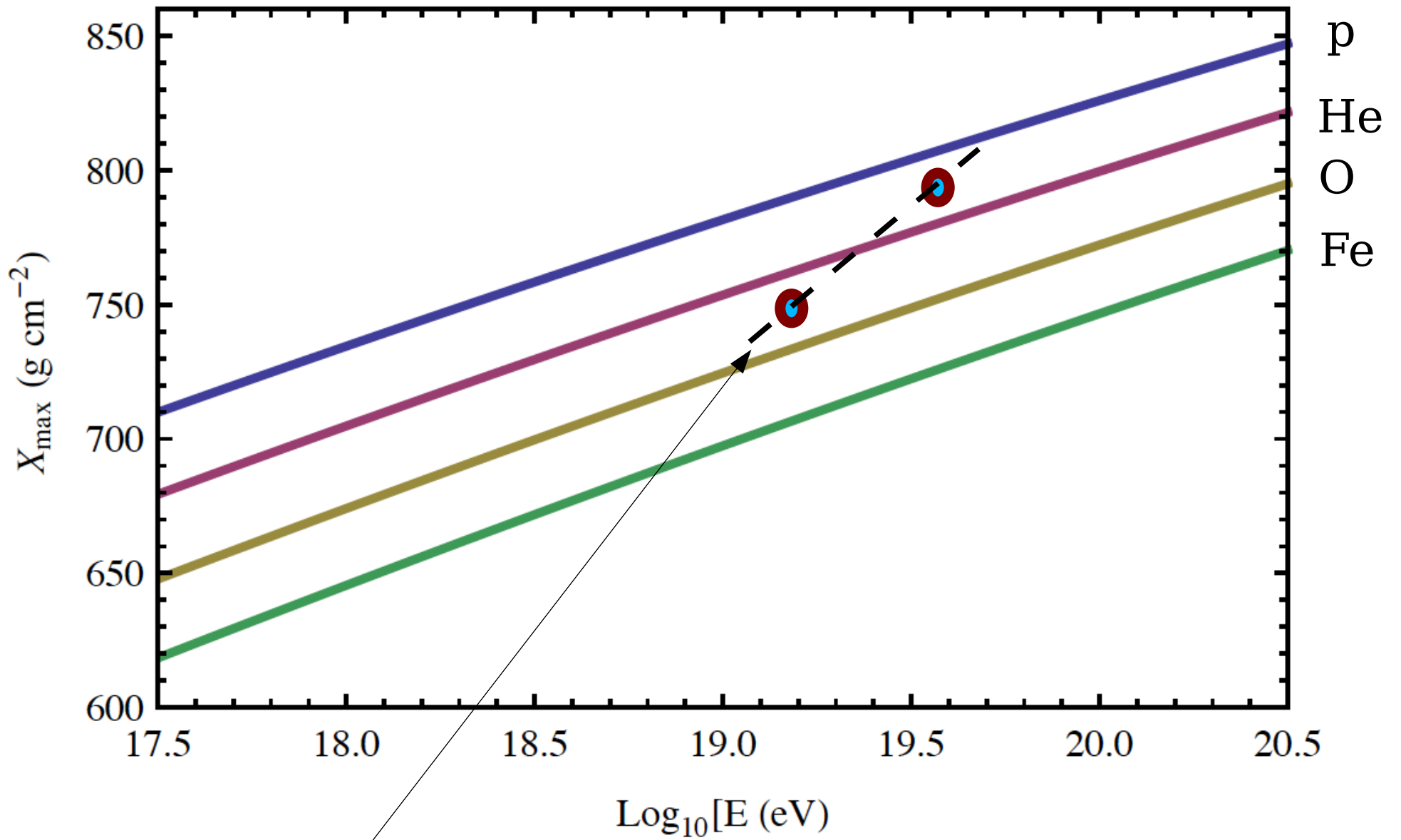
$$\langle X_{\text{Fe}} \rangle \simeq \langle X_p \rangle - 90 \text{ g cm}^{-2}$$



Measurements of

$\langle \log A \rangle$

$$\langle \ln A \rangle_E = \frac{\sum_A \phi_A(E) \ln A}{\sum_A \phi_A(E)}$$



Measurements of Composition evolution.



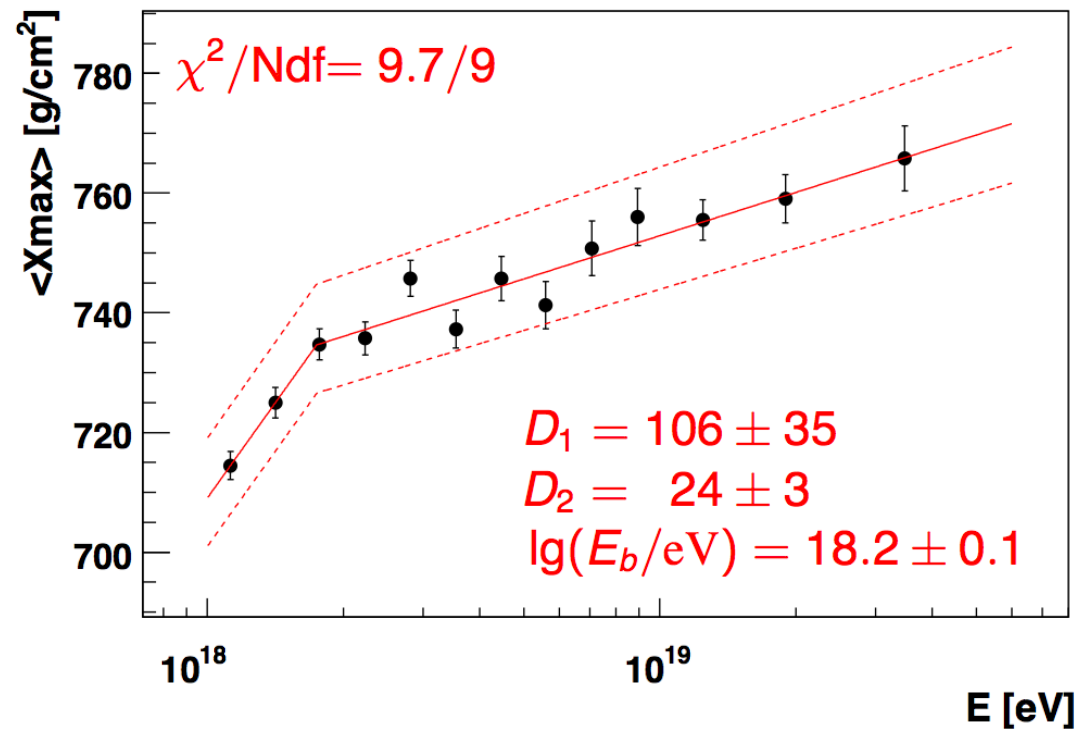
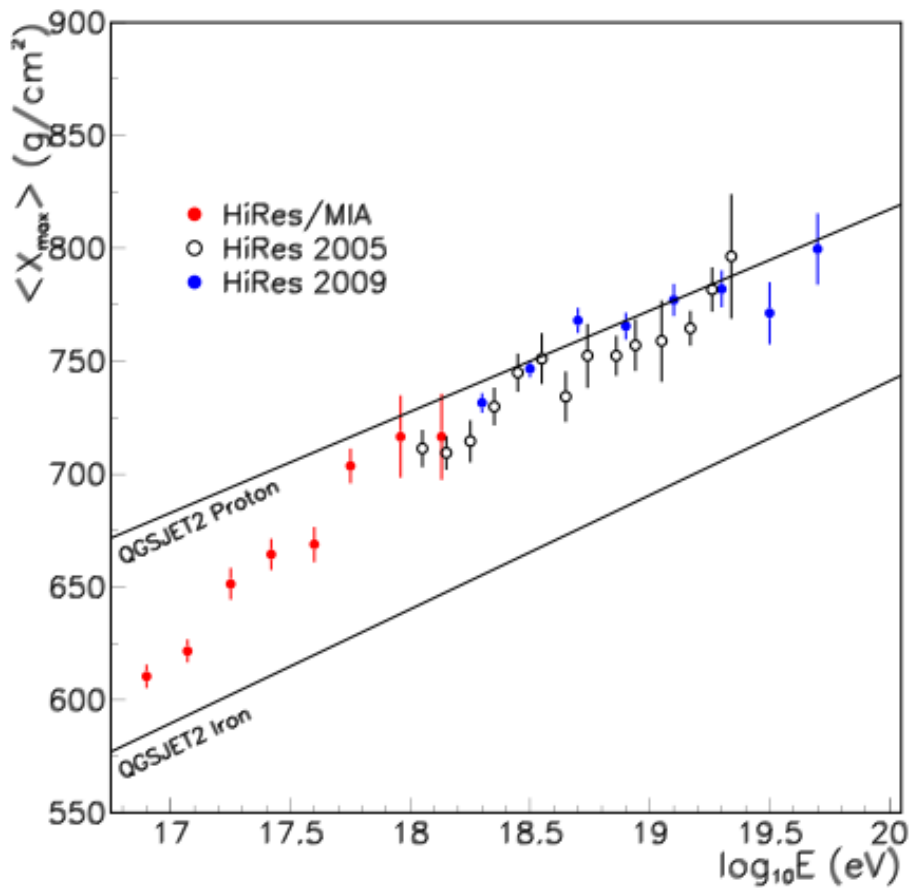
Obtain the average mass  
and its variation  
with energy

$$\langle \ln A \rangle_E = \frac{\sum_A \phi_A(E) \ln A}{\sum_A \phi_A(E)}$$

$$\langle \ln A \rangle_E = \frac{\langle X_{\max}(E) \rangle - X_p(E)}{D_p}$$

$$\frac{d\langle \ln A \rangle_E}{d \ln E} = 1 - \frac{D_{\text{exp}}}{D_p}$$

# Importance of “CORNERS”



Abrupt change in the  
variation of the properties  
of hadronic interactions  
with energy

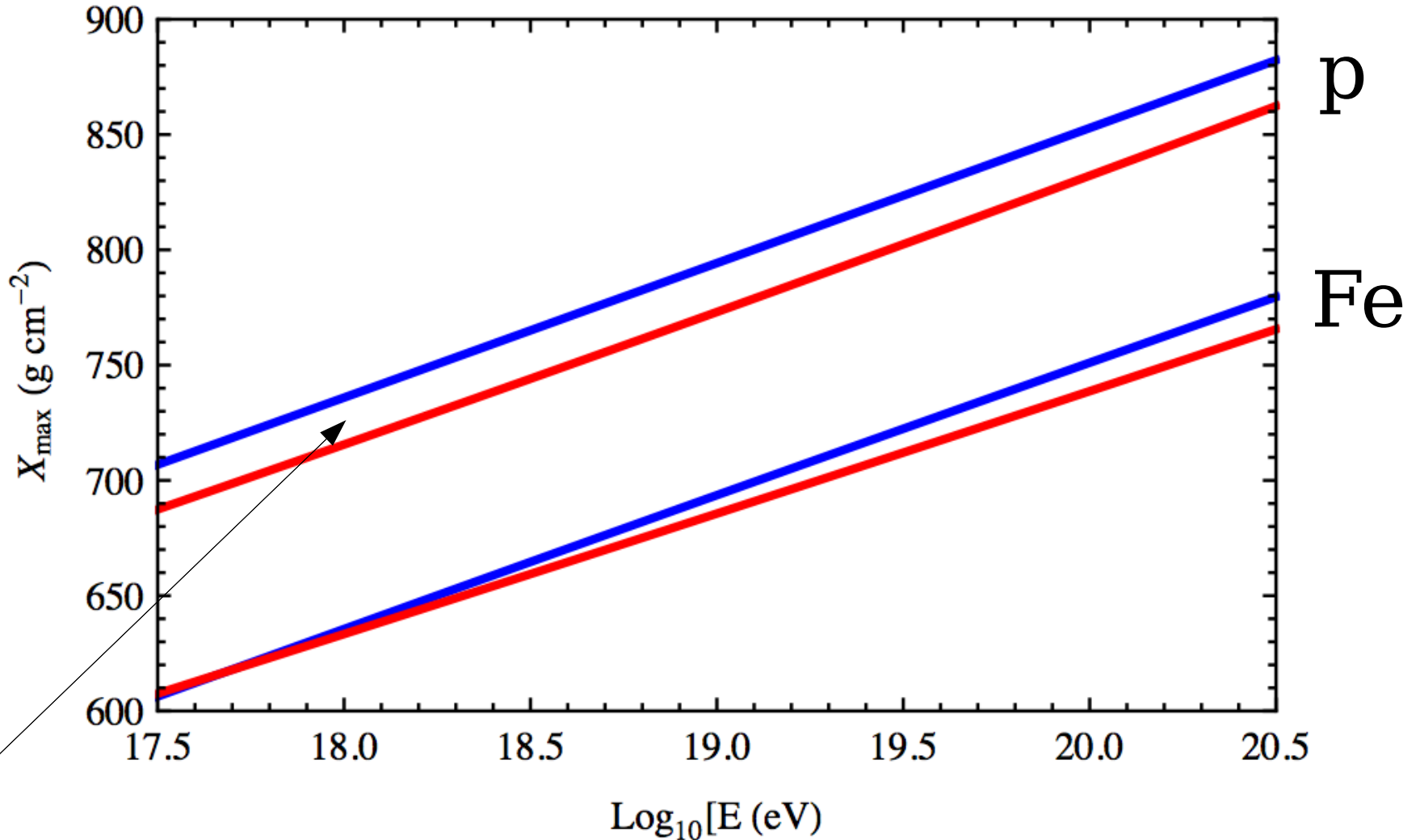
Abrupt change in  
the composition evolution.

Fig. 25.— Comparison of current HiRes stereo  $\langle X_{max} \rangle$  results with results from the HiRes-prototype/MIA hybrid (Abu-Zayyad et al. 2001) and previously published HiRes stereo results (Abbasi et al. 2005).

# Problems in comparing Auger and HiRes measurements:

Comparison of the “Theory curves”  
(same model: Sibyll 2.1)

Auger (Blue)  
HiRes (Red)



$20 \text{ g cm}^{-2}$  shift

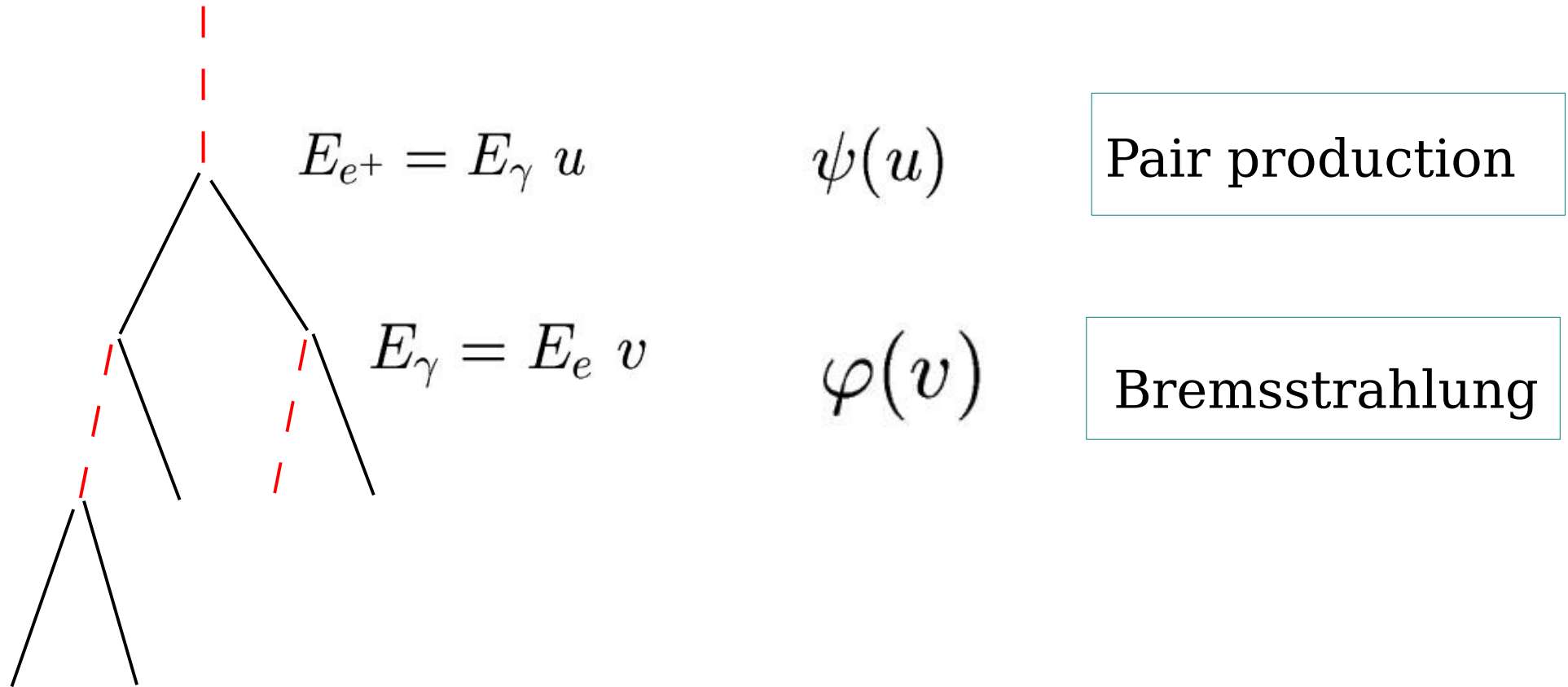
# Electromagnetic Showers

versus

# Hadronic Showers

Toy model  
discussion.

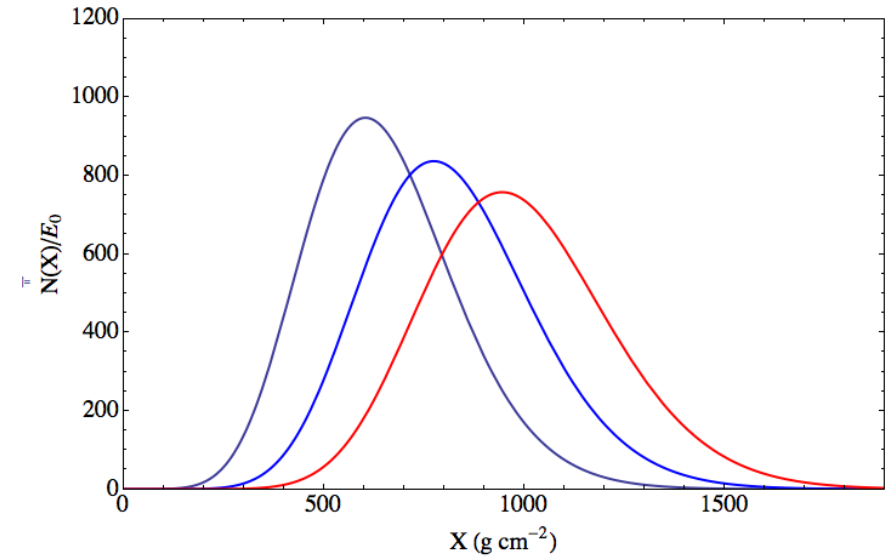
# Electromagnetic Shower



Radiation Length  
(Energy independent)

Vertices :  
theoretically understood  
(and scaling)

# Electromagnetic Showers



$$X_{\max}(E) \simeq \lambda_{\text{rad}} \ln \left( \frac{E}{\varepsilon} \right)$$

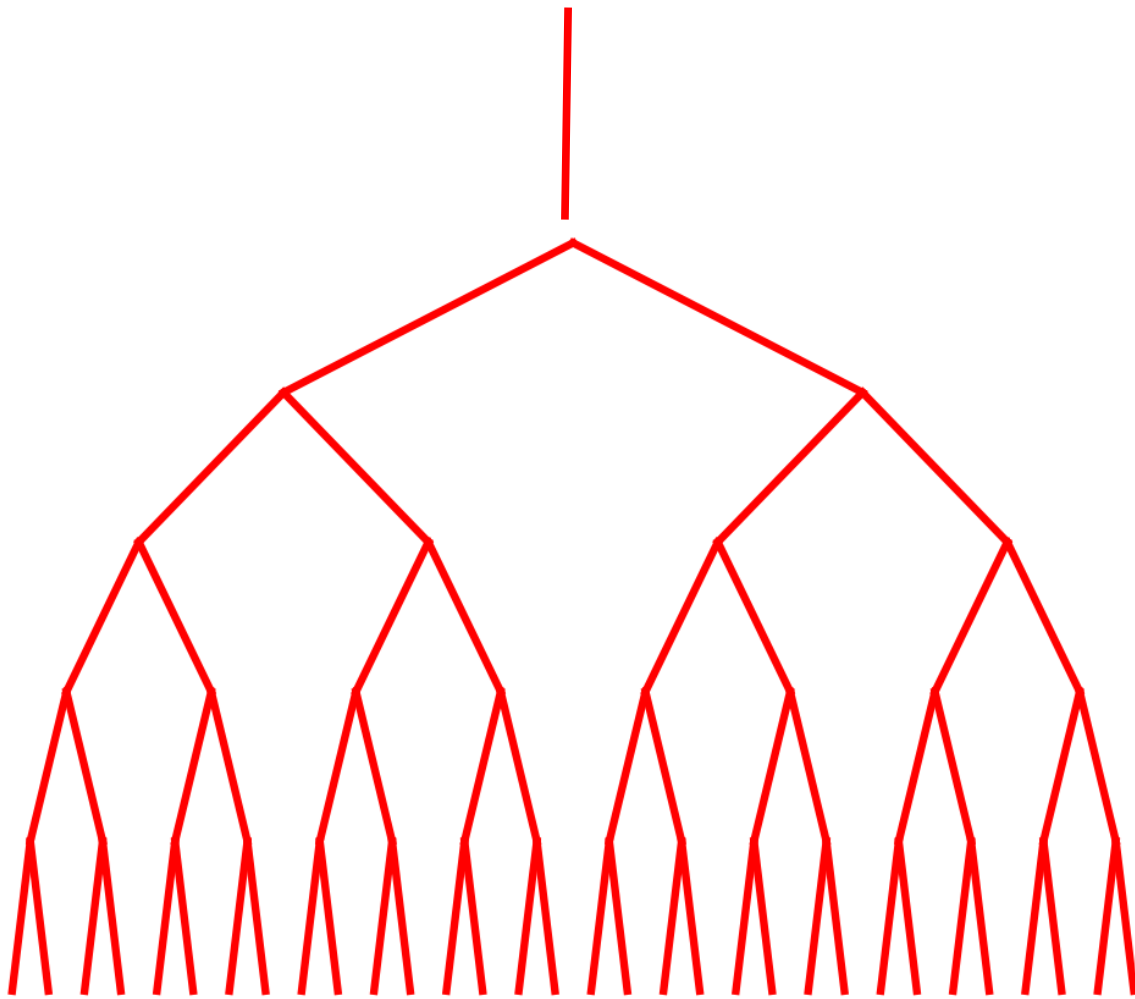
Logarithmic growth of the penetration.

$$N_{\max}(E) \simeq \frac{E}{\varepsilon} \frac{1}{\sqrt{\ln(E/\varepsilon)}}$$

Energy Conservation

Elongation rate = 85  $(\text{g/cm}^2)/\text{decade}$

Heitler toy model  
for electromagnetic  
showers



“Electron-photon”  
particle

Splitting length  $\lambda$   
Critical energy  $\varepsilon$

$$N(X, E) = 2^{X/\lambda}$$

$$N_{\max}(E) = \frac{E}{\varepsilon}$$

$$X_{\max}(E) = \lambda \log_2 \left( \frac{E}{\varepsilon} \right)$$

Electromagnetic showers:

$$\langle X_{\max}(E) \rangle = X_0 + D_\gamma \log E$$

$$D_\gamma = \ln 10 X_{\text{rad}} \simeq 85 \text{ g cm}^{-2}$$

Fluctuations:

$$\sigma_X^2(\gamma, E) = \text{constant}$$

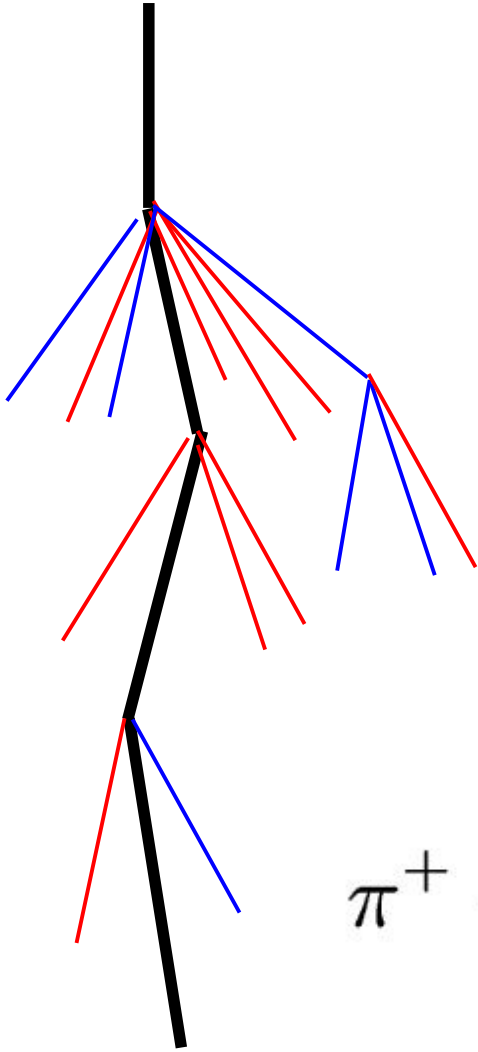
$$\sigma_X^2(\gamma, E) \simeq 1.1 X_{\text{rad}} \simeq 40 \text{ g cm}^{-2}$$



# Proton Shower

Vertices : theoretically not  
Understood

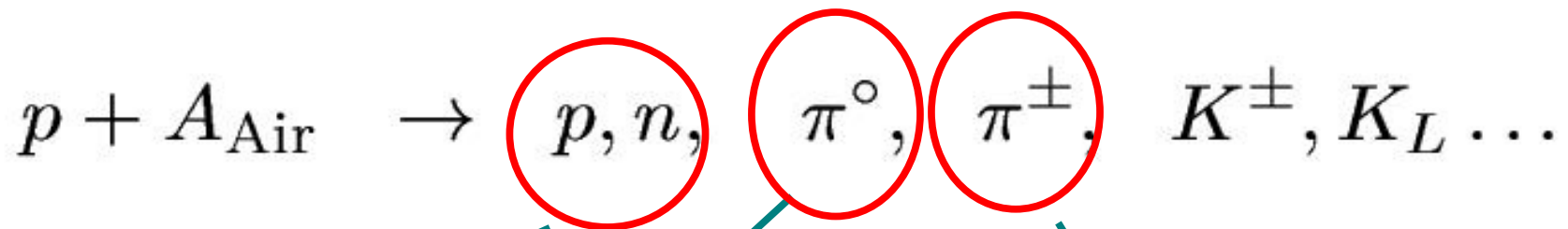
(and energy dependent)



$$\pi^0 \rightarrow \gamma\gamma$$

$$\pi^+ \rightarrow \mu^+ \nu_\mu$$

# HADRONIC INTERACTIONS



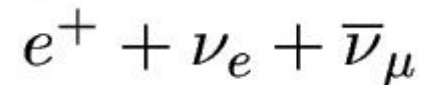
Leading nucleon  
~ 50% of energy

$\pi^0 \rightarrow \gamma\gamma$   
Electromagnetic  
Shower

**Decay**



↓

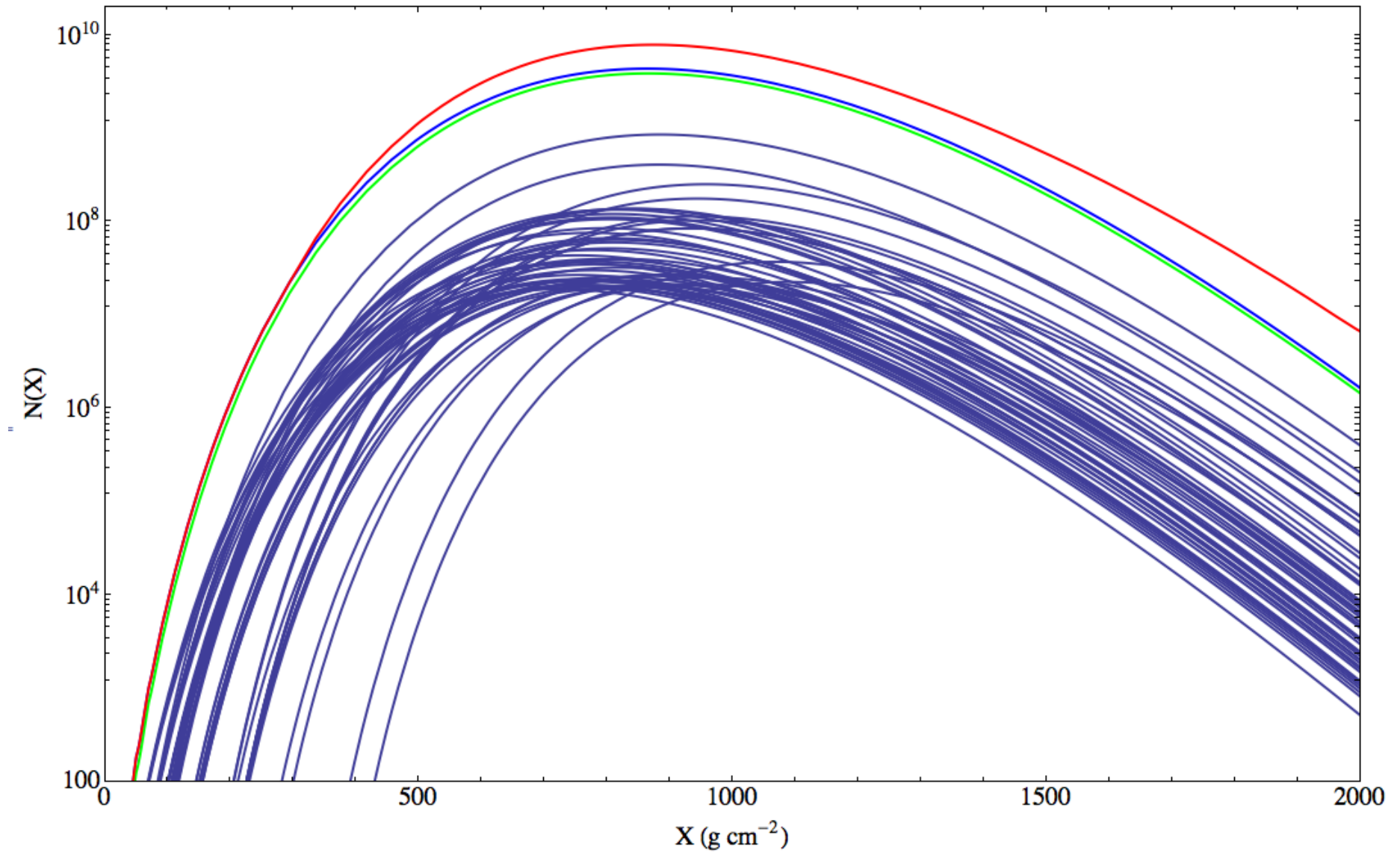


**Interaction**

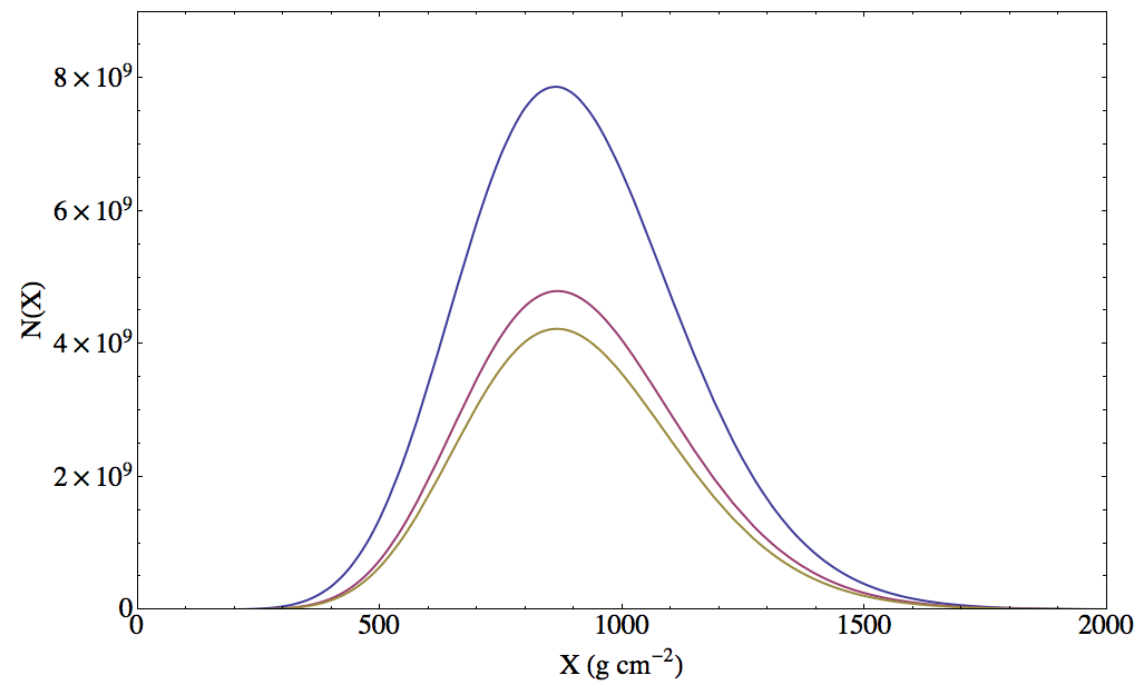
Inclusive spectra  
of secondary particles



One single proton Shower:  $E_0 = 10^{19}$  eV

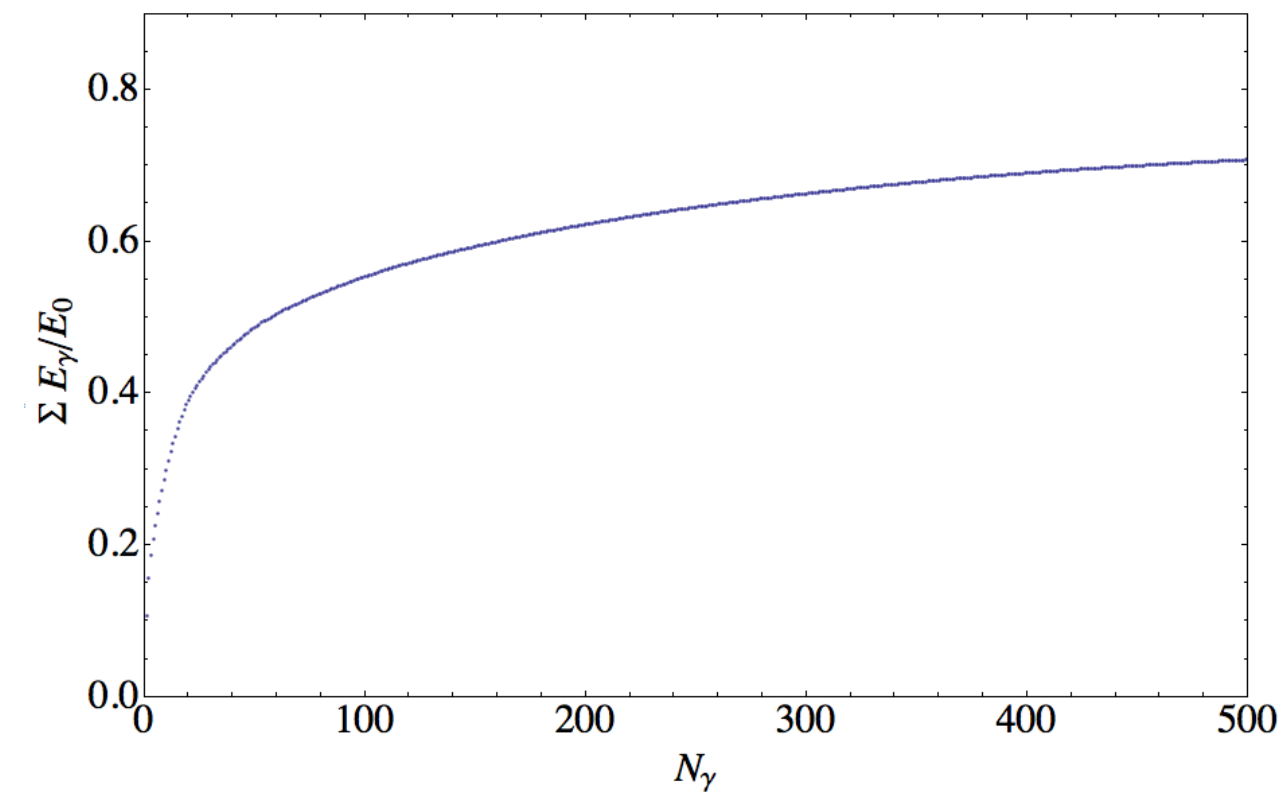


50 highest energy individual sub-showers



100 photons  $\sim 50\%$  of energy  
1000 photons  $\sim 70\%$  of energy

Approximately 100 photons  
in 30-40 interaction vertices  
control the structure of the  
shower:  $x \sim 0.1$



# Toy Model for hadronic shower

$$p + \text{air} \rightarrow \binom{n}{2} \pi^0 \rightarrow n \gamma$$

Energy equally divided among  $n$  photons.

$$E_\gamma \simeq \frac{E_0}{n}$$

$$\frac{dN_\gamma}{dz} = \sum_n P_n \delta \left[ z - \frac{1}{n} \right]_n$$

$$\langle X_{\max}^{(p)} \rangle = \langle X_{1\text{st}} \rangle + X_{\text{rad}} \left\langle \log \left( \frac{E_0}{n_\gamma \varepsilon} \right) \right\rangle$$

1<sup>st</sup> interaction

Development of  
photon shower  
of energy  $E/n$

$$\langle X_{\max}^{(p)} \rangle = \langle X_{1\text{st}} \rangle + X_{\text{rad}} \left\langle \log \left( \frac{E_0}{n_\gamma \varepsilon} \right) \right\rangle$$

$$\langle X_{\max}^{(p)} \rangle = \lambda_p + X_{\text{rad}} \log \left[ \frac{E_0}{\varepsilon} \right] - X_{\text{rad}} \langle \log n_\gamma \rangle$$

Interaction  
Length

Photon  
Shower

Particle production  
properties

$$\langle X_{\max}^{(p)} \rangle = \lambda_p + X_{\text{rad}} \log \left[ \frac{E_0}{\varepsilon} \right] - X_{\text{rad}} \langle \log n_\gamma \rangle$$

Interaction length

“Softness”

Elongation Rate

$$\frac{d\langle X_{\max}^{(p)}(E) \rangle}{d \log E} = X_{\text{rad}} + \frac{d\lambda_p(E)}{d \log E} - X_{\text{rad}} \frac{d\langle \log n_\gamma(E) \rangle}{d \log E}$$

Evolution with  
Energy of the  
Interaction length

Evolution with  
energy of the  
“softness” of the  
spectrum



$X_{\max}$

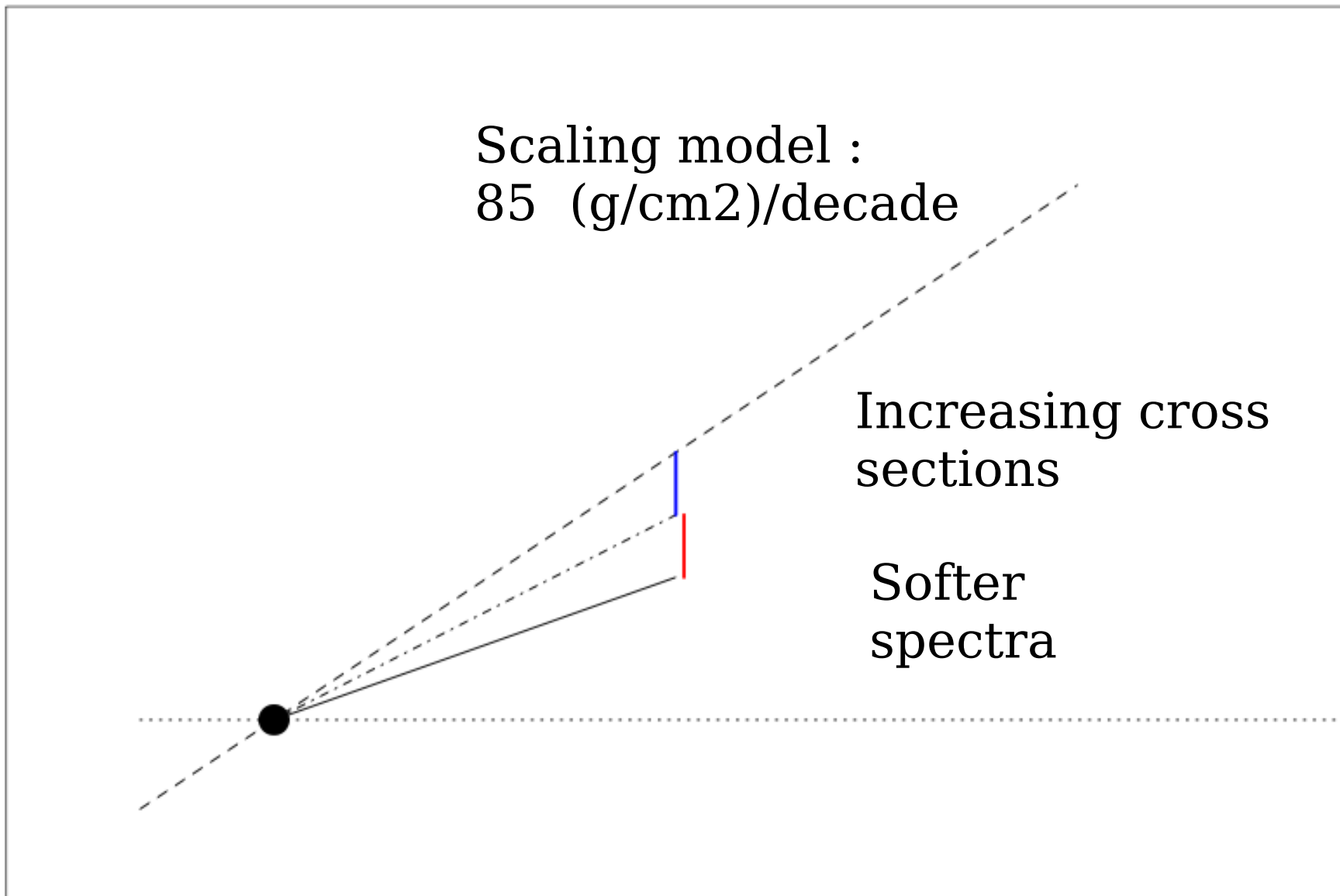
Scaling model :  
85 (g/cm<sup>2</sup>)/decade

Increasing cross  
sections

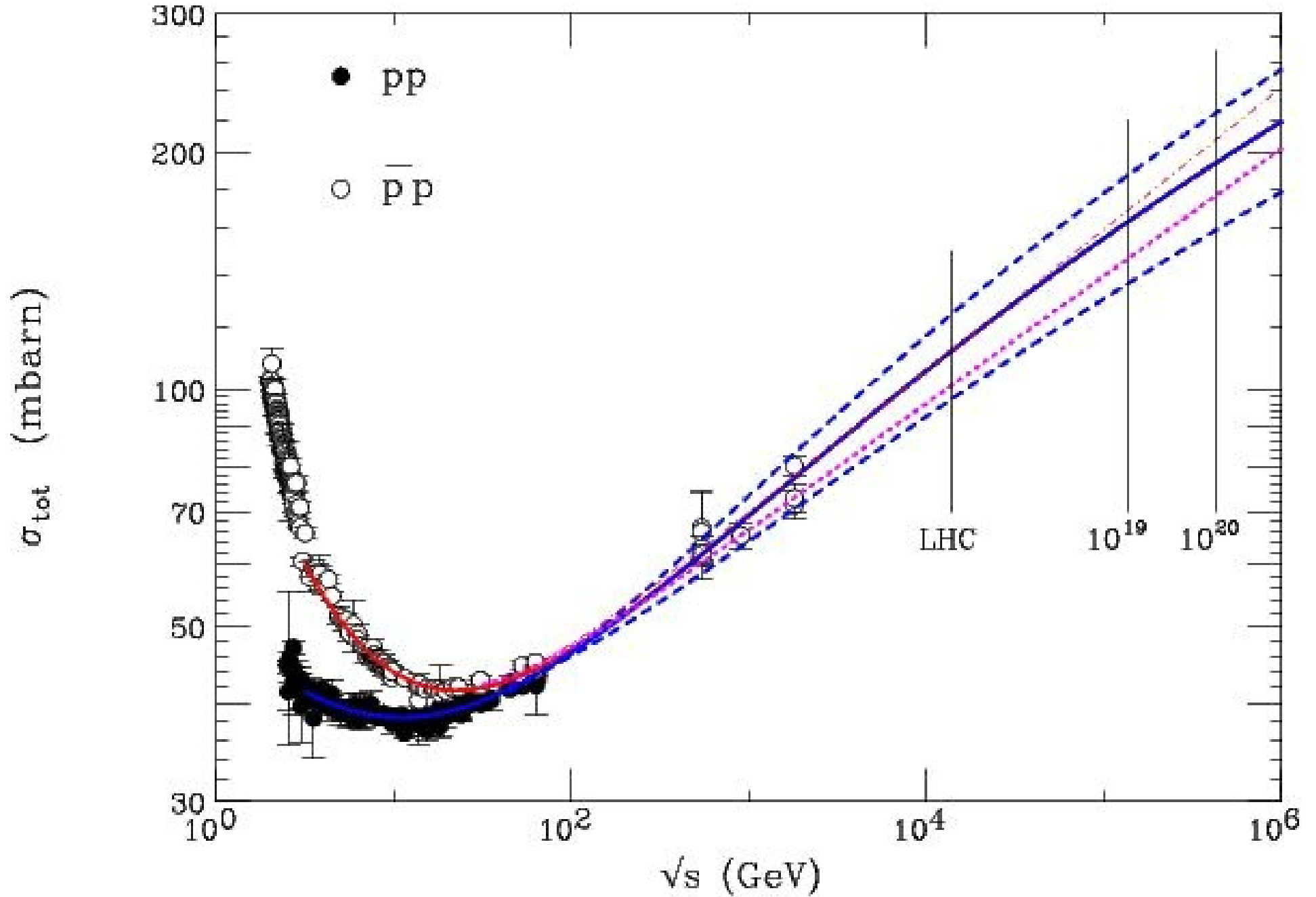
Softer  
spectra

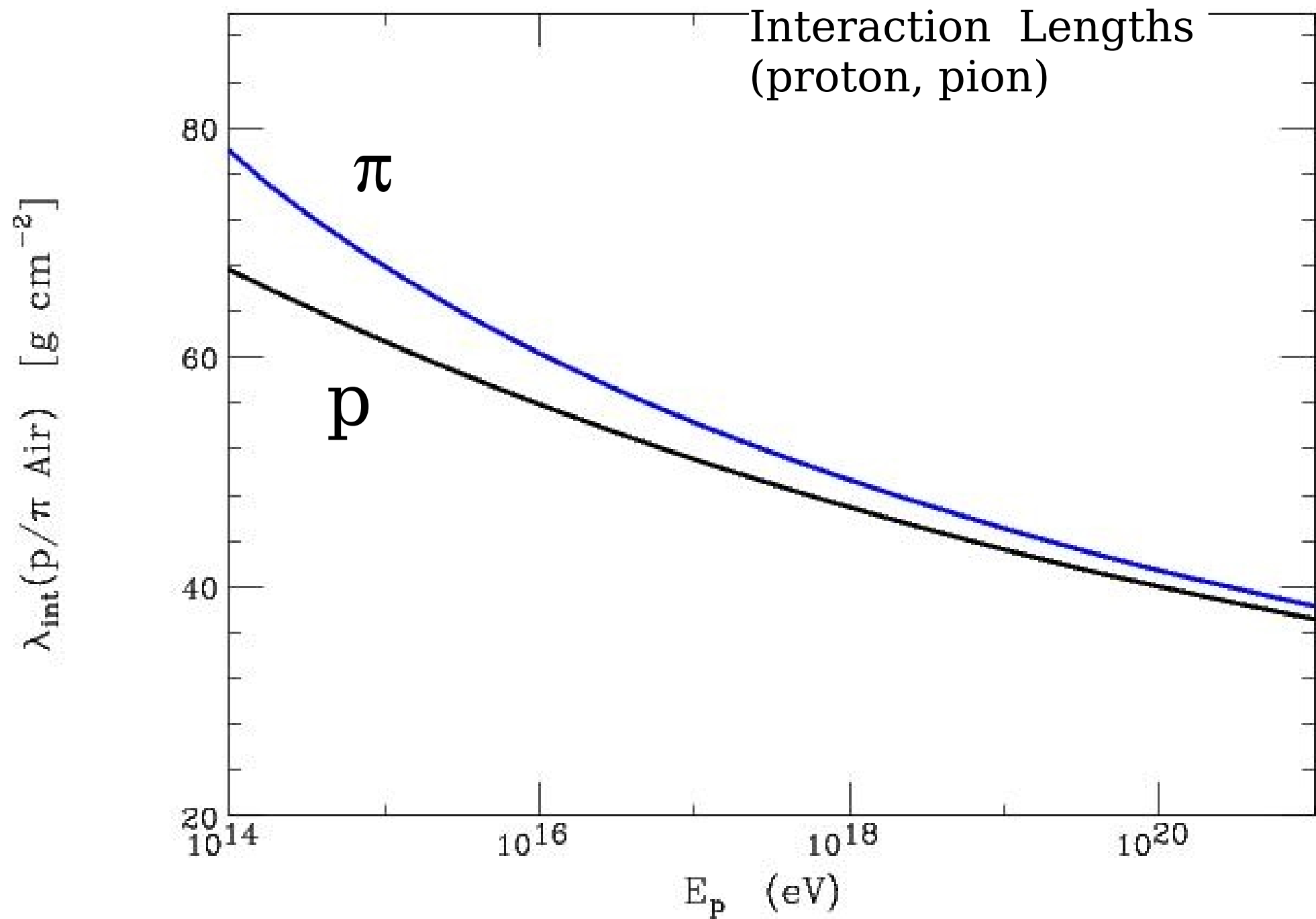
Elongation Rate  
For protons

Log[Energy]

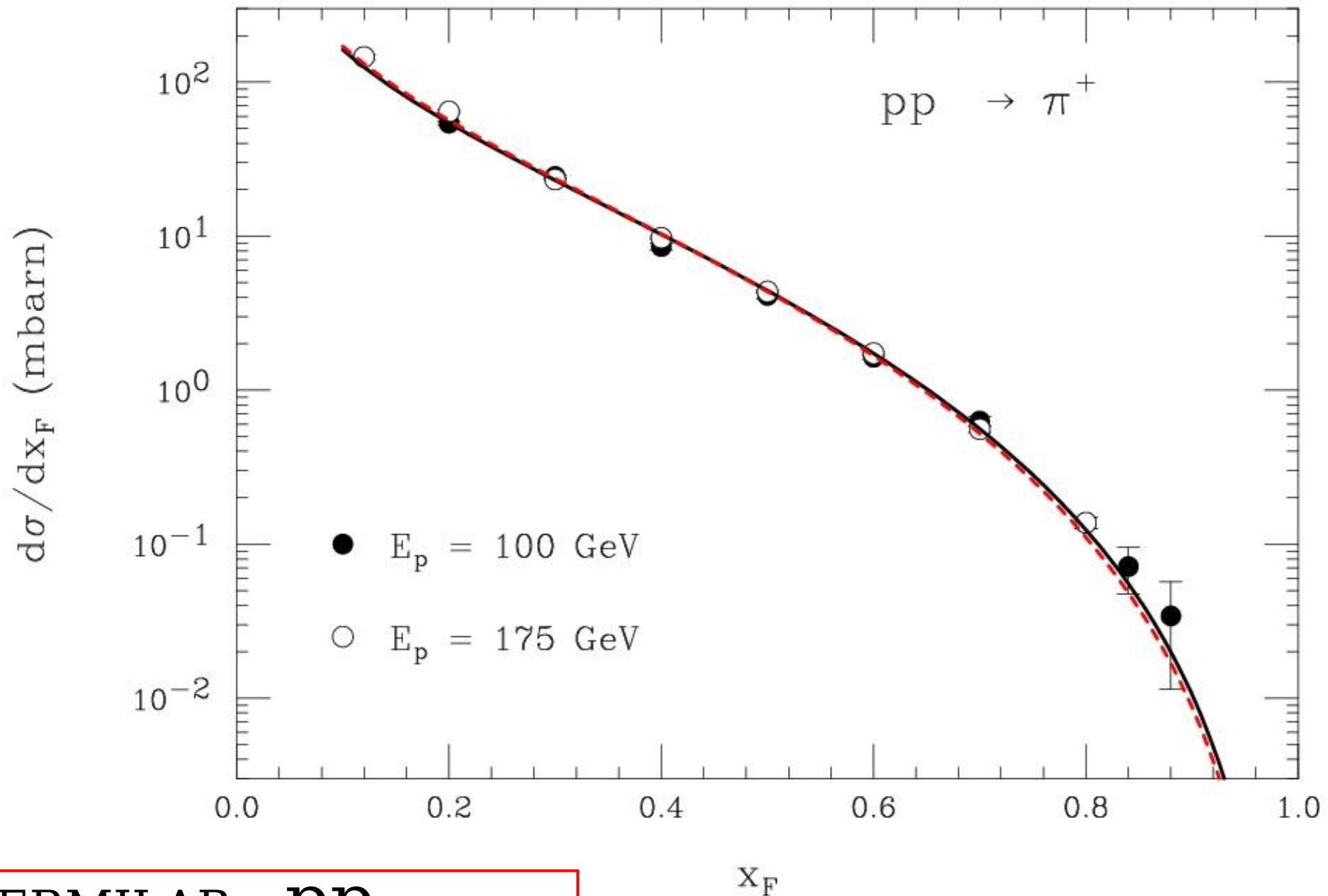


# Total pp Cross Section



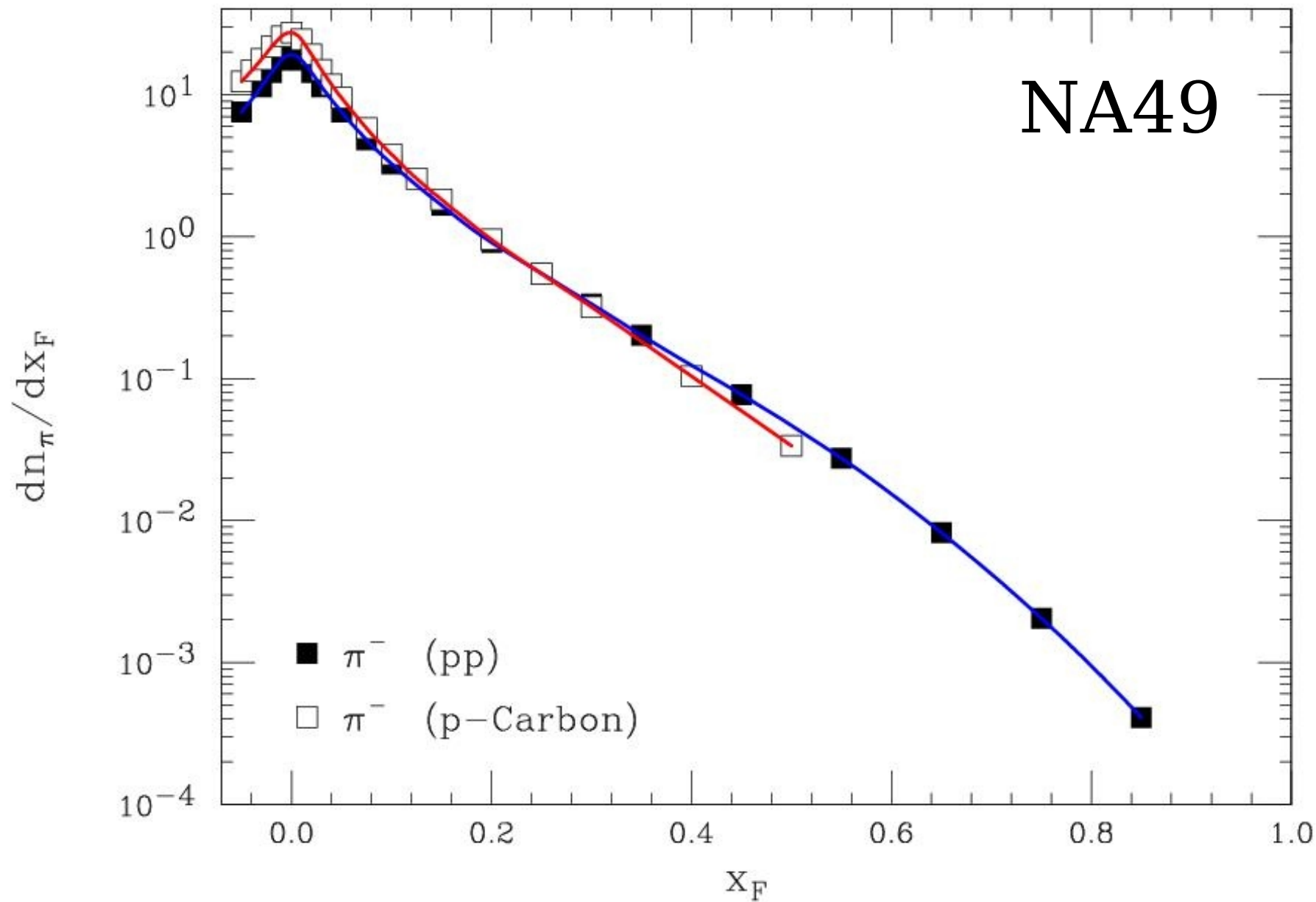


# Phenomenological Evidence for SCALING

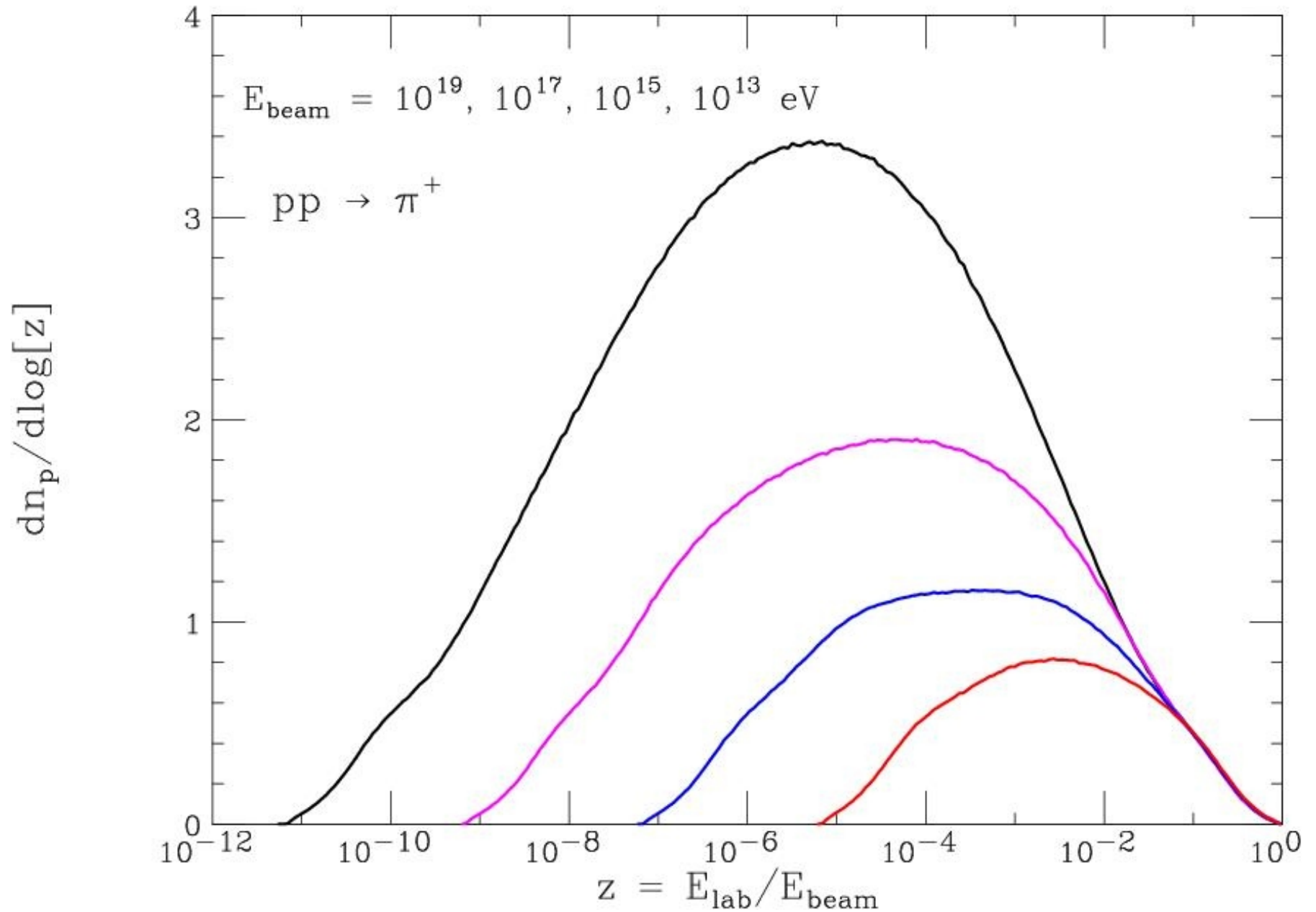


FERMILAB: **pp**  
Brenner et al (1982)

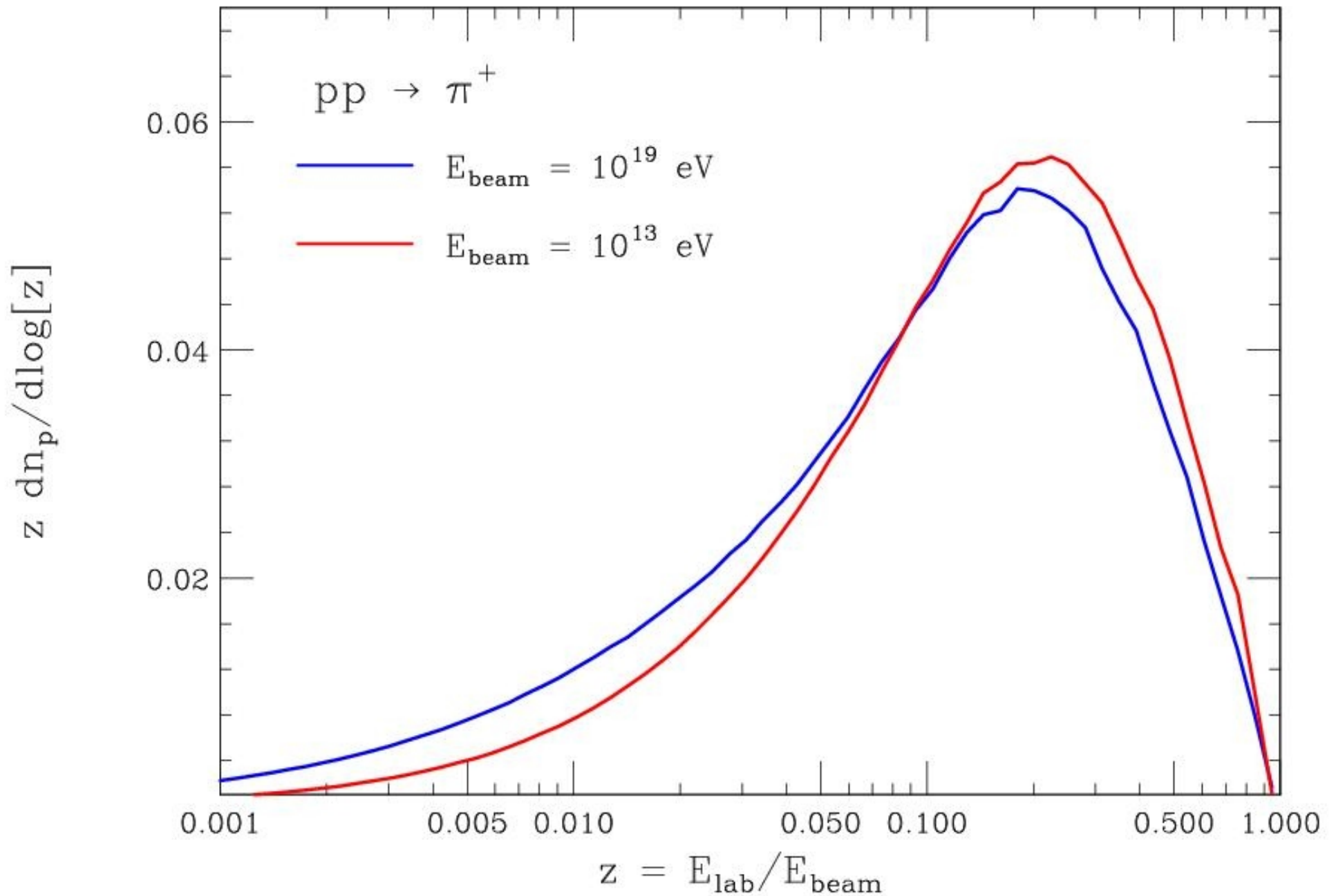
# NUCLEAR effects: $pp$ vs $p-^{12}\text{C}$

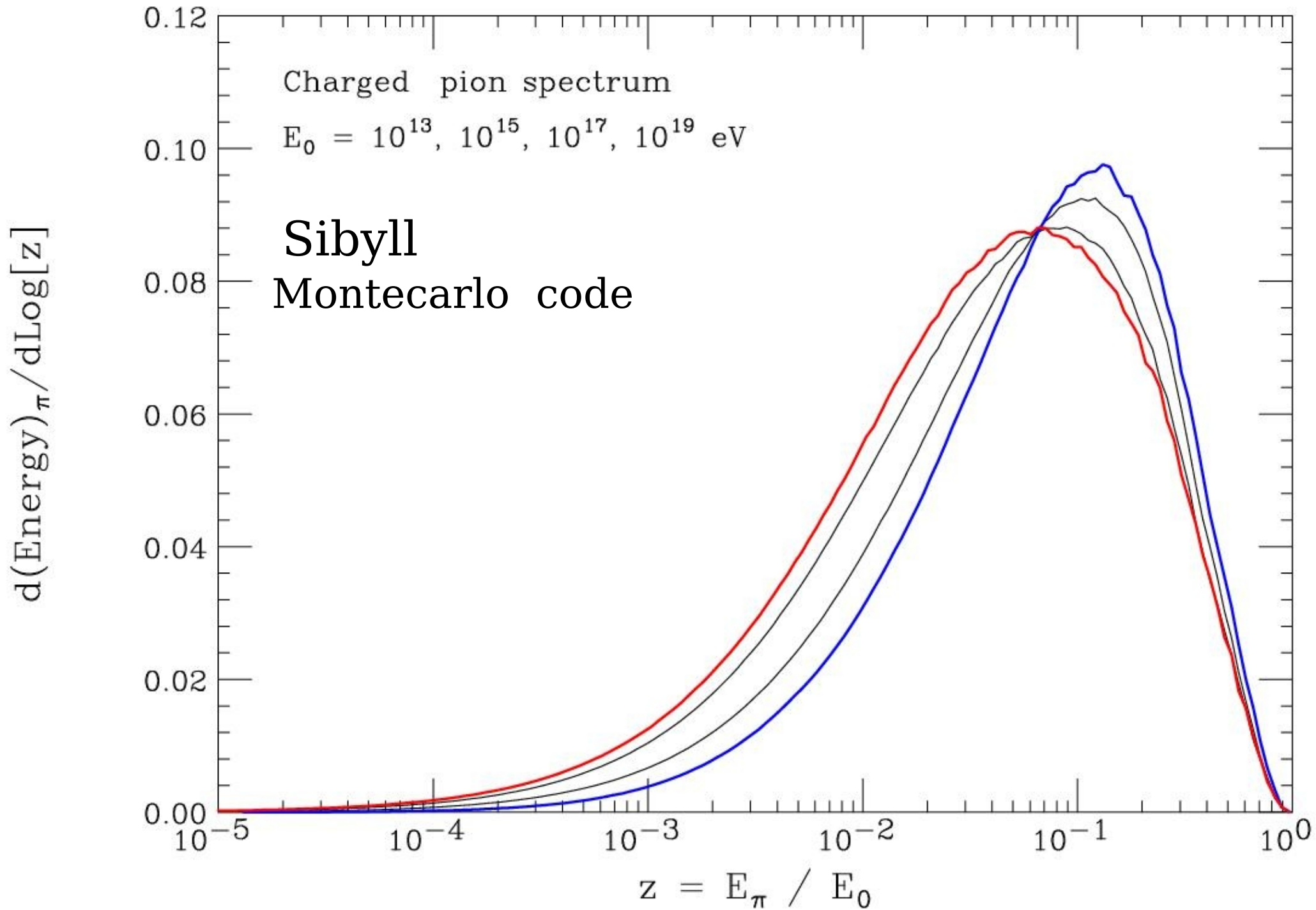


# EXTRAPOLATION to HIGH ENERGY (Pythia pp)



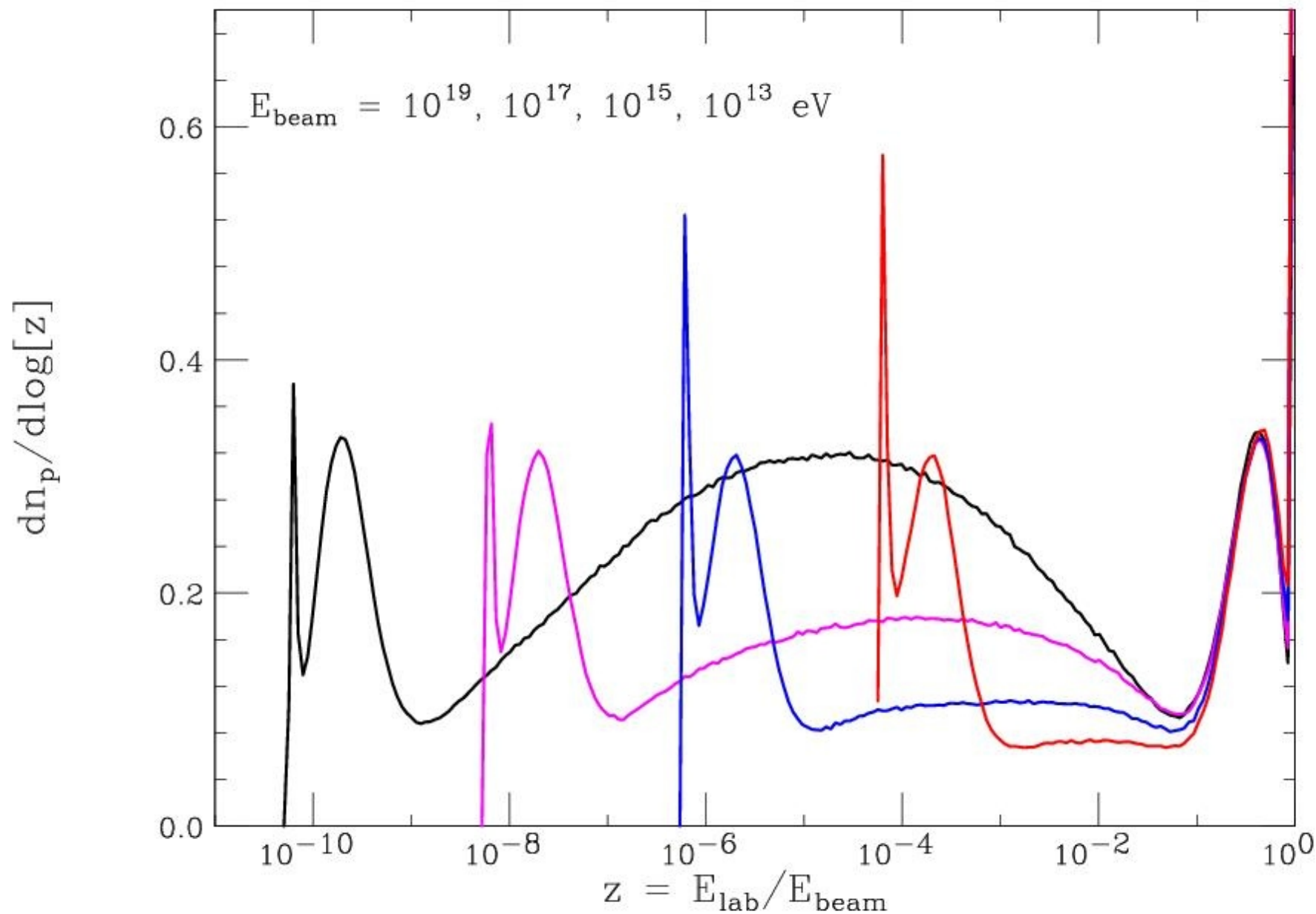
# EXTRAPOLATION to HIGH ENERGY (Pythia pp)



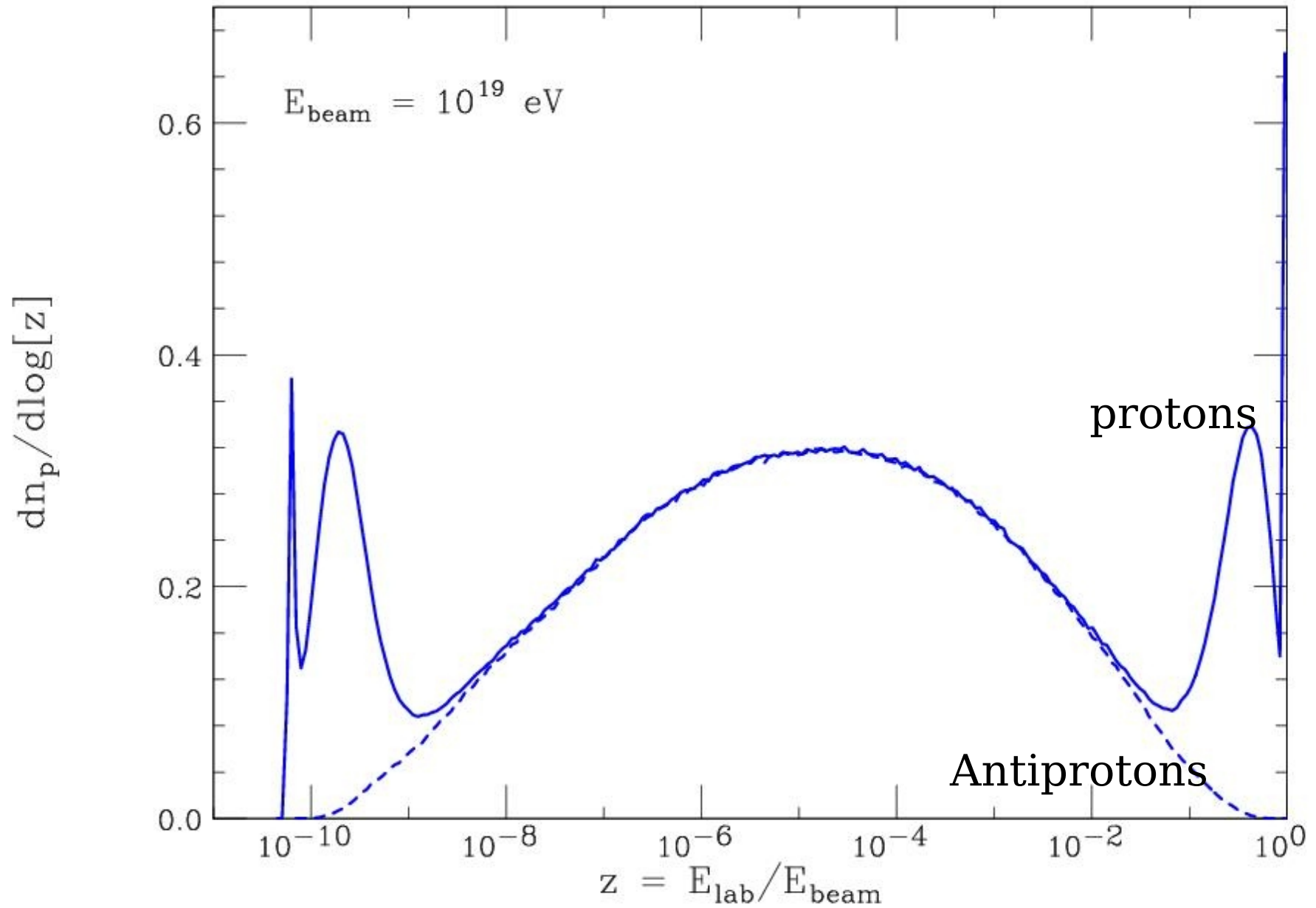




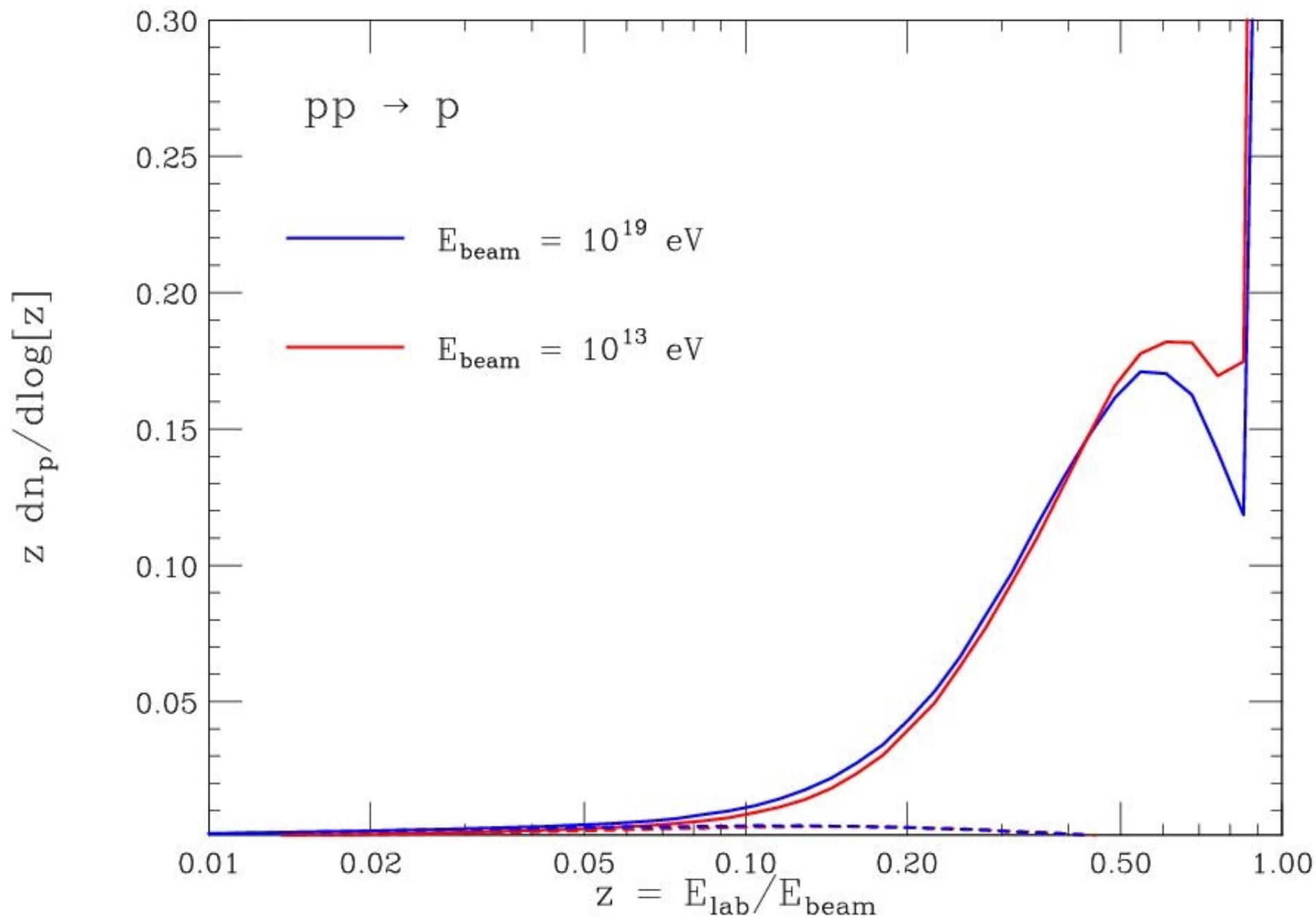
# PROTON Spectra (elasticity spectra)



# PYTHIA PROTON Spectra



# PROTON Spectra (elasticity spectra)



# C.R. DATA

## Astrophysical Information

Energy Spectrum  
Composition

## Hadronic Interactions

Cross sections,  
Inclusive spectra  
Multiplicities

From Accelerator Data + Theory → Astrophysics

C.R. DATA

```
graph TD; A[C.R. DATA] --> B[Astrophysical Information]; A --> C[Hadronic Interactions];
```

Astrophysical  
Information

Energy Spectrum  
Composition

Hadronic  
Interactions

Cross sections,  
Inclusive spectra  
Multiplicities

$$\langle \ln A \rangle_E = \frac{\langle X_{\max}(E) \rangle - X_p(E)}{D_p}$$

Data

$$\langle \ln A \rangle_E$$

=

$$\langle X_{\max}(E) \rangle$$

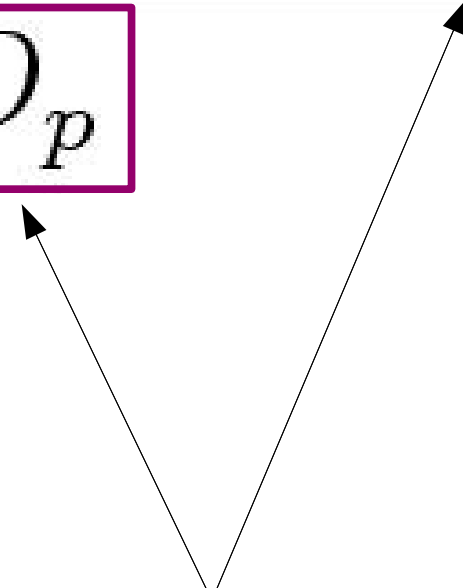
-

$$X_p(E)$$

$$D_p$$

Astrophysical  
Information

Hadronic  
Interactions



How can we include systematic uncertainties in the modeling of hadronic interactions in the estimate of properties of Cosmic Rays?

“Spread” of predictions for different model.

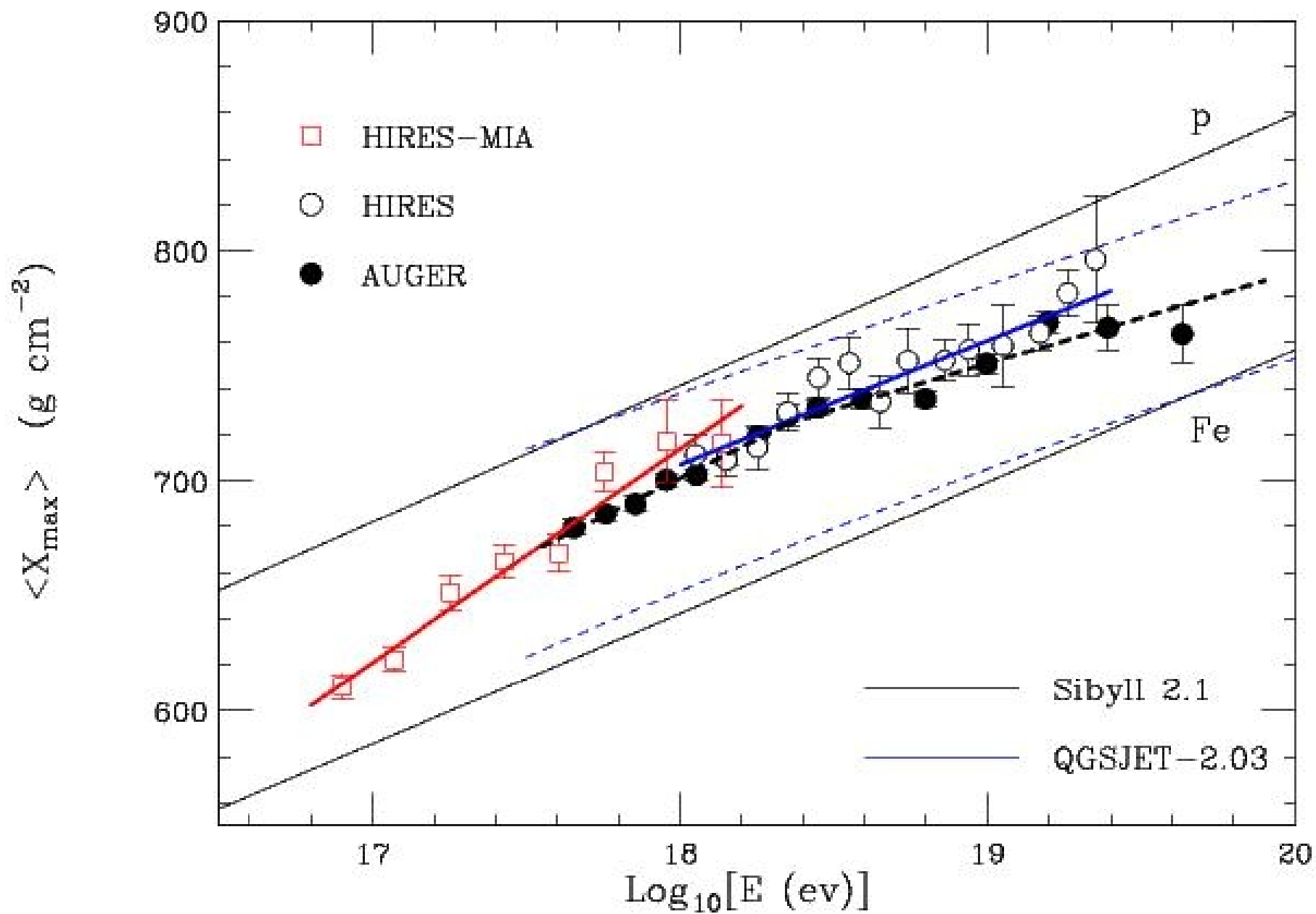
Overestimate ?


Some models are lower quality.

Underestimate ?

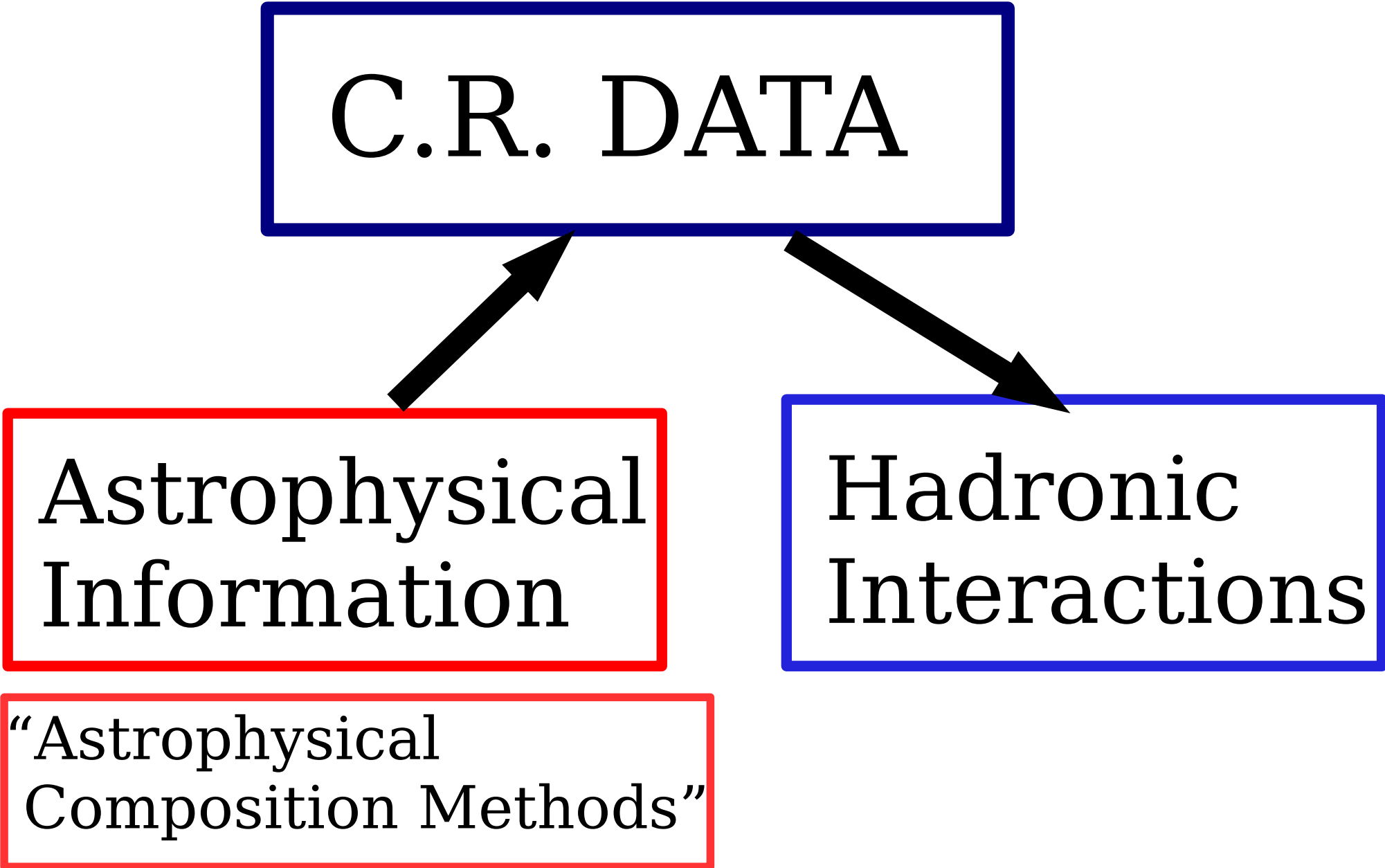
Perhaps we are missing something important.





From Cosmic Ray Data  Hadronic Interactions

C.R. DATA



```
graph TD; A[C.R. DATA] --> B[Hadronic Interactions]; A --> C[Astrophysical Information]; D["Astrophysical Composition Methods"] --> C;
```

Astrophysical  
Information

Hadronic  
Interactions

“Astrophysical  
Composition Methods”

From Cosmic Ray Data  Hadronic Interactions

C.R. DATA

Astrophysical  
Information

Hadronic  
Interactions

“Astrophysical  
Composition Methods”

$1 < A < 56$  (very likely)

# “Astrophysical Composition Methods”

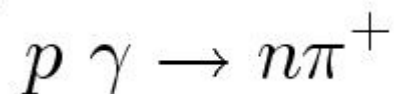
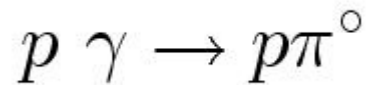
- Energy Spectrum  
“imprints” of Energy Loss
- “Cosmic Magnetic  
Spectrometer”

Features in the Cosmic Ray Energy Spectrum can in principle give information on the nature of the particle

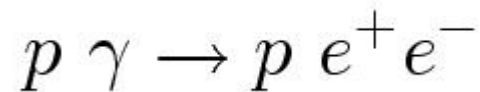
Interpreted as the effect of energy loss during propagation from their extragalactic sources.

Known target: 2.7 K CMBR radiation field

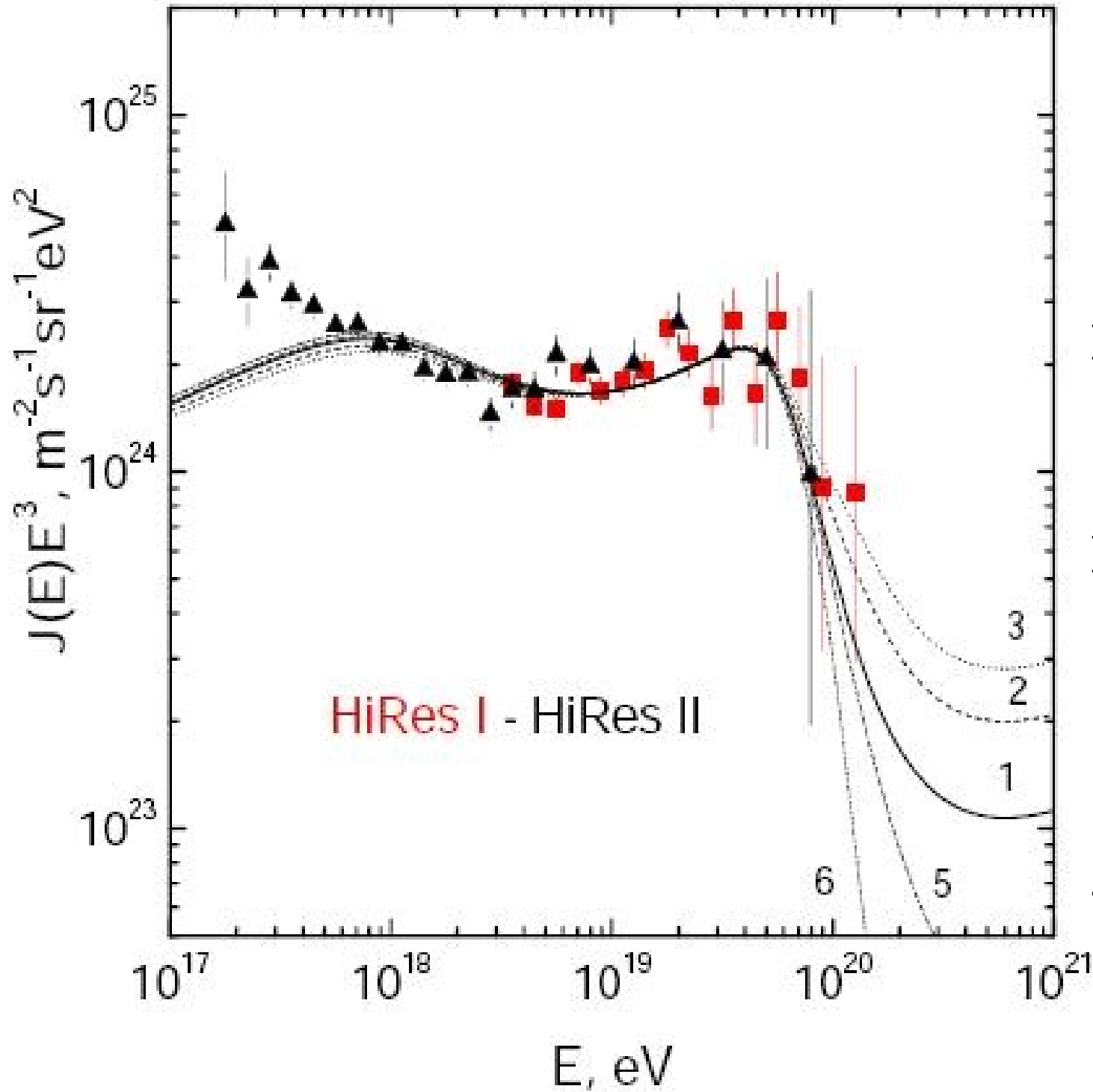
Energy Thresholds for protons :



“GZK”



Pair Production



Berezinsky  
et al.

Inject Smooth  
power law  
Spectrum.

Let propagation  
leave its  
“imprint”  
on the shape  
of the spectrum.

“ANKLE”

-->

“DIP”

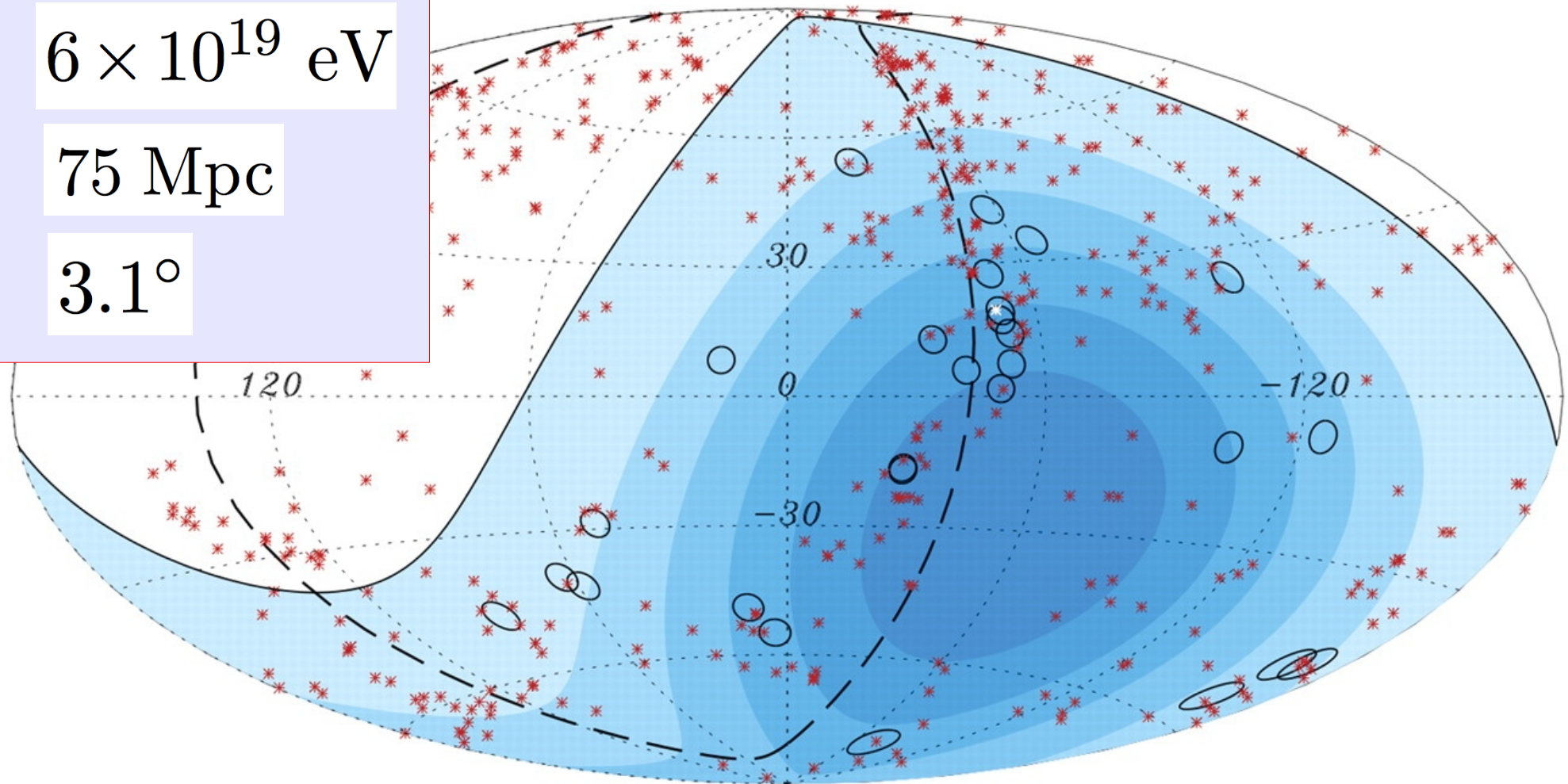
e+e- production

# AUGER result on Correlations with the VCV AGN catalogue November 2007.

$6 \times 10^{19}$  eV

75 Mpc

$3.1^\circ$



Select highest energy Showers.

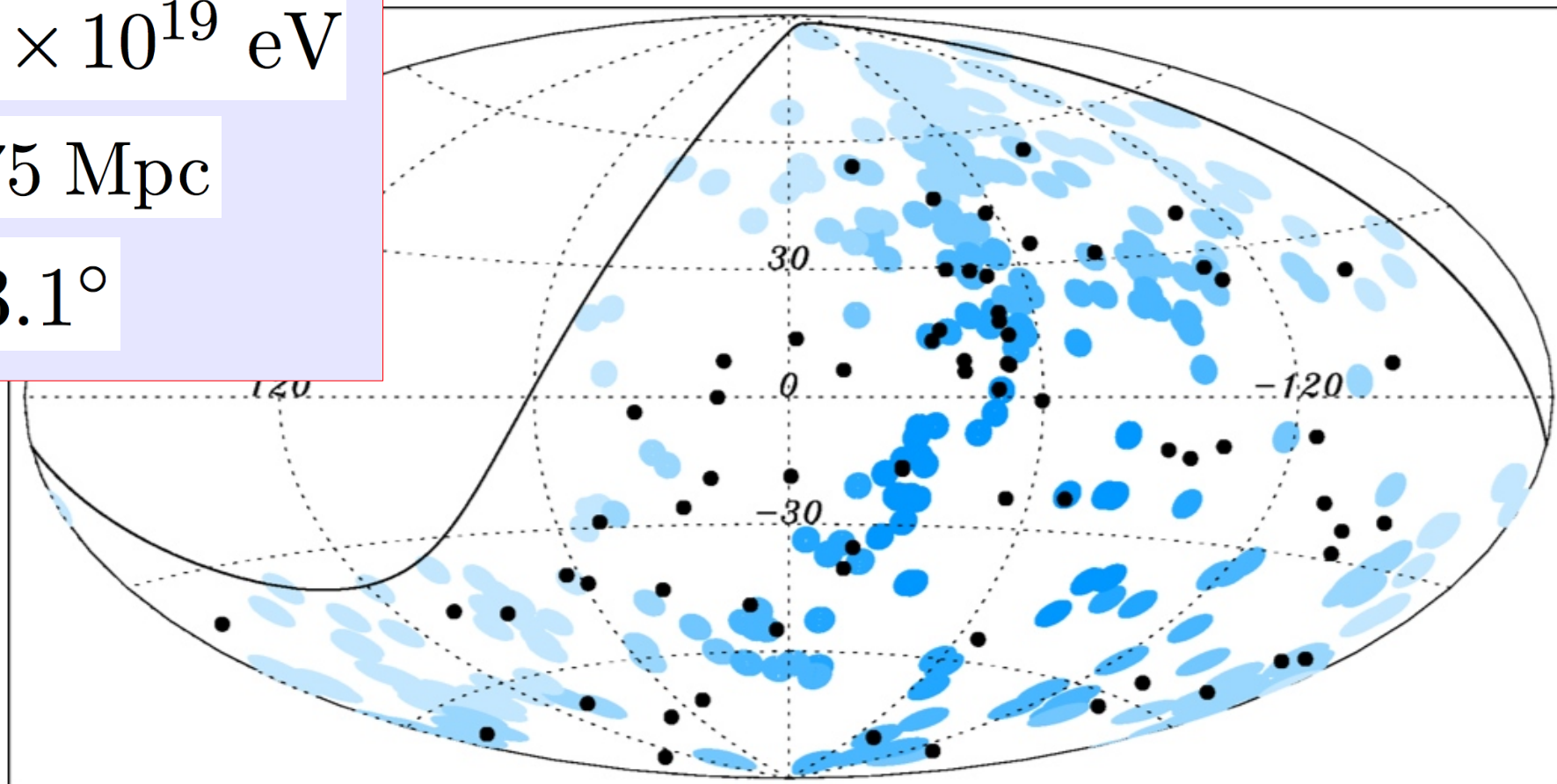
14 ev.	8 coincid. (2.9)
13 ev.	9 coincid. (2.7)

# AUGER result on Correlations with the VCV AGN catalogue Update september 2010.

$6 \times 10^{19}$  eV

75 Mpc

$3.1^\circ$



Significant dilution  
[but not disappearance]  
of the statistical significance

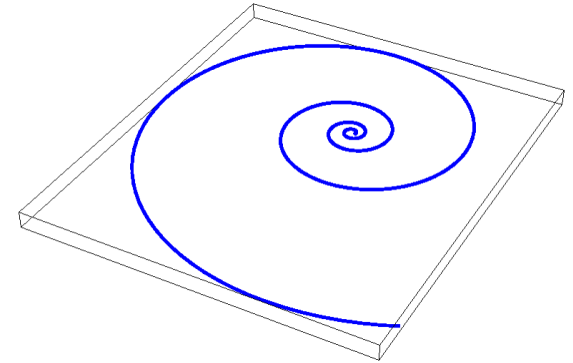
14 ev.	8 coincid.	(2.9)
13 ev.	9 coincid.	(2.7)
42 ev.	12 coincid.	(8.8)



$$\delta\theta = (\delta\theta)_{\text{Milky Way}} + (\delta\theta)_{\text{Intergalactic}} + (\delta\theta)_{\text{Source Envelope}}$$

## Deviation in GALACTIC Magnetic Field

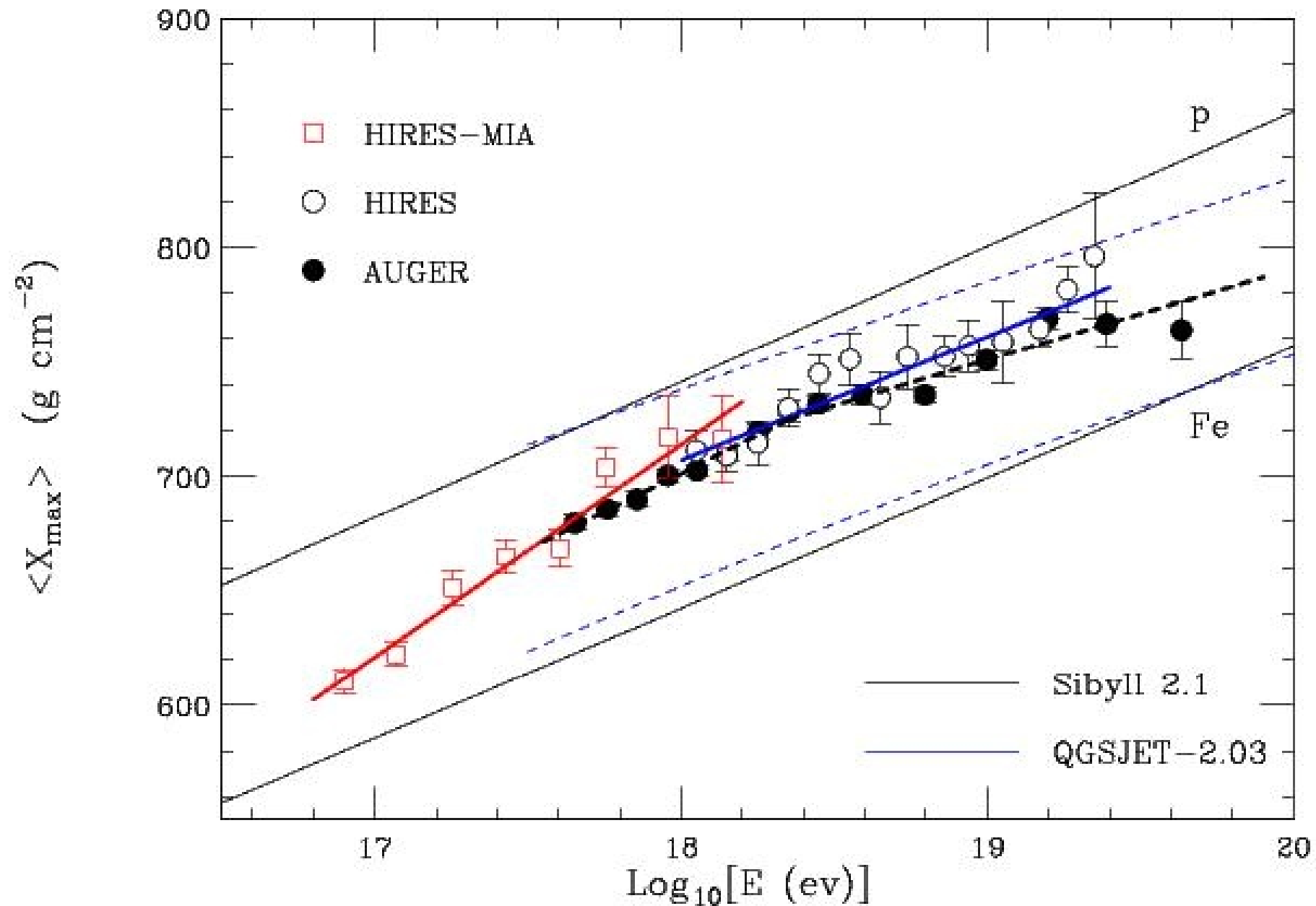
$$\delta \simeq 2.7^\circ \frac{60 \text{ EeV}}{E/Z} \left| \int_0^D \left( \frac{dx}{\text{kpc}} \times \frac{\mathbf{B}}{3 \mu\text{G}} \right) \right|$$



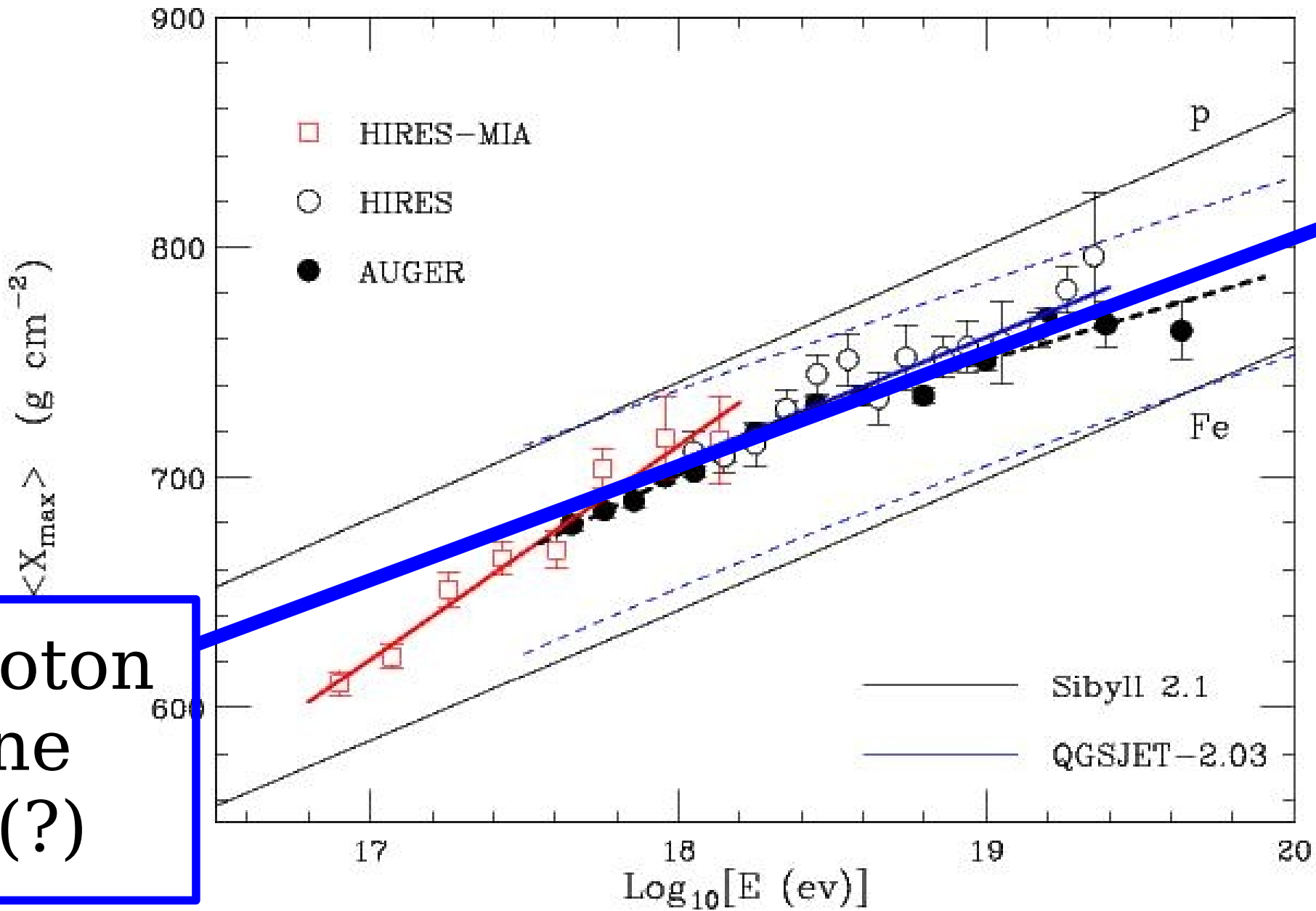
## Deviation in EXTRA-GLACTIC Magnetic Field

$$\delta_{rms} \simeq 4^\circ \frac{60 \text{ EeV}}{E/Z} \frac{B_{rms}}{10^{-9}\text{G}} \sqrt{\frac{D}{100 \text{ Mpc}}} \sqrt{\frac{L_c}{1 \text{ Mpc}}}$$

**IF** one accepts (at least for the sake of discussion)  
the astrophysical hints of a proton dominated composition....

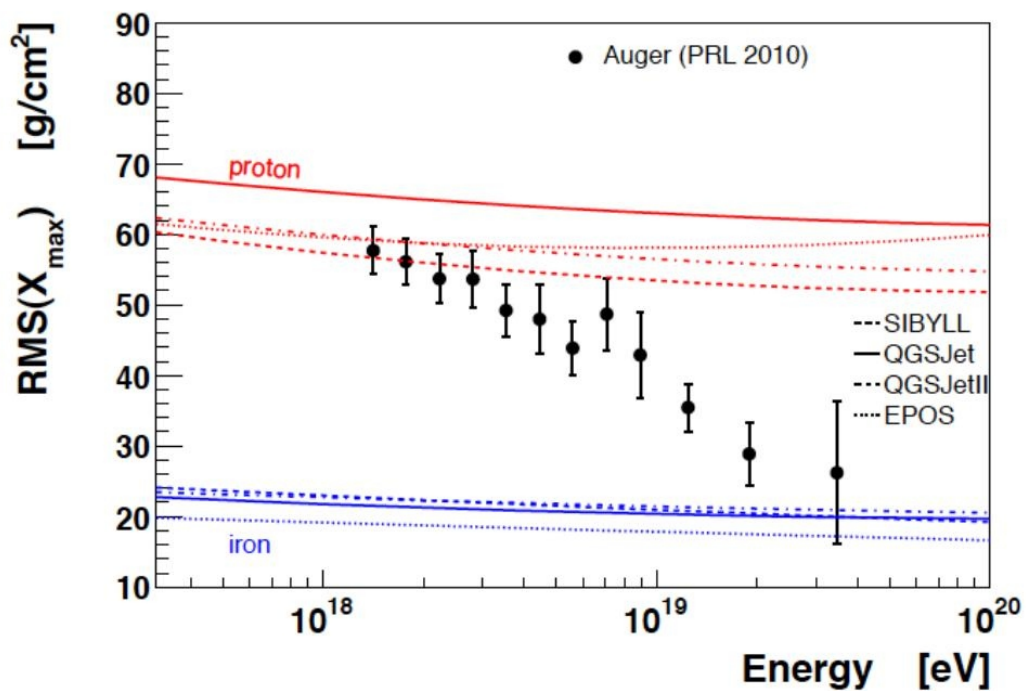


IF one accepts (at least for the sake of discussion)  
the astrophysical hints of a proton dominated composition....

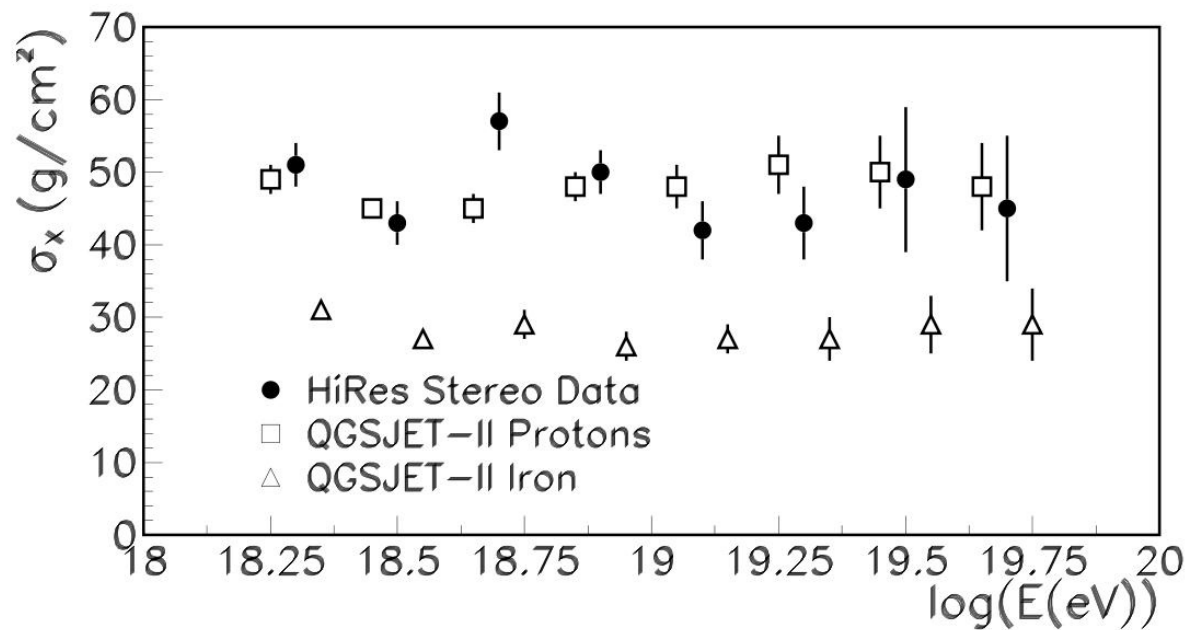


Proton  
Line  
!! (?)

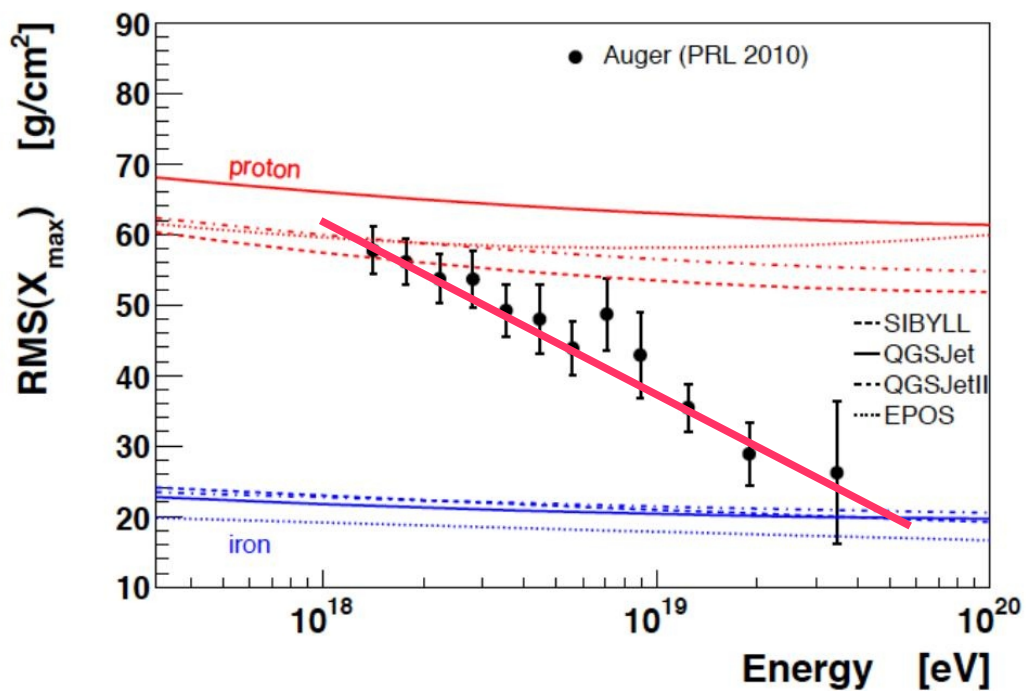
# $X_{\max}$ fluctuations



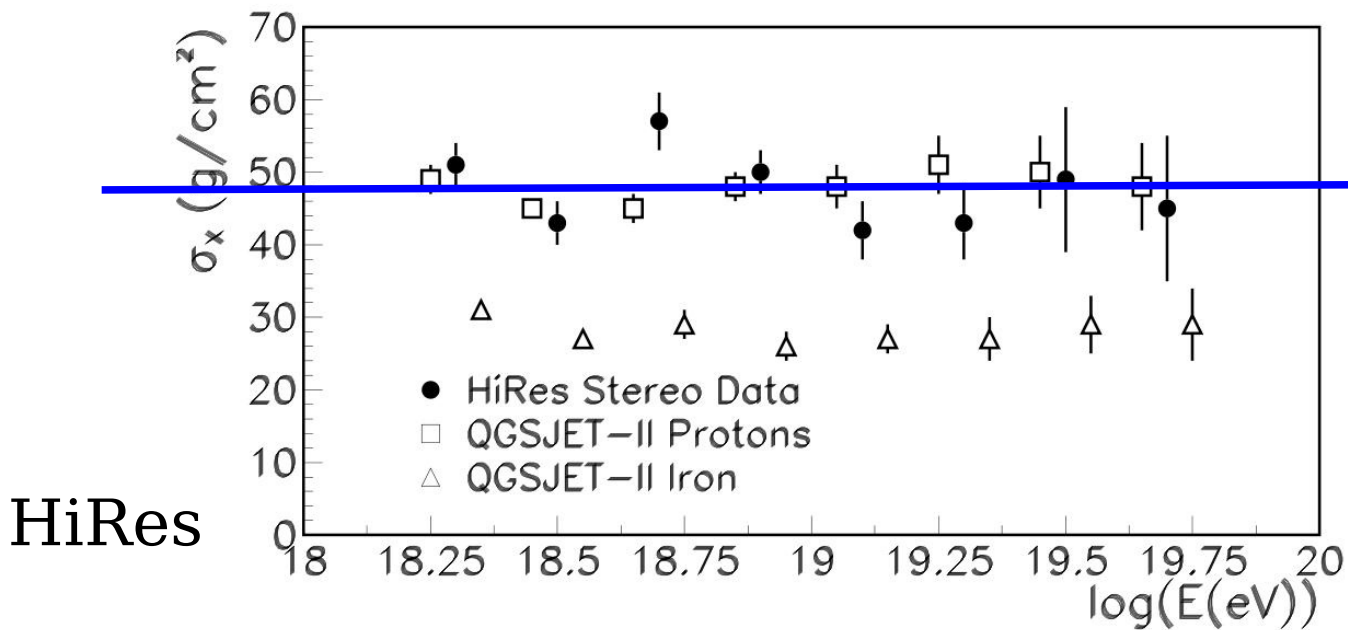
HiRes



# $X_{\max}$ fluctuations



Constant RMS



# Overall comparison of $X_{max}$ data with QGSJET02 p and FE

HIRES

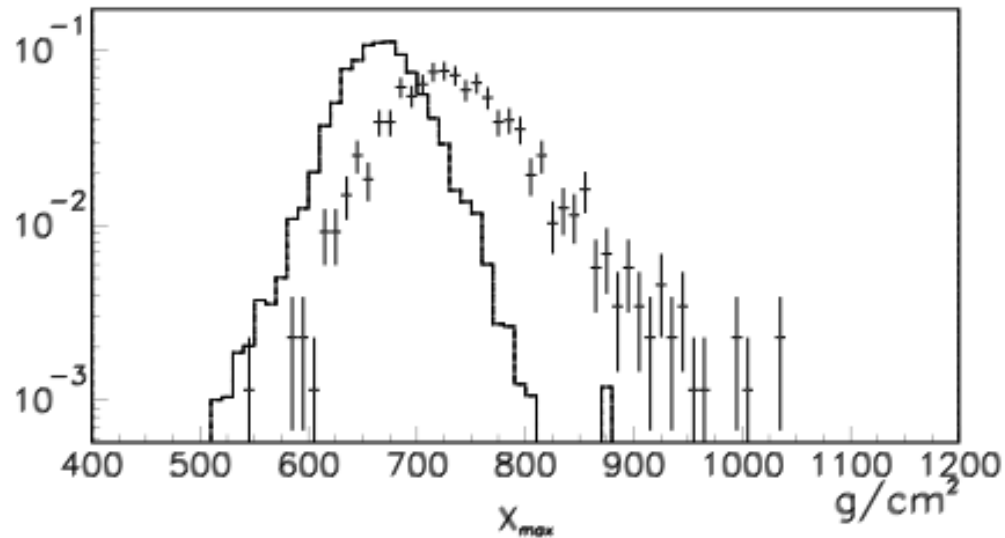
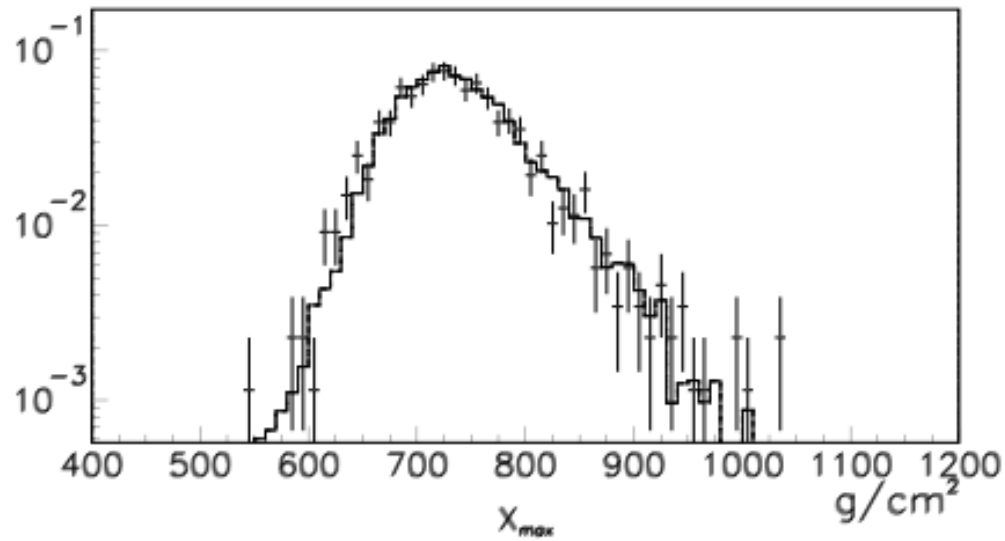


Fig. 11.— *Top:*  $X_{max}$  overlay of HiRes data (points) with QGSJET02 proton Monte Carlo airshowers after full detector simulation. *Bottom:*  $X_{max}$  overlay of HiRes data (points) with QGSJET02 iron Monte Carlo airshowers after full detector simulation.

The distribution of  $X_{\max}$  encodes valuable information on the detector performance and on the fundamental properties of the showers that is only partially captured by the first 2 moments

Personal opinion:

The  $X_{\max}$  distributions are valuable “intellectual property” of the scientists that measure it.

But for a healthy scientific discussion, they should be made available to our entire community in a reasonable time

# FLUCTUATIONS on $X_{\max}$

$$X_{\max} = X_{1\text{st}} + Y_{\max}$$

$$\sigma_{X_{\max}}^2 = \sigma_{X_{1\text{st}}}^2 + \sigma_{Y_{\max}}^2$$

$$\left(\sigma_{\langle X_{\max} \rangle}^{\text{proton}}\right)^2 \simeq \lambda_p^2 + \sigma_{Y_{\max}}^2$$

Toy model

$$\left(\sigma_{\langle X_{\max} \rangle}^{\text{proton}}\right)^2 \simeq \lambda_p^2 + X_{\text{rad}}^2 \left[ \langle (\ln n_\gamma)^2 \rangle - \langle \ln n_\gamma \rangle^2 \right]$$



$$\left(\sigma_{\langle X_{\max} \rangle}^{\text{proton}}\right)^2 \simeq \lambda_p^2 + \sigma_{Y_{\max}}^2$$

$$\left(\sigma_{\langle X_{\max} \rangle}^A\right)^2 \simeq f(A) \lambda_p^2 + \frac{\sigma_{Y_{\max}}^2}{A}$$

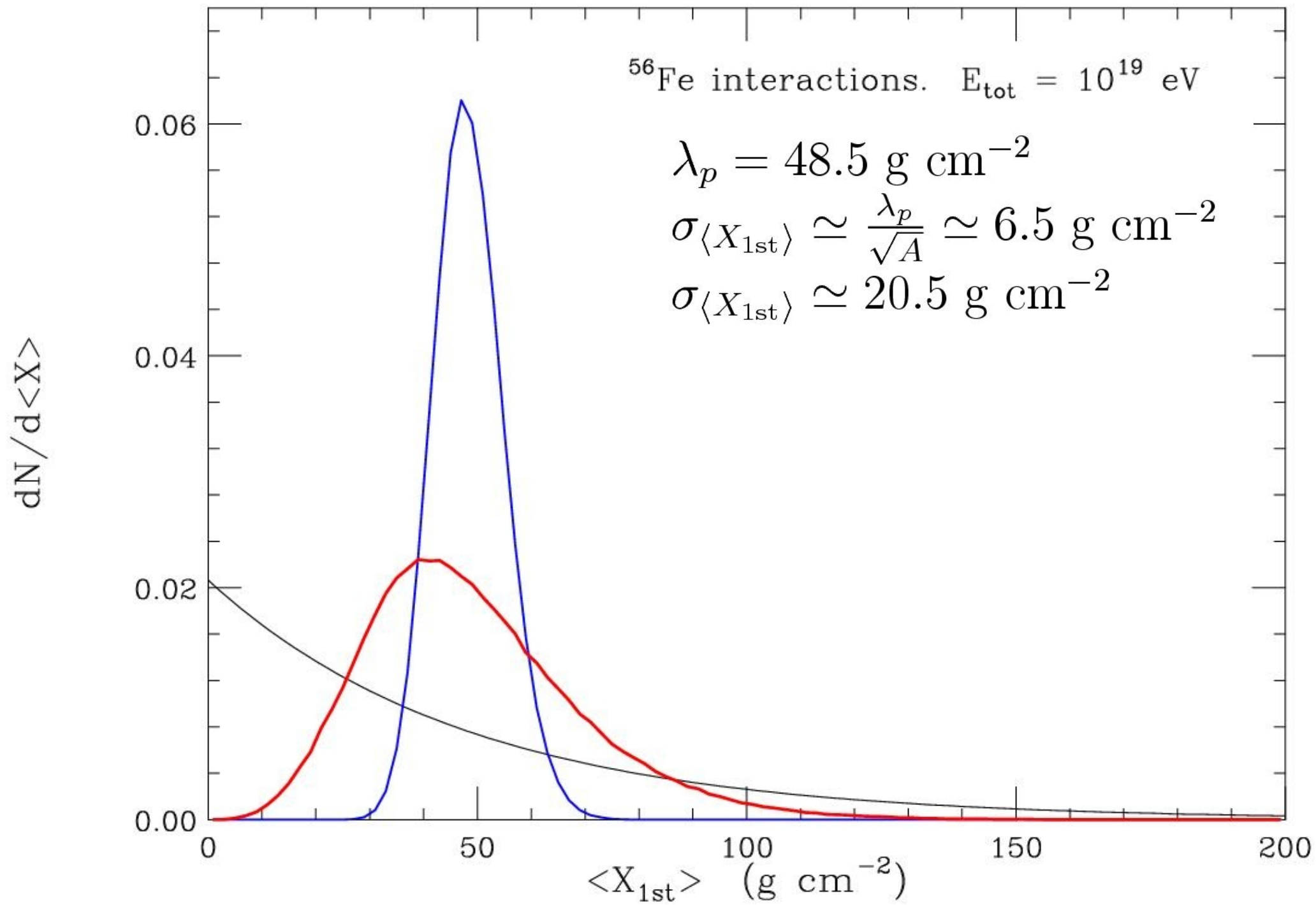
$$A = 56$$

$$\frac{1}{\sqrt{A}} = 0.13$$

$$\sqrt{f(A)} \simeq 0.4$$

$$f(A) > \frac{1}{A}$$

Nuclear interaction.  
Several Nucleons  
Interact at same point.

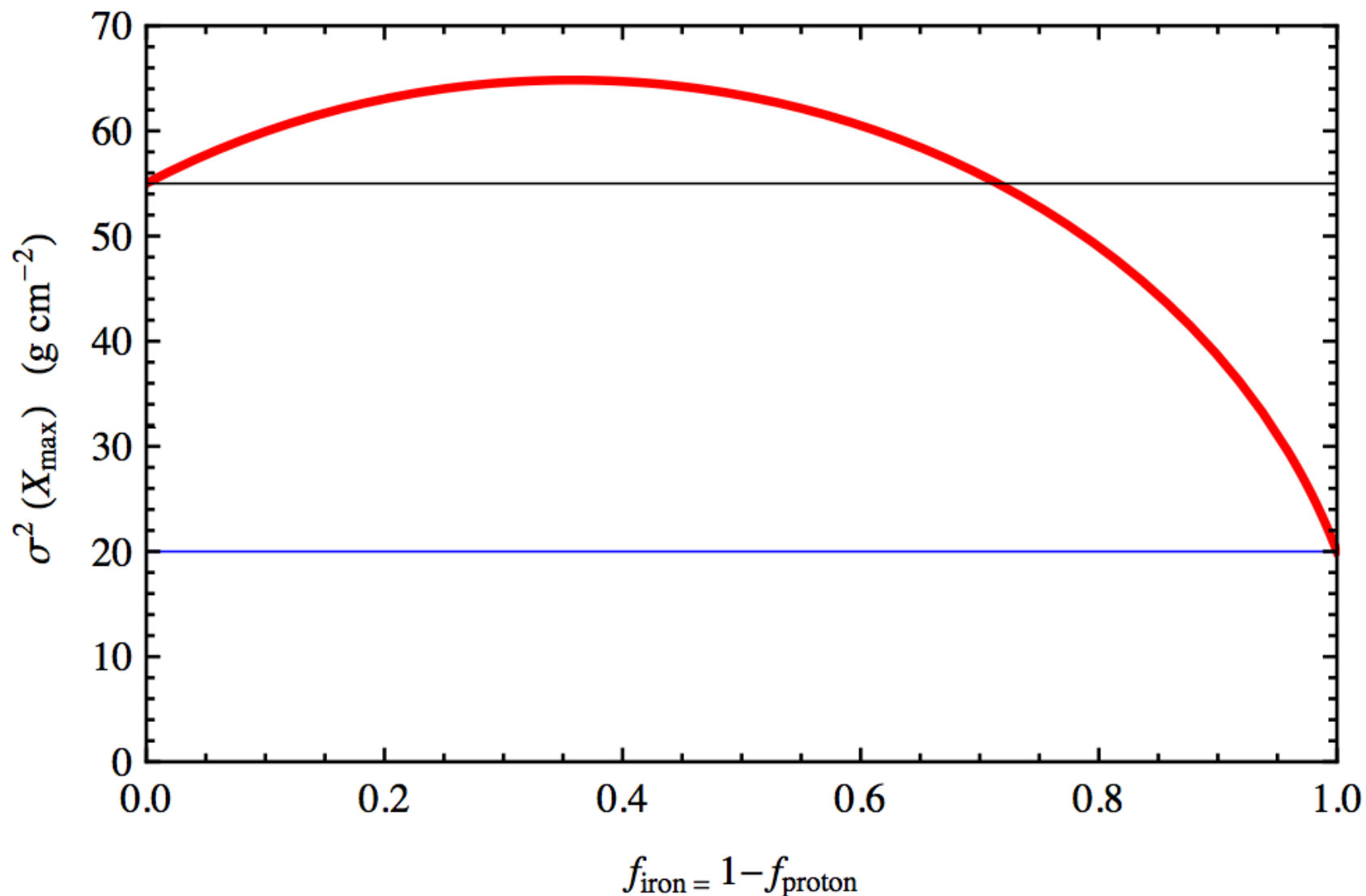


$$\sigma_X^2 = \sum_j f_j \sigma_{A_j}^2 + \sum_j f_j \langle X_{A_j} \rangle^2 - \left( \sum_j f_j \langle X_{A_j} \rangle \right)^2$$

$$\sigma_X^2 = \langle \sigma_A^2 \rangle + D_p \left[ \langle (\log A)^2 \rangle - \langle \log A \rangle^2 \right]$$

$$\sigma_X^2 \simeq \langle \sigma_A^2 \rangle + D_p \sigma_{\log A}^2$$

# Mixing Protons with Iron-nuclei



$$\sigma_X^2 = f_p \sigma_p^2 + (1 - f_p) \sigma_{\text{Fe}}^2 + f_p(1 - f_p) (\langle X_p \rangle - \langle X_{\text{Fe}} \rangle)^2$$

# THEORY

## Construction of Hadronic Models

# Hadronic Interactions

Composite (complex) Objects  
Multiple interaction structure

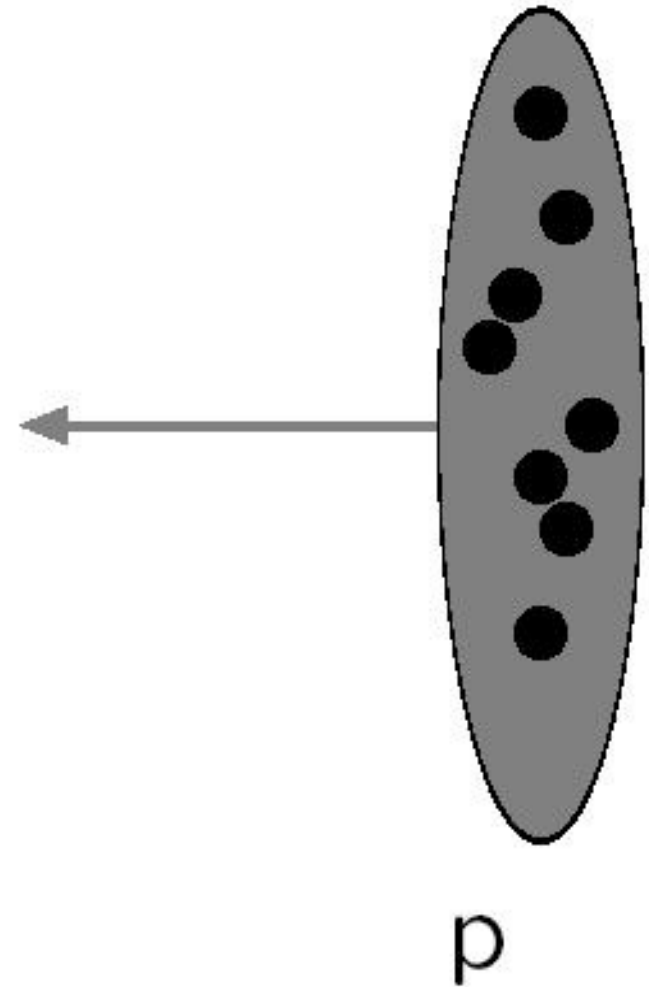
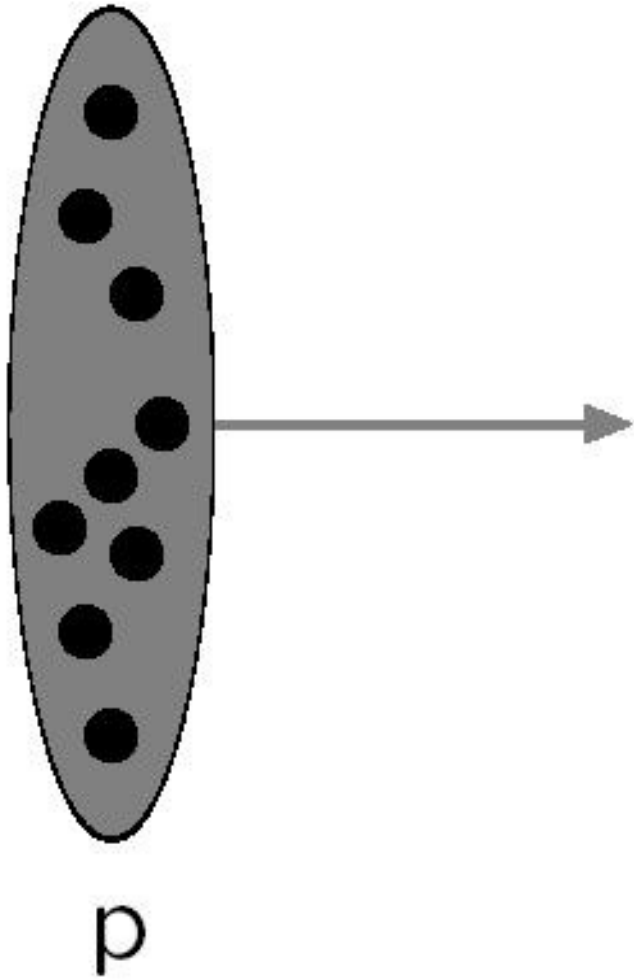
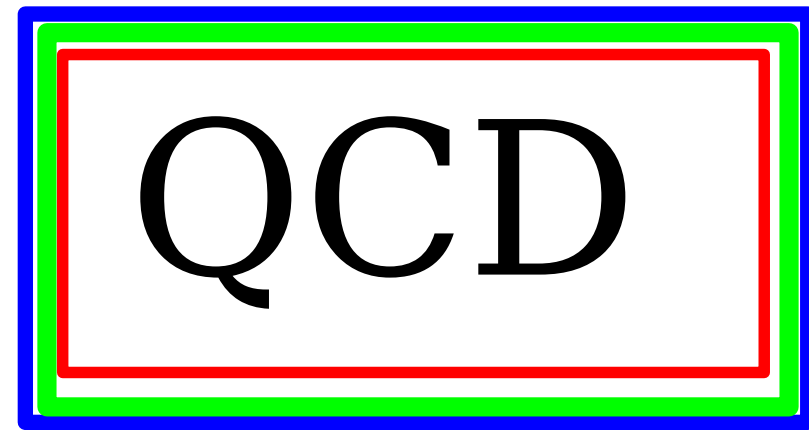
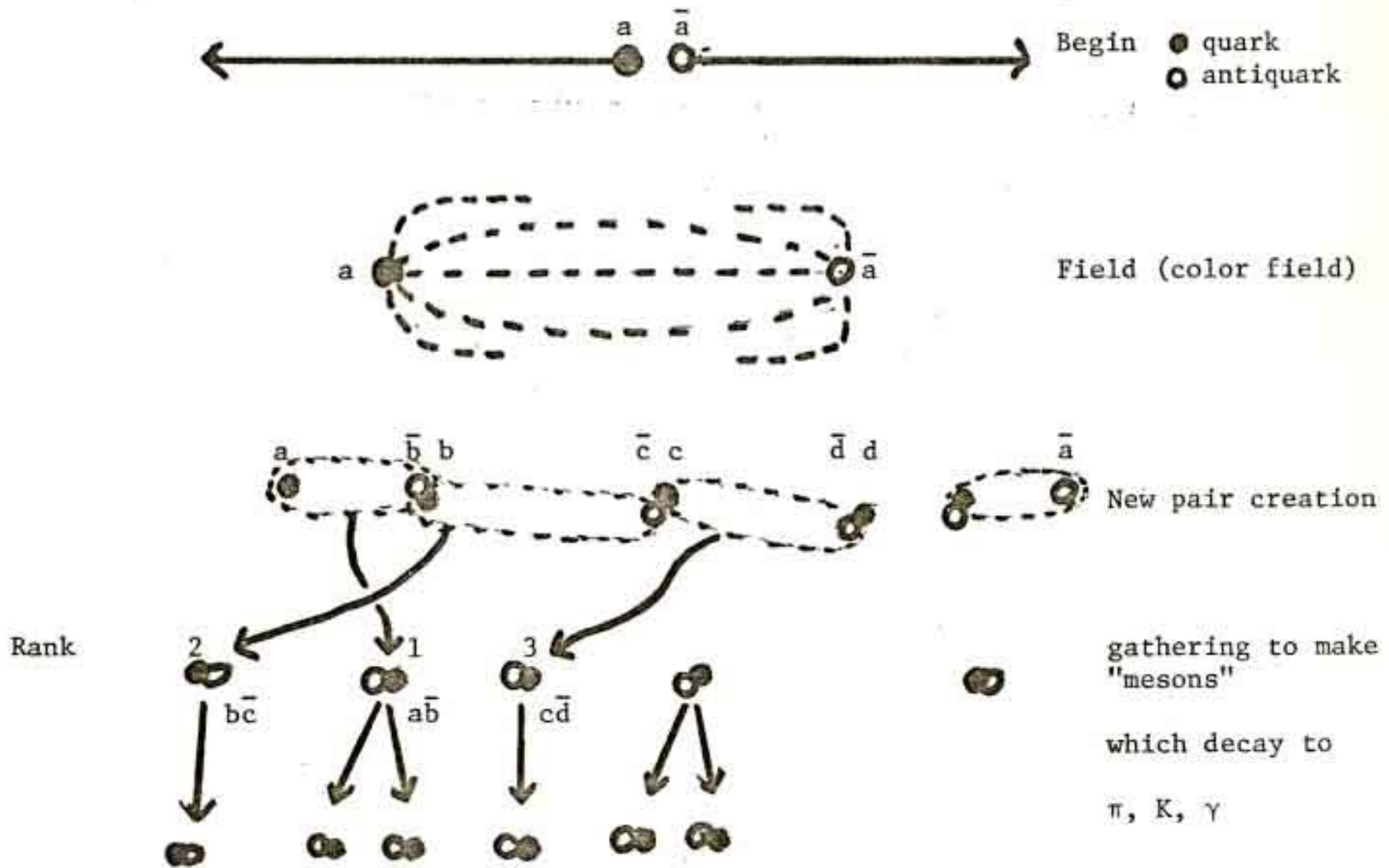


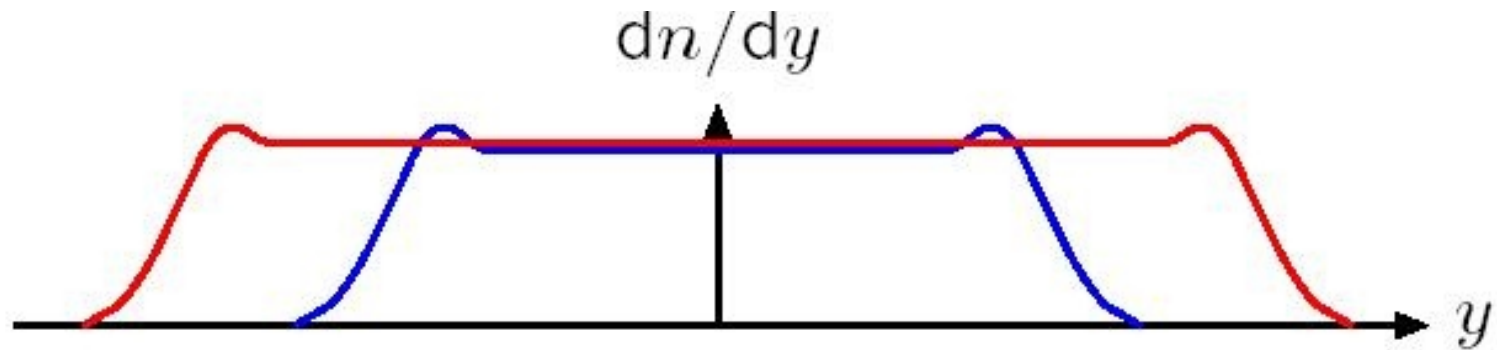
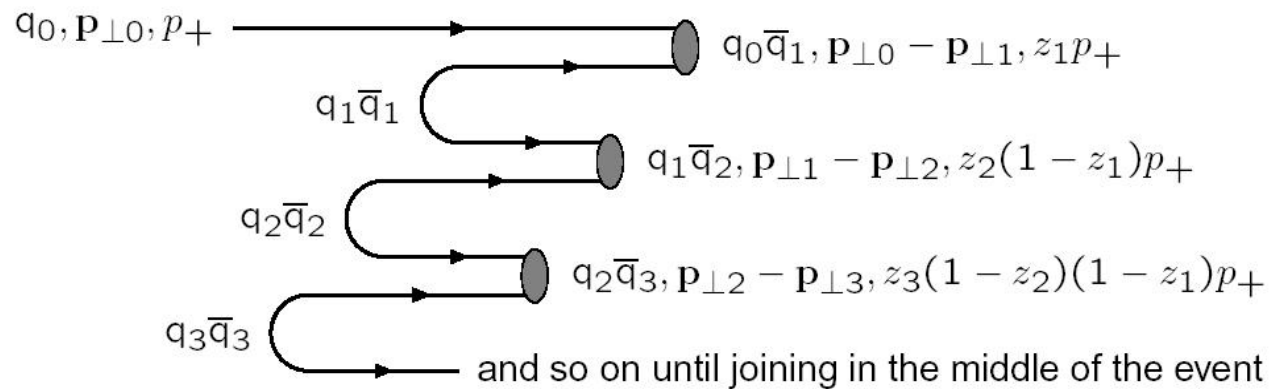
Fig. 1. An  $e^+e^-$  Annihilation



Field -Feynman : Quark - Fragmentation

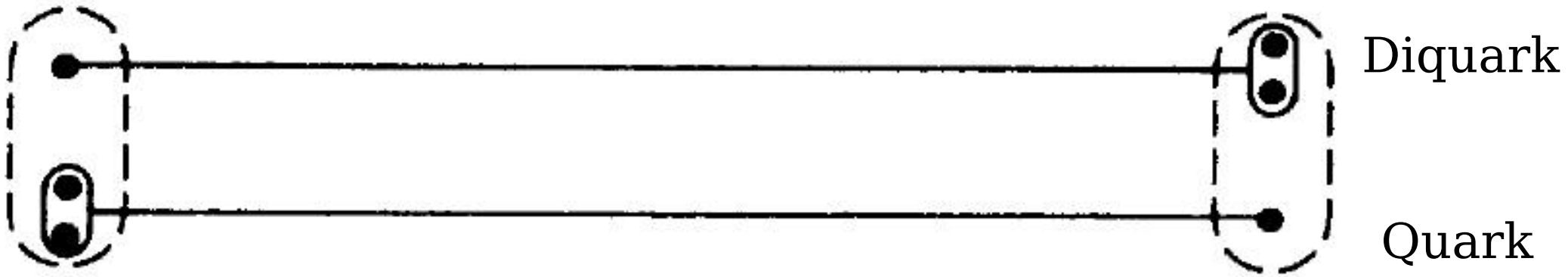
# Where does the approximate Feynman scaling comes from ?

The (iterative) Fragmentation of one COLOR STRING produces a SCALING SPECTRUM of HADRONS



$$\langle n_{ch} \rangle \approx c_0 + c_1 \ln E_{cm}, \sim \text{Poissonian multiplicity distribution}$$





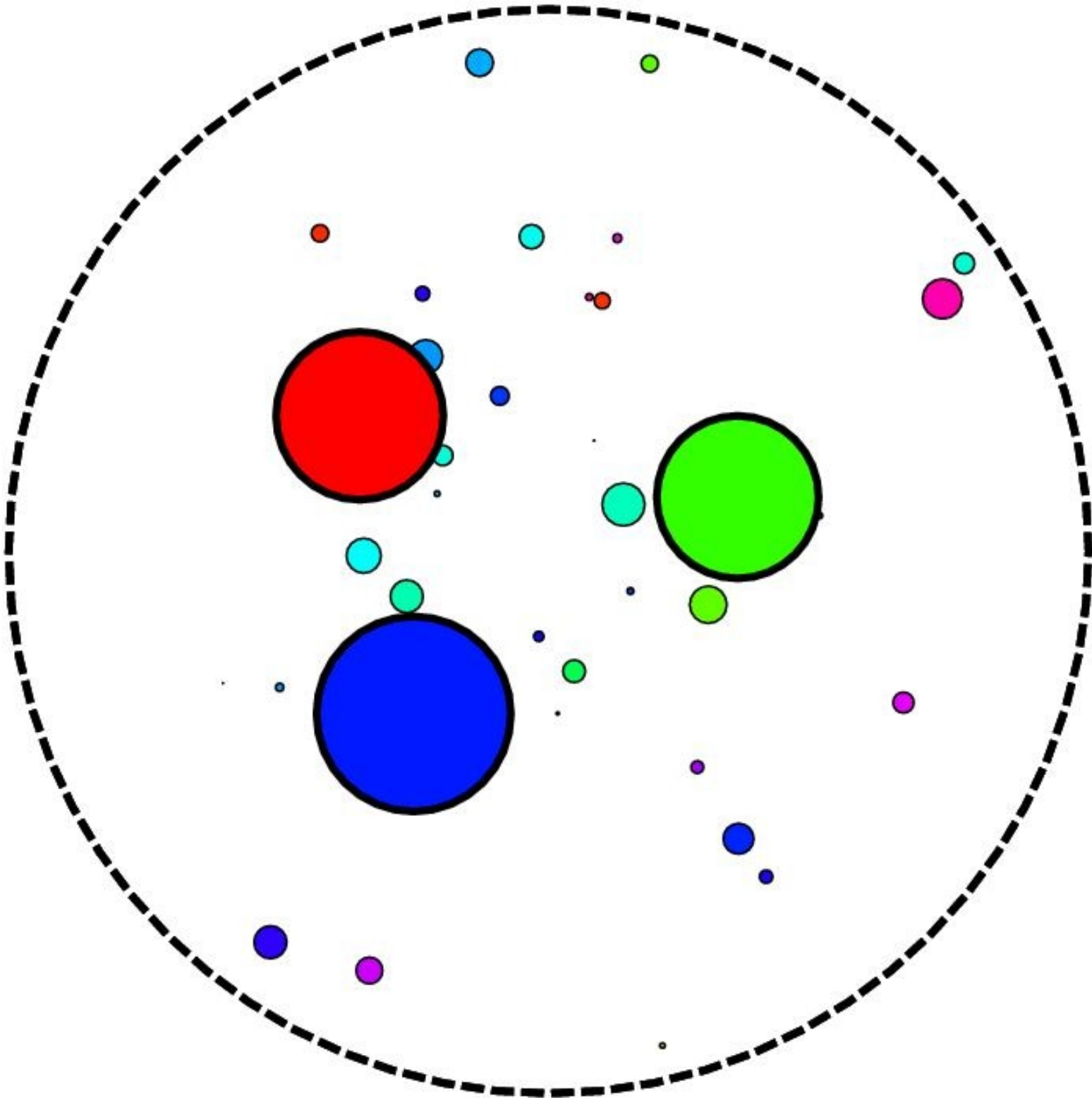
Basic Structure of  
a NON diffractive PP interactions  
is made of TWO STRINGS

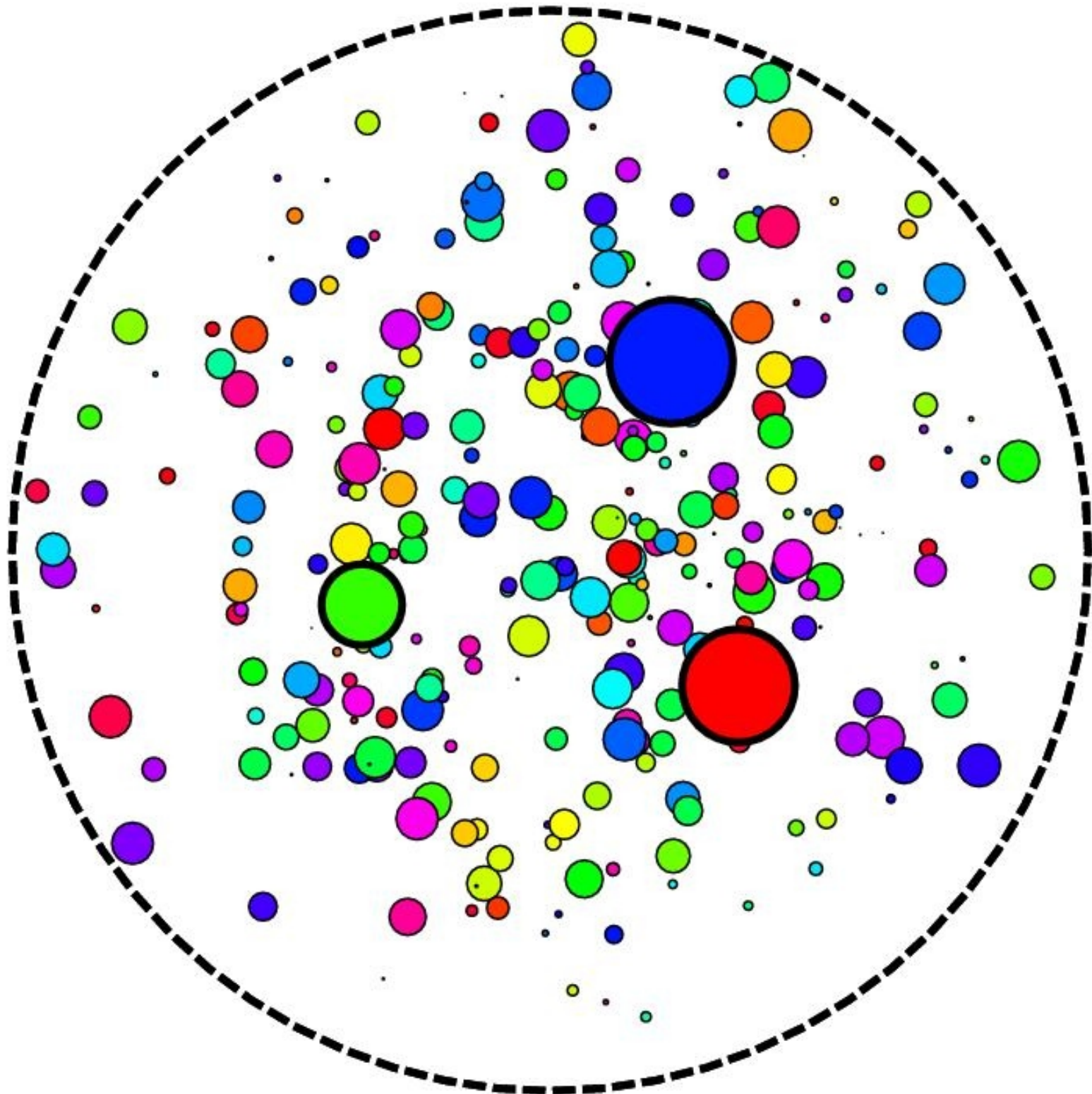
hard/semihard interactions  
result in additional strings

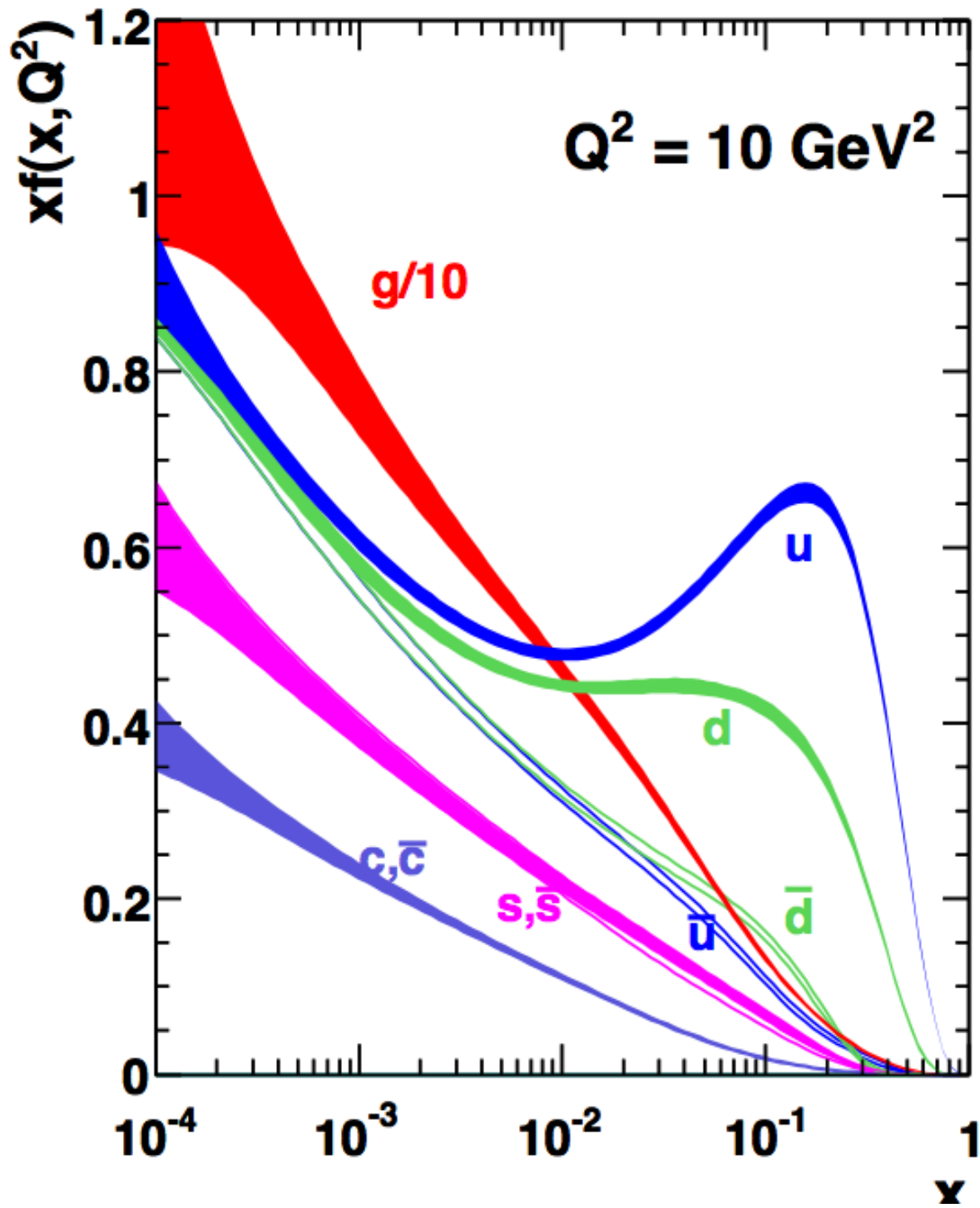
Color Structure

$$3 \otimes 3 = \bar{3} \oplus 6$$

$$3 \otimes \bar{3} = 1 \oplus 8$$



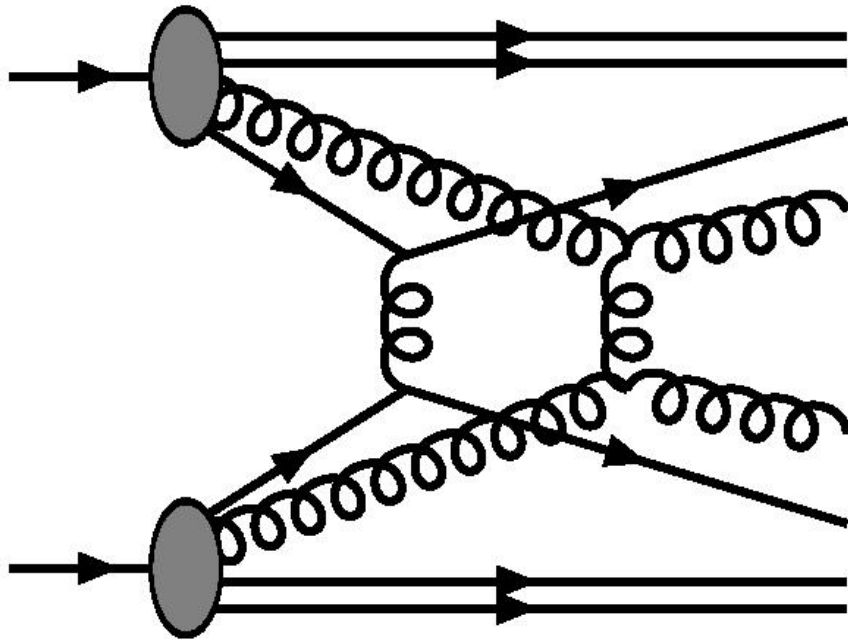




Parton  
Distribution  
Function

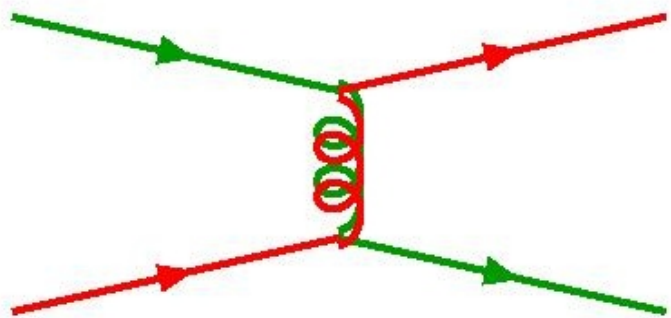
Typically 2 – 3 interactions/event  
at the Tevatron, 4 – 5 at the LHC,  
but may be more  
in “interesting” high- $p_{\perp}$  ones.

Pythia  
MC



Most particles in  
Fragmentation  
Regions  
Described by the  
“beam remnants  
strings”

# QCD $2 \rightarrow 2$



$$qq' \rightarrow qq'$$

$$q\bar{q} \rightarrow q'\bar{q}'$$

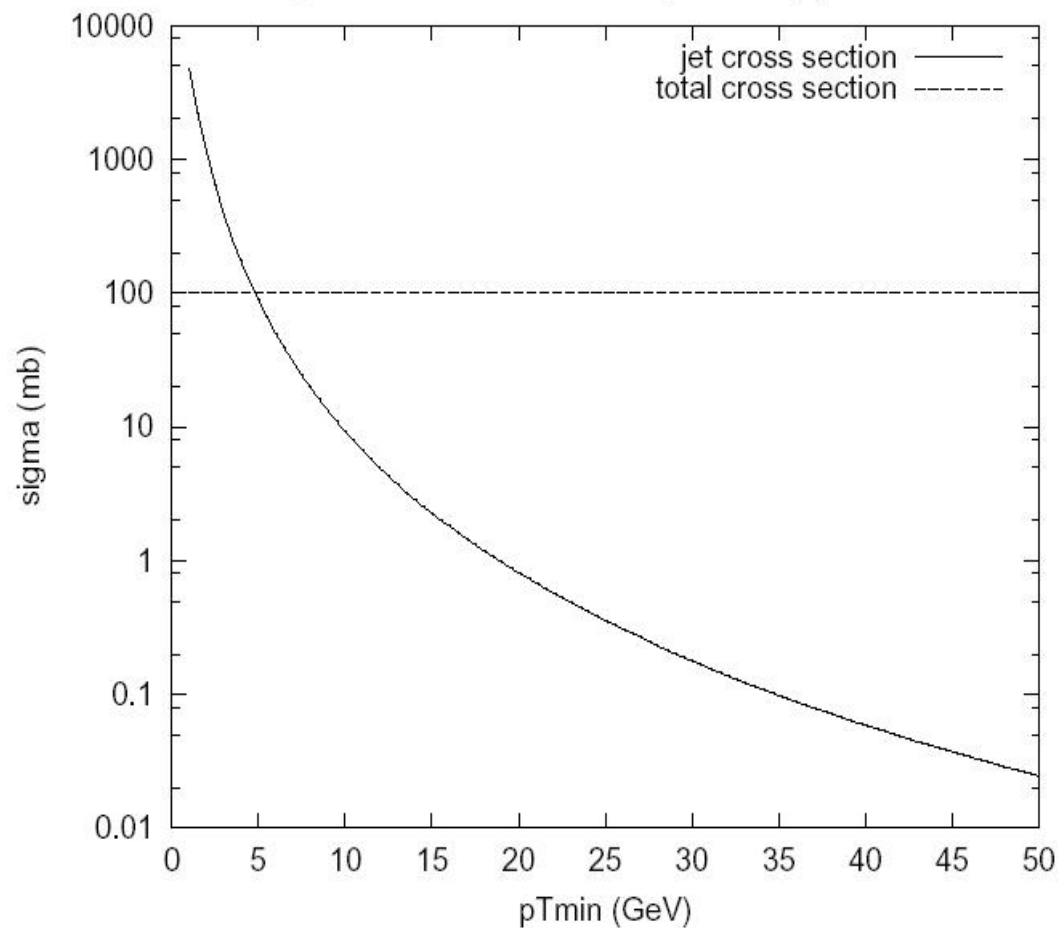
$$q\bar{q} \rightarrow gg$$

$$qg \rightarrow qg$$

$$gg \rightarrow gg$$

$$gg \rightarrow q\bar{q}$$

Integrated cross section above  $p_{Tmin}$  for pp at 14 TeV



$$d\sigma/dp_{\perp}^2 \approx 1/p_{\perp}^4 \text{ for } p_{\perp} \rightarrow 0.$$

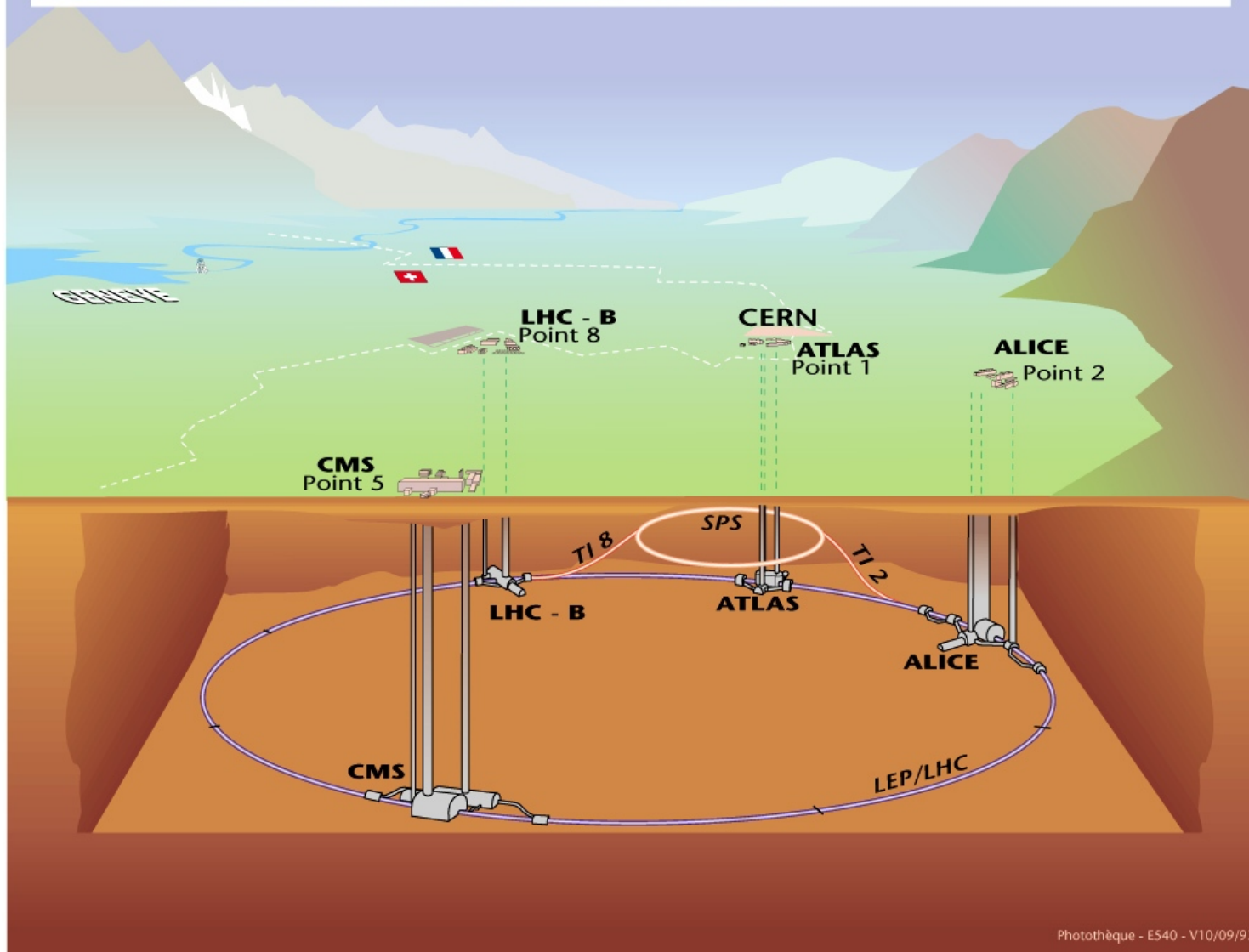
# MULTIPLE INTERACTIONS

- Estimate of the average number of Elementary interactions per pp scattering
- “Spatial Distribution” [proton spin] (Transverse coordinates) of the partonic constituents.
- Fluctuations of the “parton configuration” of an interacting hadron.

Beyond PDF's  
Parton Distribution Functions

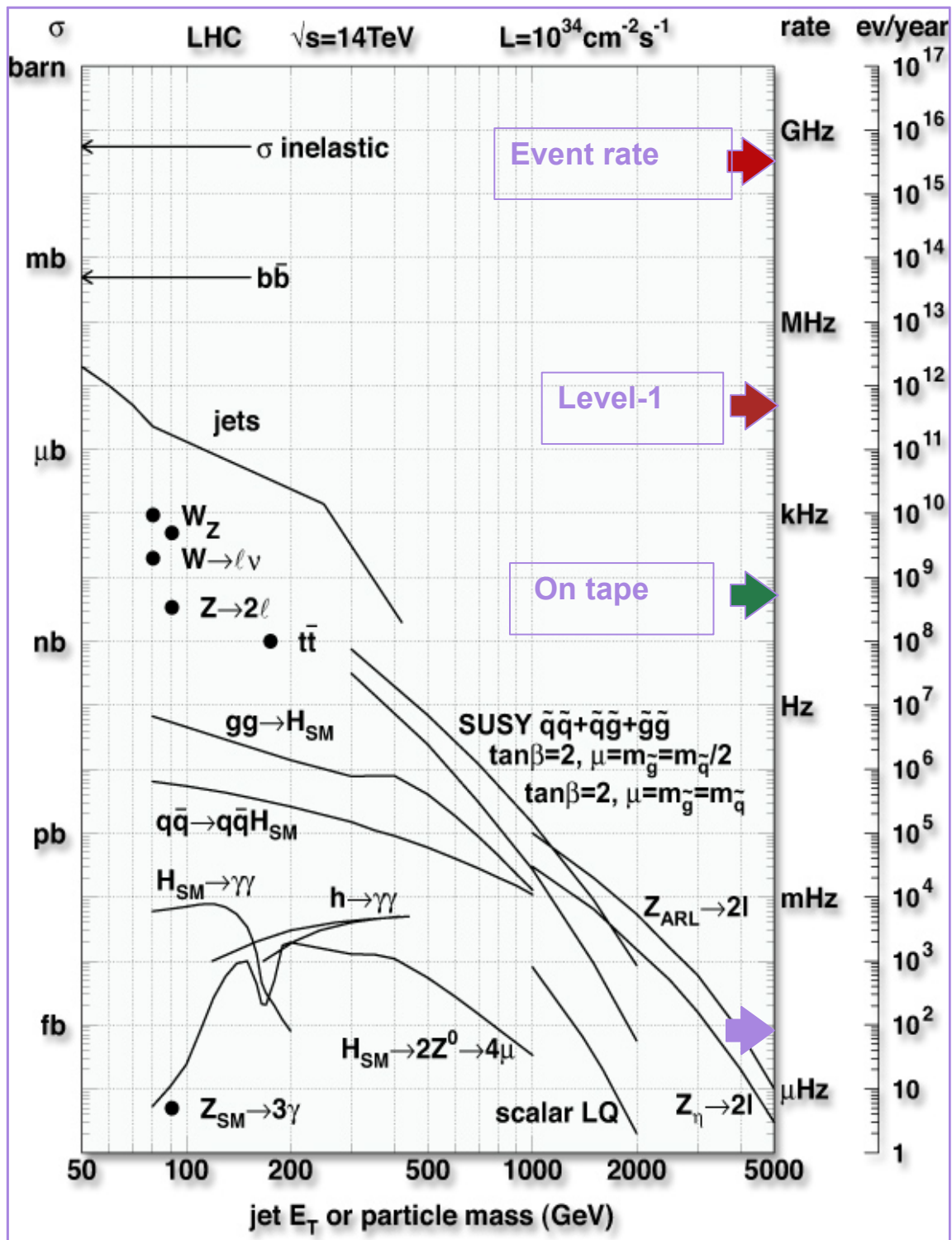
# Very Important potential of LHC

## Vue d'ensemble des expériences LHC.

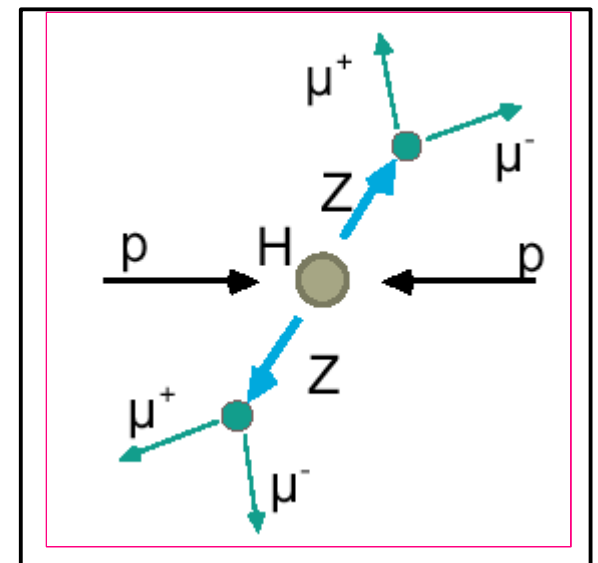


7 + 7 TeV  
PP collider





Higgs discovery golden channel



$\sigma_{\text{tot}}$  $\sigma_{\text{el}}$ 

$$\frac{d\sigma_{\text{el}}}{dt}$$

$$\frac{dN_{\text{ch}}}{dy}$$

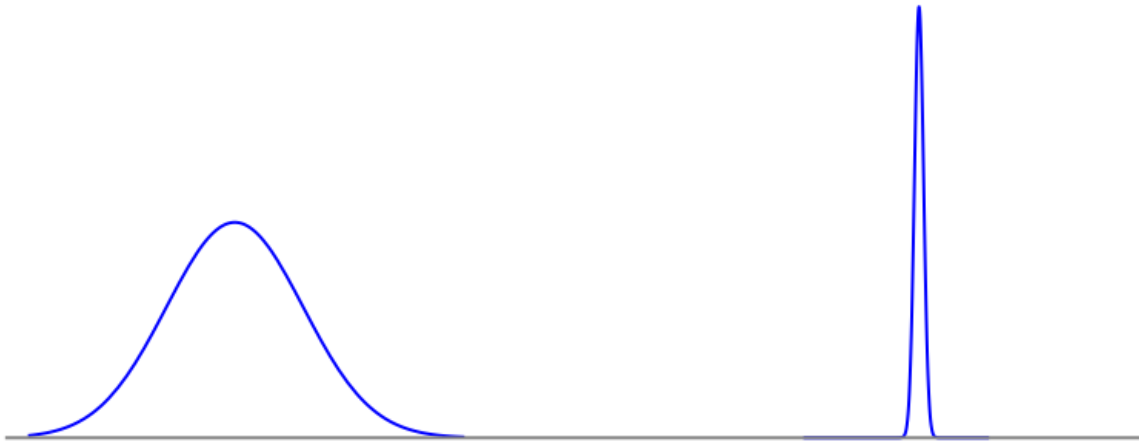
$$\frac{dN_{\text{ch}}}{d\eta}$$

$$\frac{dN_{\text{ch}}}{dp_{\perp} dy}$$

 $\sigma_{\text{diffractive}}$  $\sigma_{\text{FD}}$  $\sigma_{\text{BD}}$  $\sigma_{\text{DD}}$ 

$$\frac{d^2\sigma_{\text{diff}}}{dt dM_X^2}$$

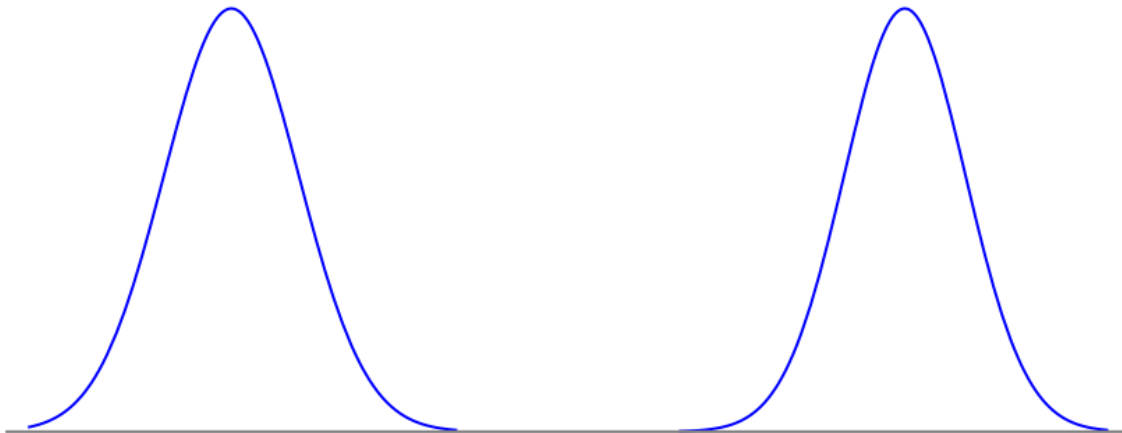
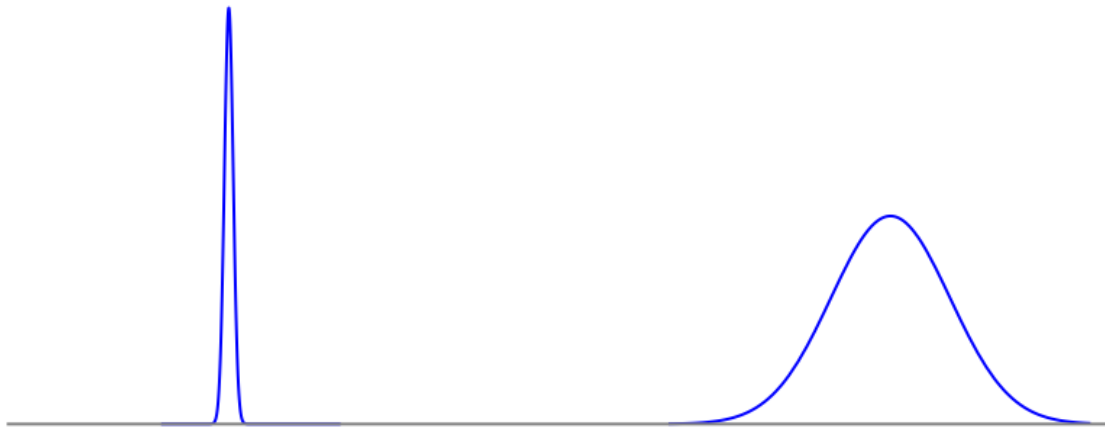
# Diffraction



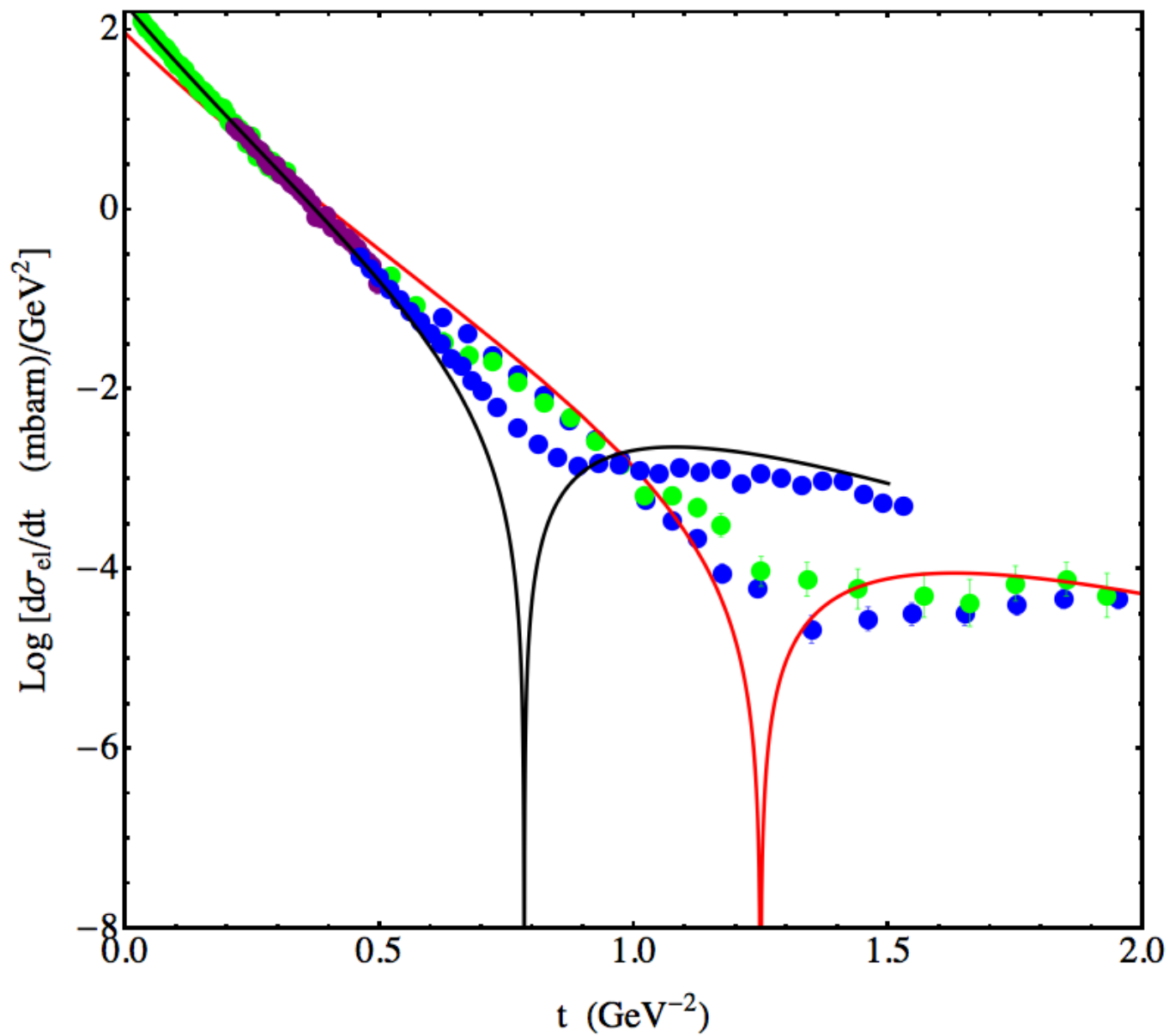
$h_1 h_2 \rightarrow h_1^* h_2$  (beam diffraction),

$h_1 h_2 \rightarrow h_1 h_2^*$  (target diffraction),

$h_1 h_2 \rightarrow h_1^* h_2^*$  (double diffraction).

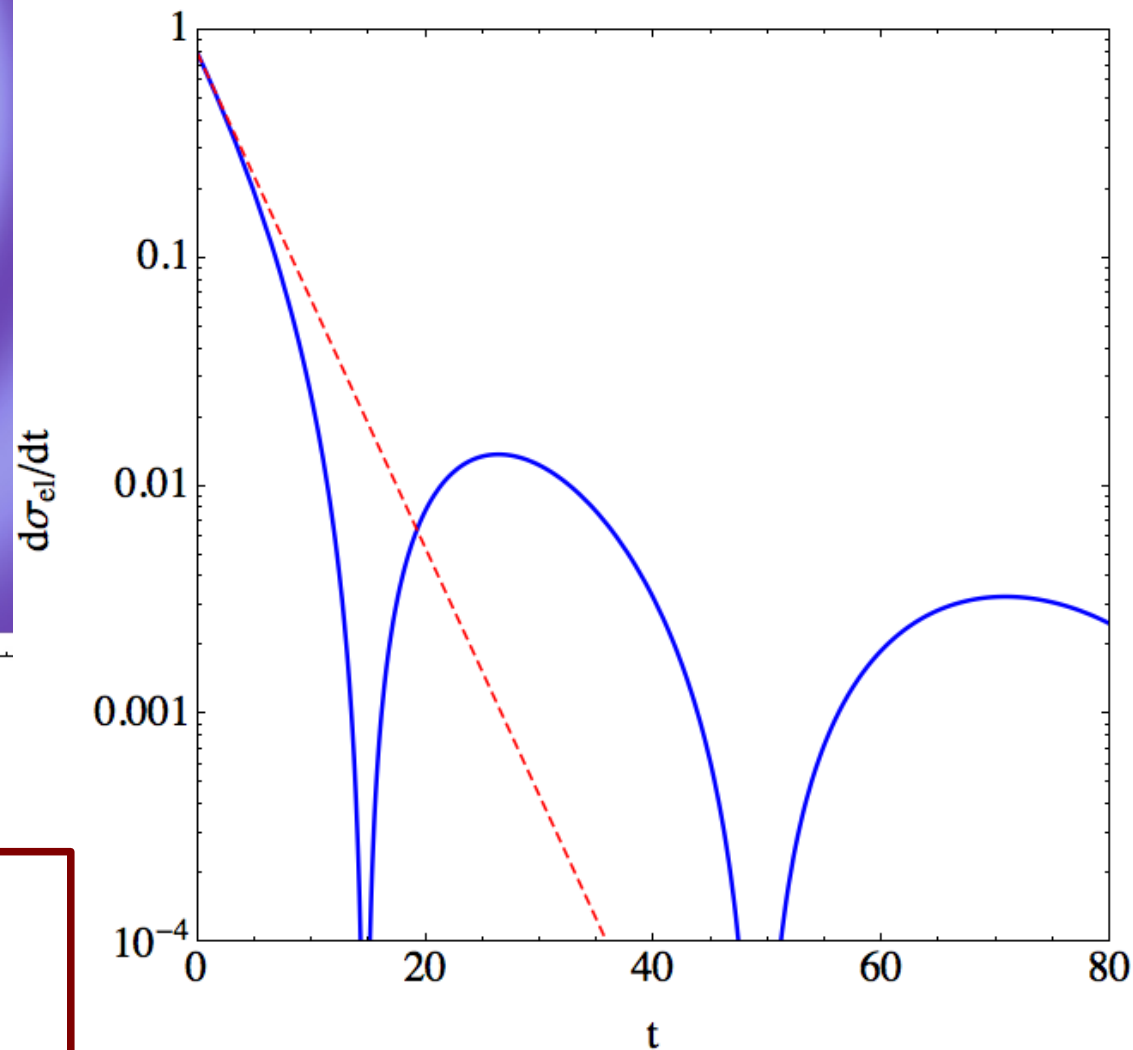
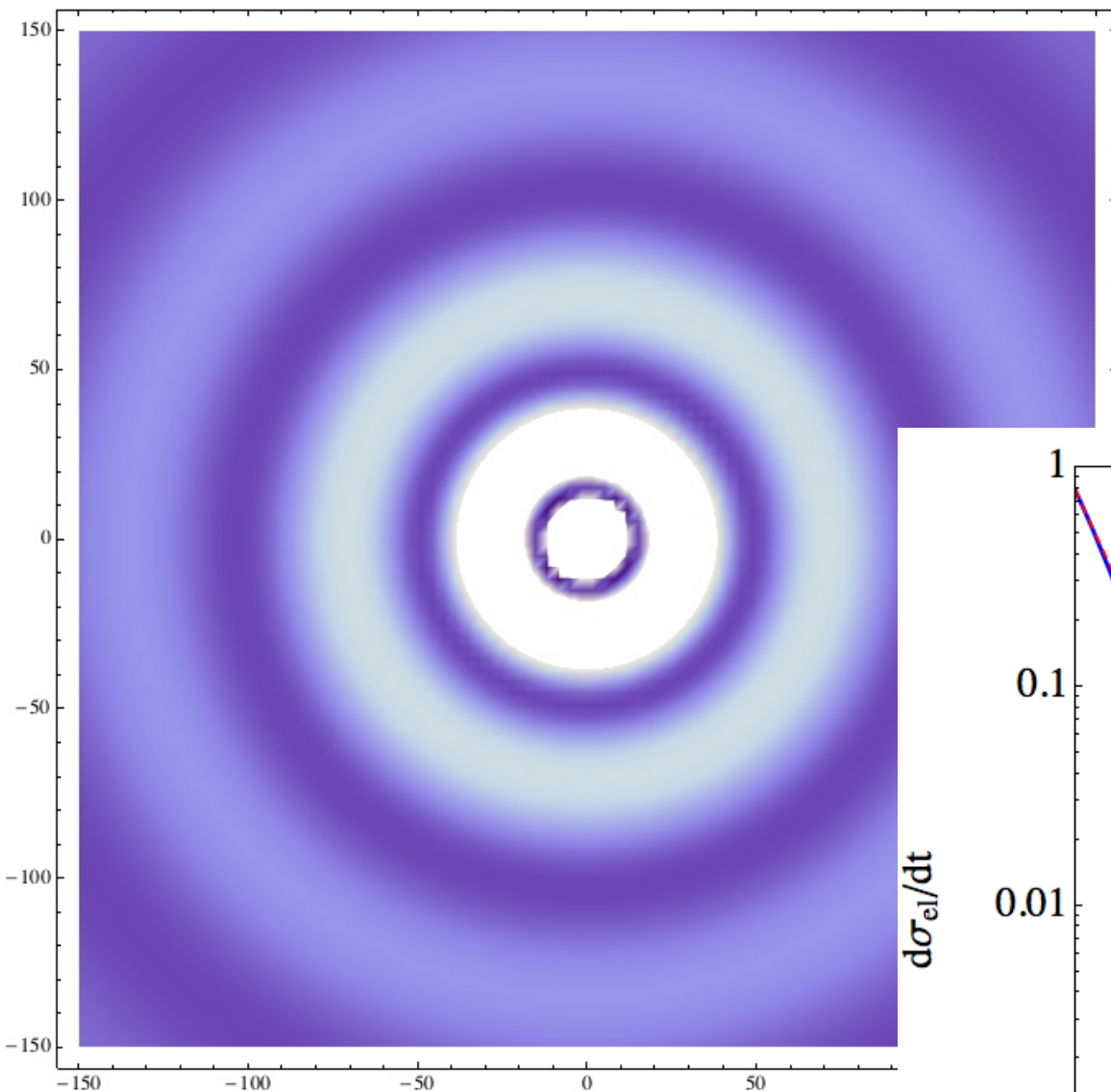


ISR 62.3 GeV  
CERN UA4 546 GeV



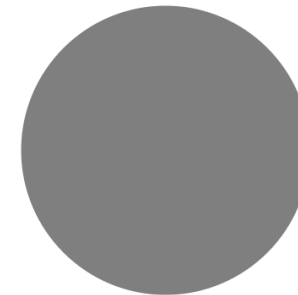
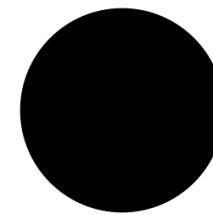
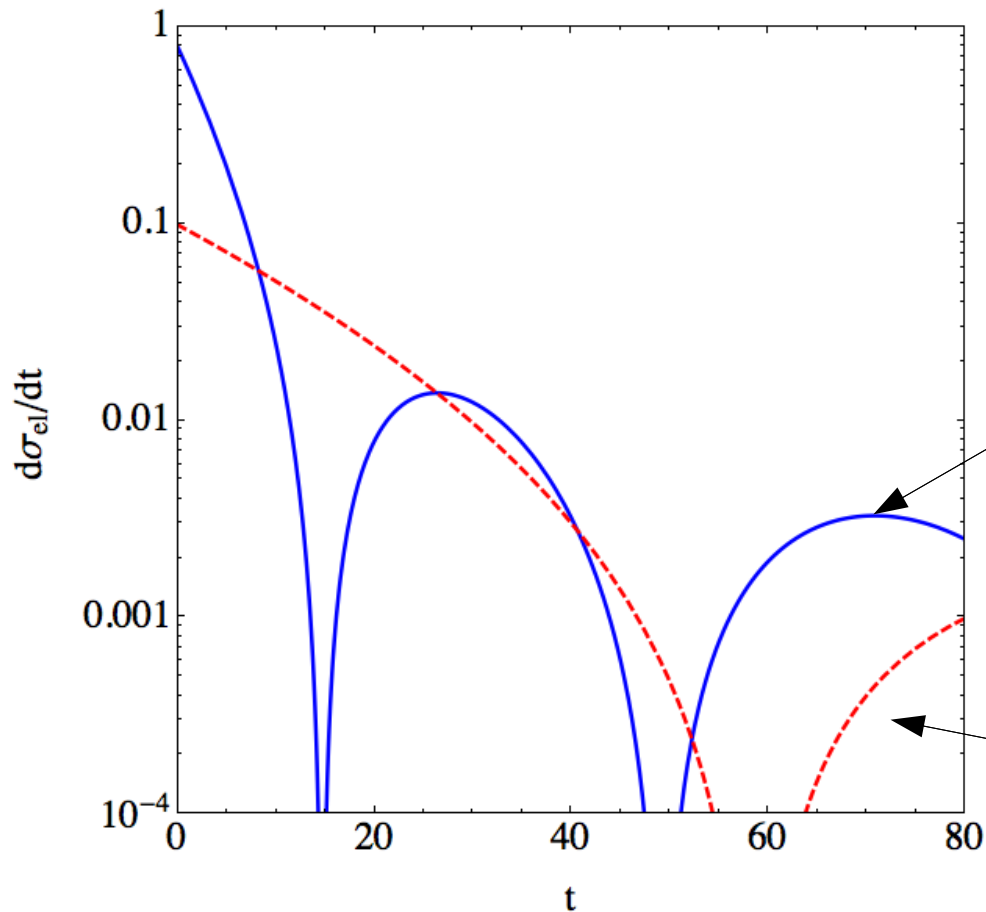
Black Disk  
Of radius R.

Diffraction Pattern



$$\sigma_{el} = \sigma_{abs} = \pi R^2$$

# Elastic scattering distributions



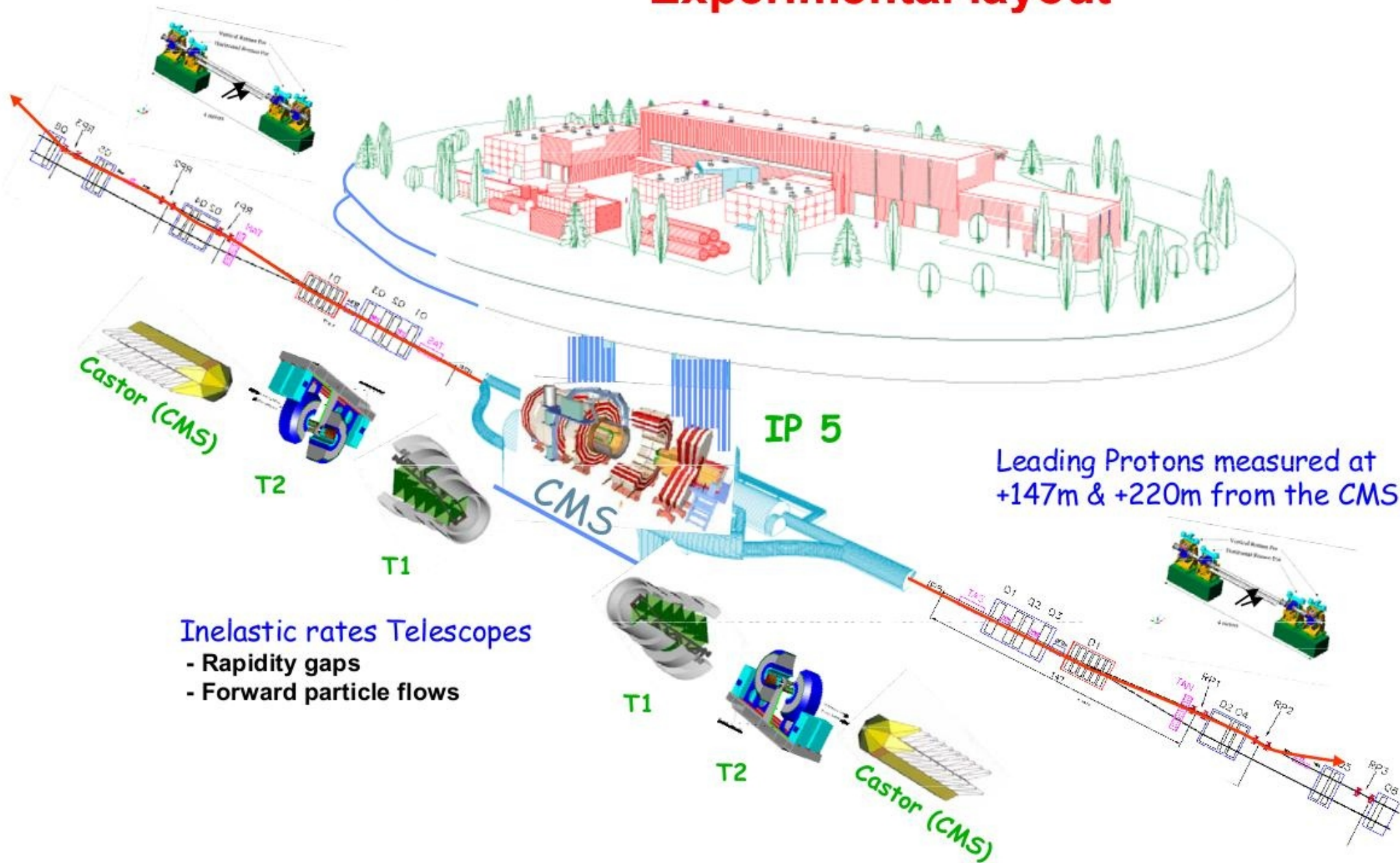
Larger  
Gray Disk

smaller  
Black Disk

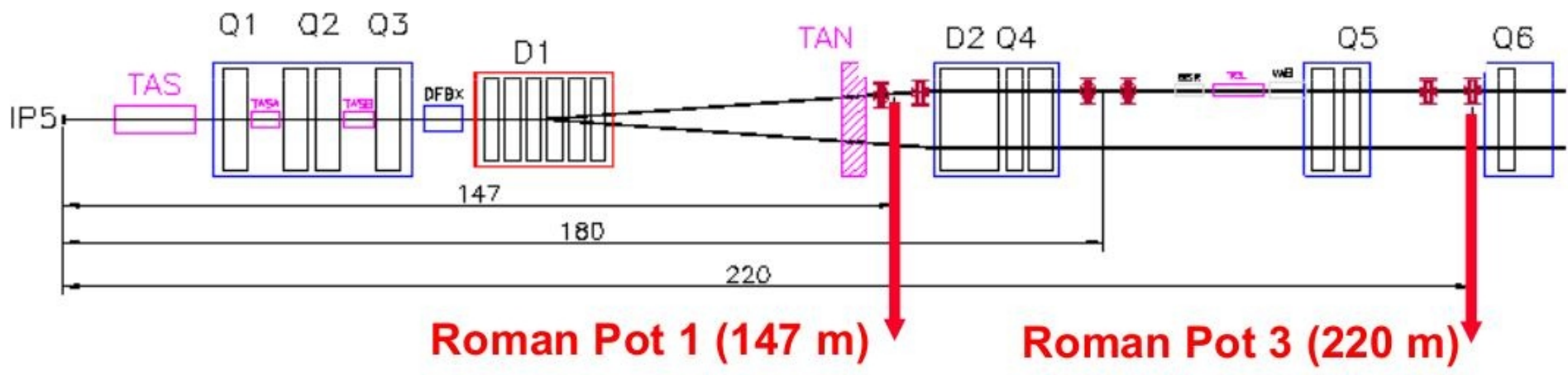
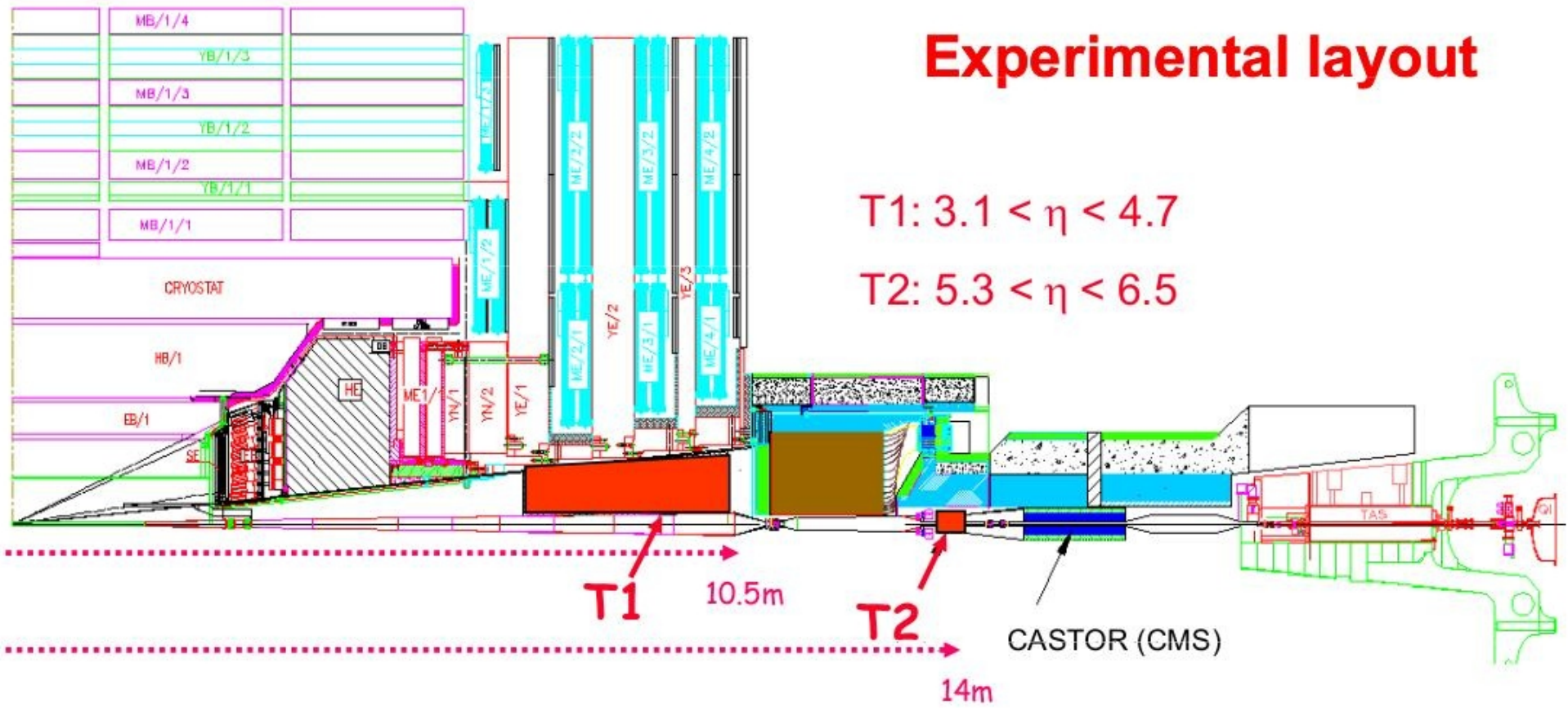
$$\sigma_{el} = \frac{\sigma_{tot}^2 (1 + \rho^2)}{16\pi B_{el}}$$

Leading Protons measured at  
-220m & -147m from the CMS

## Experimental layout



## Experimental layout





# CROSS SECTION MEASUREMENT

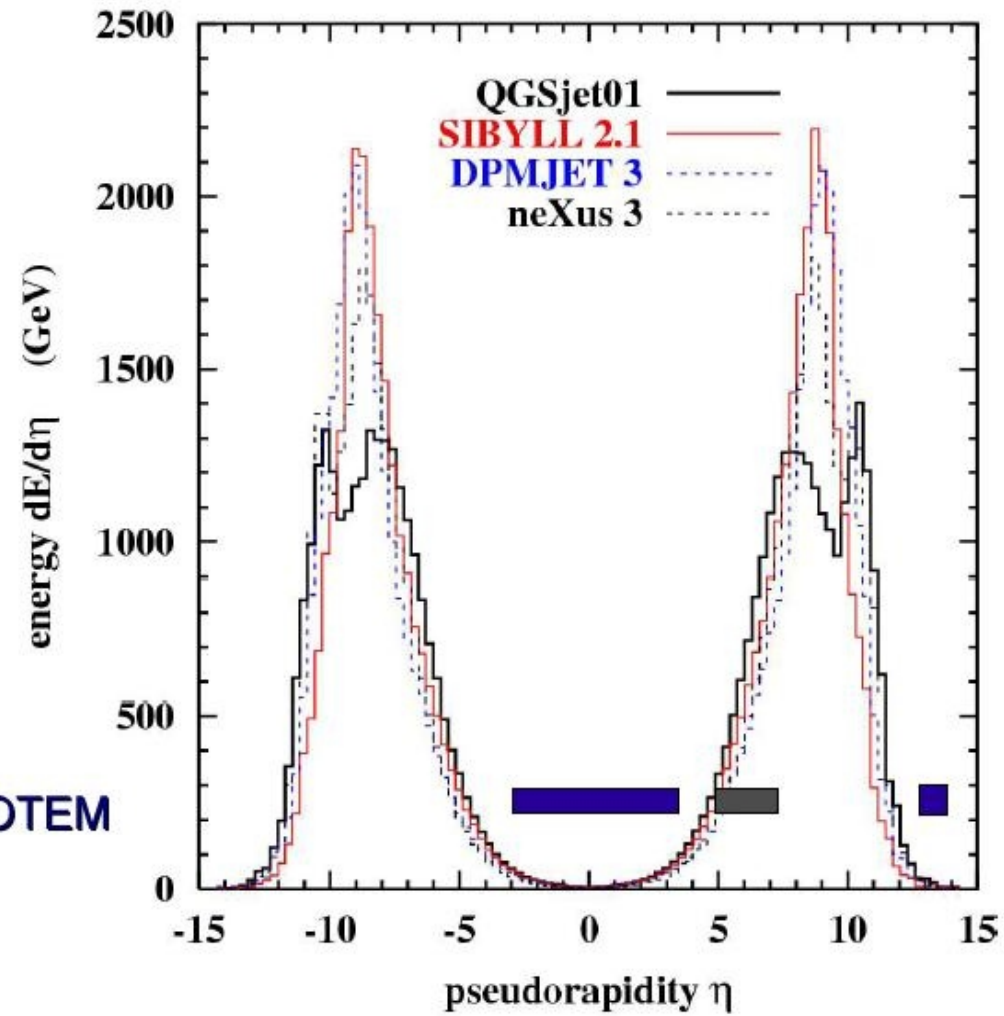
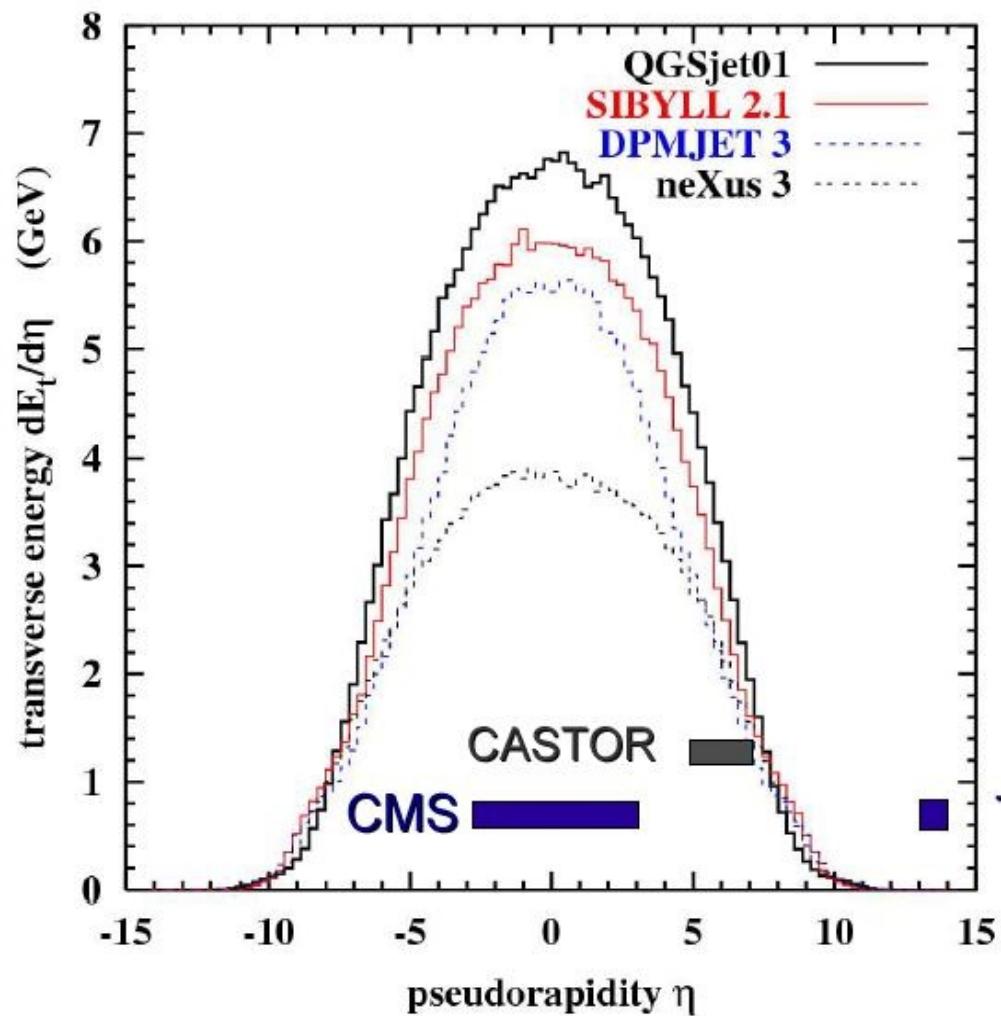
$$\mathcal{L} \sigma_{tot}^2 = \frac{16 \pi}{1 + \rho^2} \times \left. \frac{dN_{el}}{dt} \right|_{t=0} \quad \text{Optical Theorem}$$

$$\mathcal{L} \sigma_{tot} = N_{el} + N_{inel}$$

$$\sigma_{tot} = \frac{16 \pi}{1 + \rho^2} \times \frac{\left( dN_{el} / dt \right) \Big|_{t=0}}{N_{el} + N_{inel}}$$

$$\mathcal{L} = \frac{1 + \rho^2}{16 \pi} \frac{\left( N_{el} + N_{inel} \right)^2}{\left( dN_{el} / dt \right) \Big|_{t=0}}$$

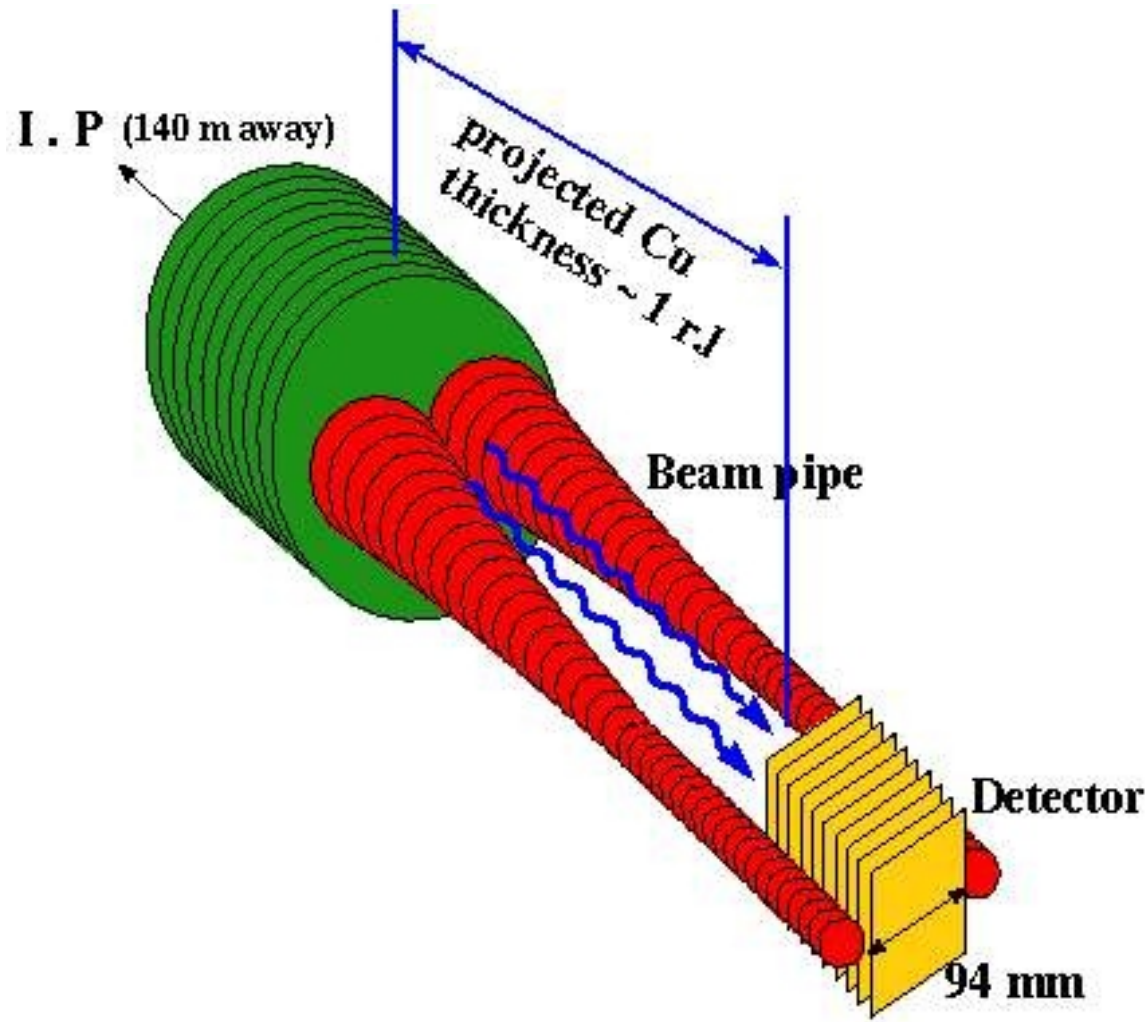
[Luminosity Determination]



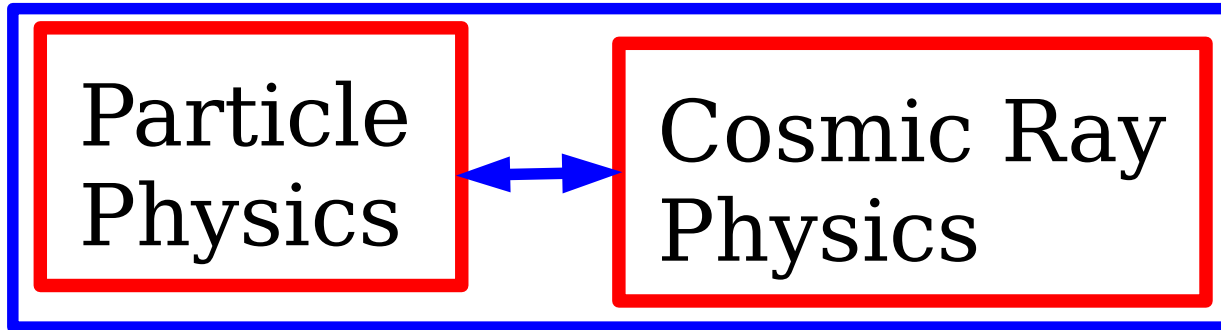
**PROBLEM of PHASE SPACE COVERING**

# LHCF

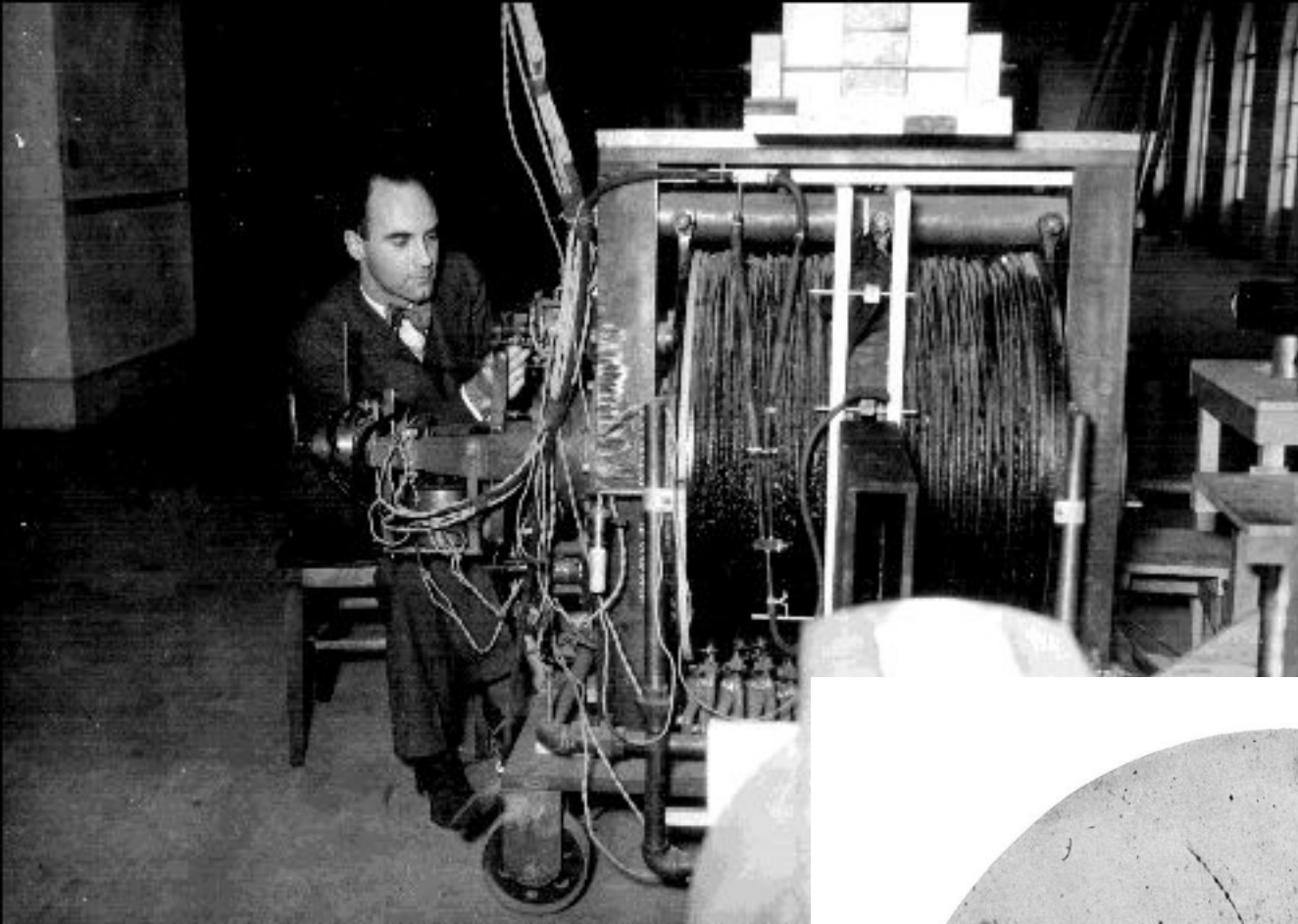
Calorimeter  
for neutral particles  
in the very forward region



Two  
non-identical  
Detectors



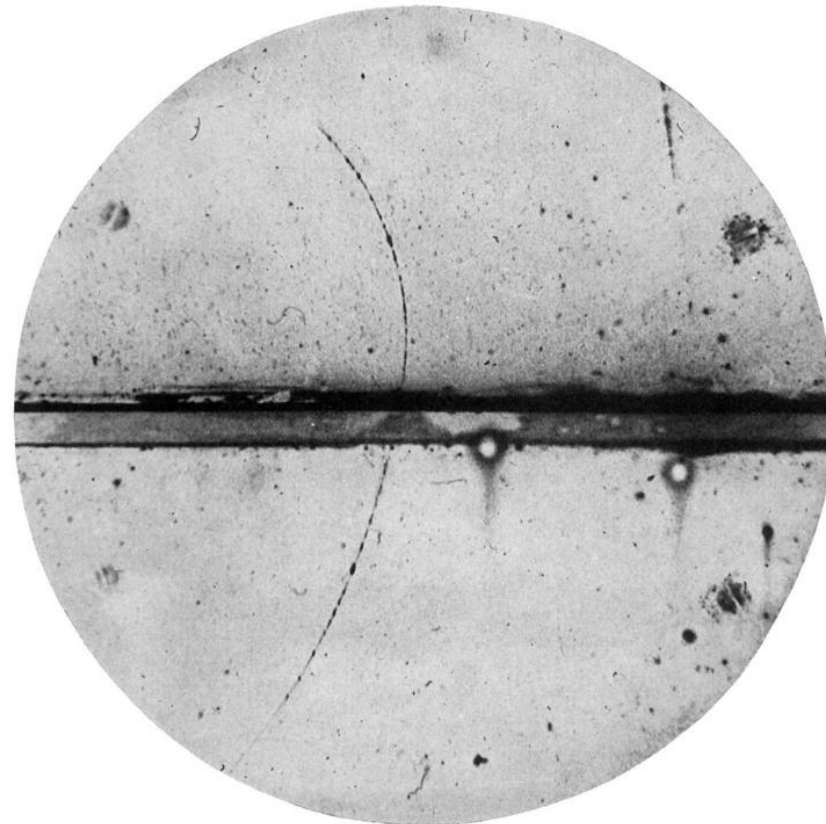
A long Common History



Carl Anderson  
(february 1933)

Near his  
"Wilson chamber"

© Copyright California Institute of Technolog  
Commercial use or modification of this ma

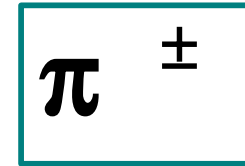
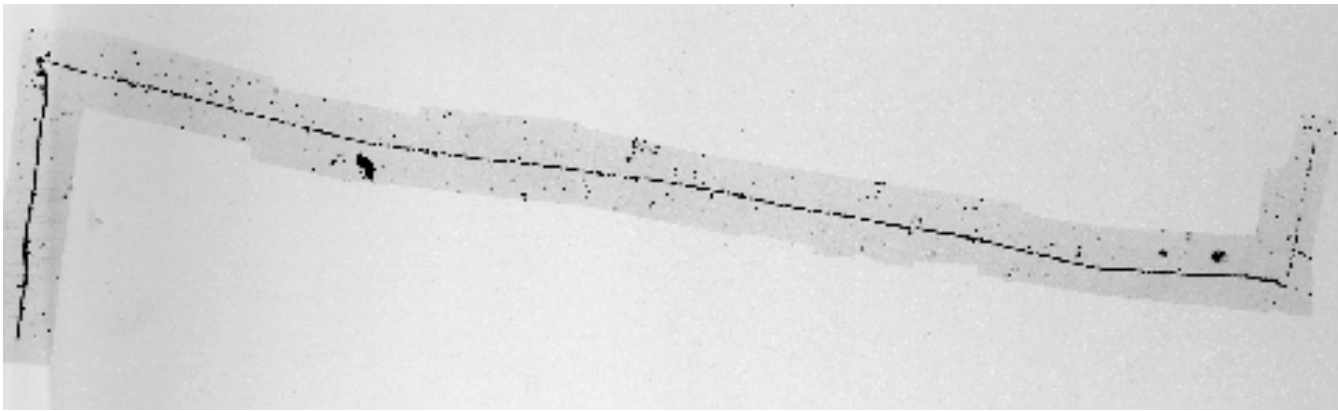


23 MeV

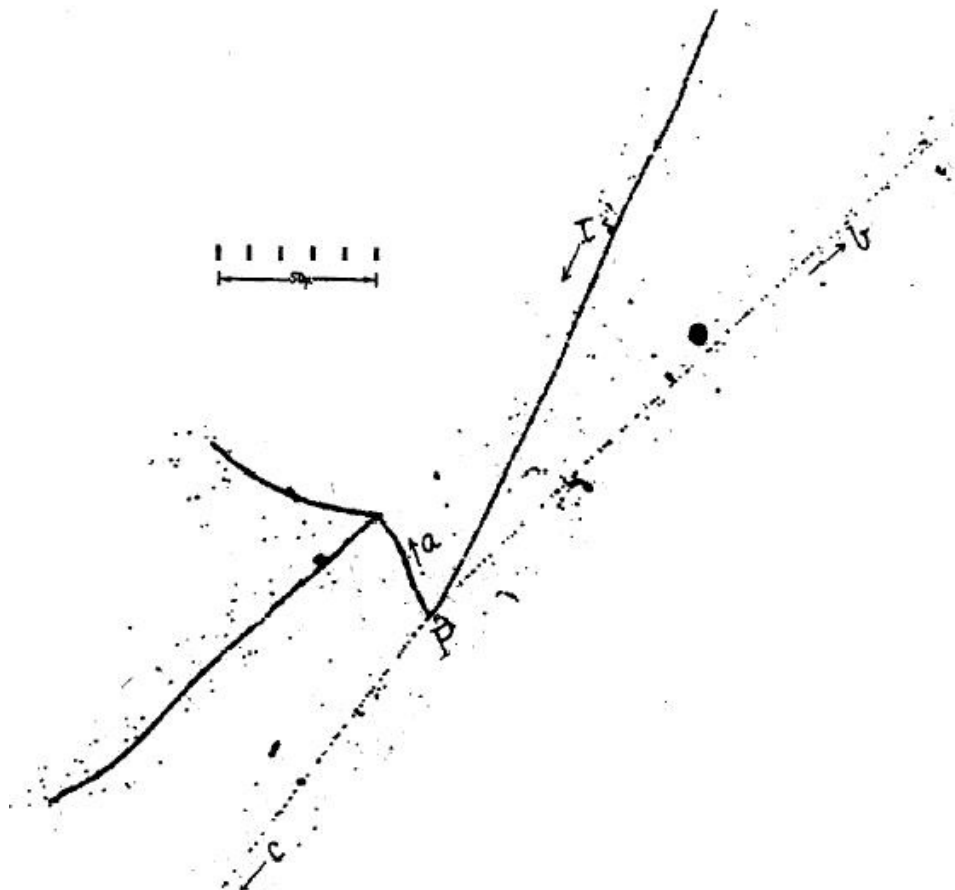
6 mm  
Lead plate

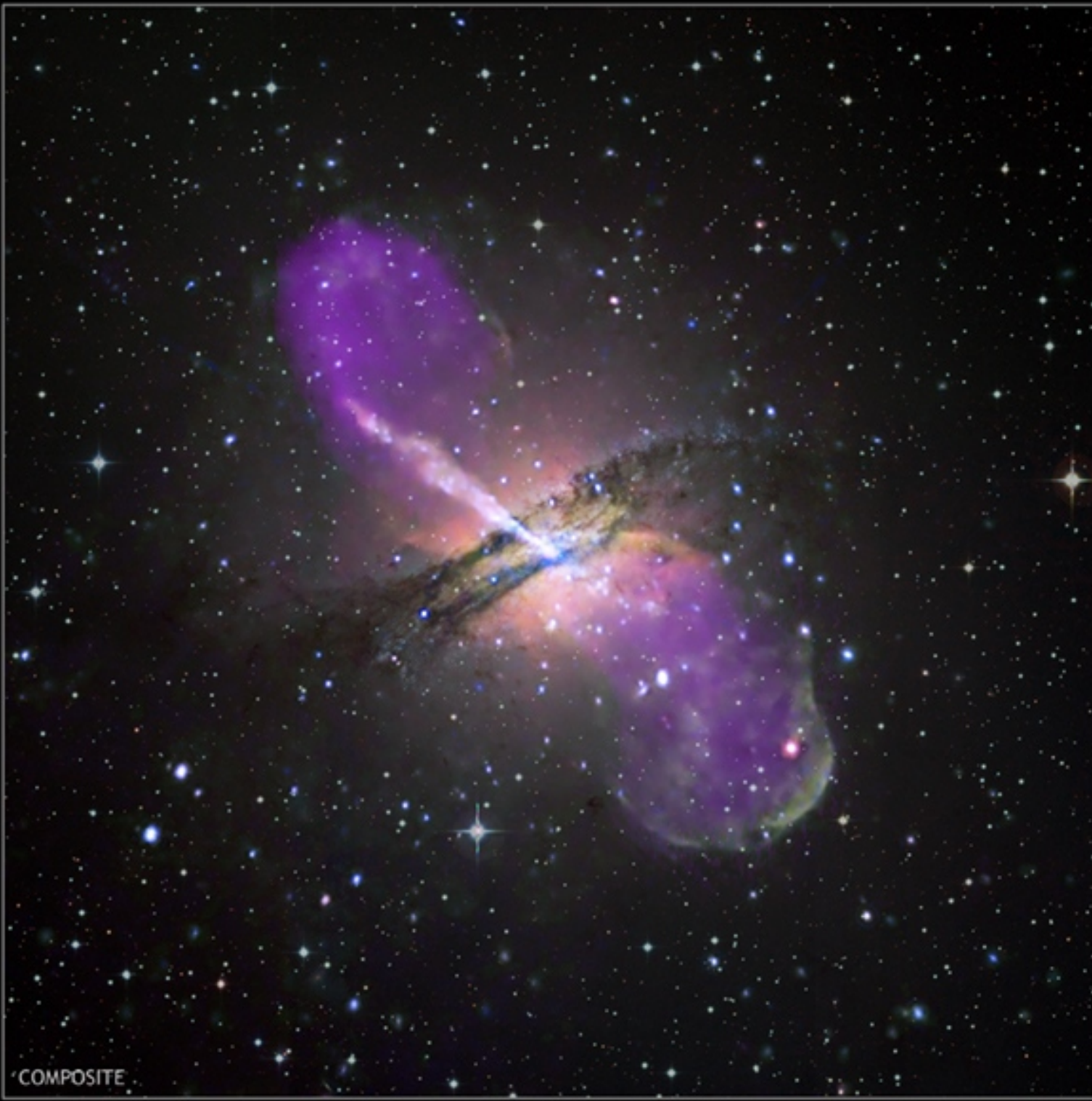
63 MeV

Discovery of the  
POSITRON



Occhialini , Powell





COMPOSITE

X-RAY

RADIO

OPTICAL

We are studying at the same time

“Gigantic Astrophysical Beasts”

Millions of light years away

Length scale  $10^{+24}$  cm

Microscopic

Partonic constituents of matter

Length scale  $10^{-13}$  cm

Exciting

Difficult



Many Questions....

The fascinating “Intellectual Adventure”  
of exploring and understanding  
the “High Energy Universe” is continuing.

Many Questions....

The fascinating “Intellectual Adventure” of exploring and understanding the “High Energy Universe” is continuing.

I believe that Gianni Navarra continues to contribute to this scientific “quest”.

- Via the observatories he contributed to build and that continue to produce new data (and surprises).
- In the activities of community of younger scientists he played a crucial role to form [thanks for organizing this meeting!]
- In the ideas and enthusiasm he communicated to so many of us (including me...).